

## Market Rule Amendment Proposal Form

### Part 1 - Market Rule Information

Identification No.:	MR-00481-R08
Subject:	Market Renewal Program - Final Alignment
Title:	Chapter 0.7 Appendices – System Operations and Physical Markets
Nature of Proposal:	<input type="checkbox"/> Alteration <input type="checkbox"/> Deletion <input checked="" type="checkbox"/> Addition
Chapter:	0.7
Appendix:	0.7
Sections:	All
Sub-sections proposed for amending:	Various
Current Market Rules Baseline:	

### Part 2 - Proposal History

Version	Reason for Issuing	Version Date
1.0	Draft for Stakeholder Review	June 7, 2024
2.0	Draft for Technical Panel Review	July 2, 2024
3.0	Publish for Stakeholder Review and Comment	July 17, 2024

Version	Reason for Issuing	Version Date
4.0	Submitted for Technical Panel Vote	September 3, 2024
5.0	Recommended by the Technical Panel; submitted for IESO Board review	September 10, 2024

Approved Amendment Publication Date:

Approved Amendment Effective Date:

### Part 3 - Explanation for Proposed Amendment

Provide a brief description that includes some or all of the following points:

- The reason for the proposed amendment and the impact on the IESO-administered markets if the amendment is not made.
- Alternative solutions considered.
- The proposed amendment, how the amendment addresses the above reason and impact of the proposed amendment on the IESO-administered markets.

### Summary

The IESO proposes to amend the market rules to support the implementation of the Market Renewal Program (MRP), via the Final Alignment (FA) Batch.

The FA Batch consolidates all Technical Panel provisionally recommended/IESO Board provisionally approved market rule amendments, with three types of further modifications:

1. Updates or corrections to earlier batches resulting from the ongoing implementation and engagement processes;
2. Transitional market rules required to facilitate the mechanics of transitioning from the old market to the renewed market; and
3. Administrative “conforming change” – to reflect any updates or corrections, e.g. update to references and defined terms.

This proposal is based on input from various stakeholder engagement initiatives for the Market Renewal Program.

Further information on MRP can be found on the IESO’s [Market Renewal webpage](#).

### Background

Previous drafts of MRP market rule amendments have been provisionally approved by the IESO Board. The Final Alignment batch consolidates these provisionally approved amendments, with amendments where required, into a single batch that will follow the

formal process for market rule amendments, including a formal vote by Technical Panel to recommend the market rules for IESO Board consideration, and formal approval by the IESO Board.

Given the scope of changes being proposed by MRP, each market rule chapter is impacted. The Final Alignment batch is structured such that there is a proposal for each chapter, with separate proposals for appendices 7 and 9.

The implementation of MRP will require two parallel sets of market rules to exist concurrently; the legacy market rules and the renewed market rules. The renewed market rules, which these proposals will create, will be labelled with unique chapter numbers to delineate them from the legacy market rules. A new section A, and in some chapters a section B, details the transitional nature of the two sets of market rules. As the renewed market rules are new chapters, there are no changes tracked. For a tracked changes view compared against the current market rules baseline, please refer to the MRP [Final Alignment](#) page.

## Discussion

The accompanying ["Summary of Changes - Final Alignment \(Readers Guide\)"](#) provides a summary of the market rule amendments to the market rules.

## Part 4 - Proposed Amendment

# Appendix 7.1 – Energy Offer, Schedule or Forecast Information

## 1.1 Energy Offers/Schedules/Forecasts from Generation Resources

- 1.1.1 In order for a *generation resource* to provide *energy*, its *registered market participant* shall submit an *offer*, schedule or forecast, as applicable that includes, at a minimum, the information specified in this section 1.1.
- 1.1.2 *Resource* name.
- 1.1.3 *Registered market participant*.
- 1.1.4 *Dispatch day* and *dispatch hour(s)* for which *offer*, schedule or forecast applies.
- 1.1.5 For a *dispatchable generation resource*, two to twenty *price-quantity pairs* for each *dispatch hour*, the final of which represents the maximum quantity of the *offer*.
- 1.1.6 For a *dispatchable generation resource*, one to five sets of ramp quantity and its corresponding ramp up and ramp down values for each *dispatch hour* applicable to the entire range of the *resources* output contained in the *offer*.
- 1.1.7 Is this a standing *offer*, schedule or forecast? Yes/No. If Yes, Date To: \_\_\_\_\_  
For which day(s) of the week? \_\_\_\_\_
- 1.1.8 For a *dispatchable generation resource* other than a *quick-start resource* or a nuclear *generation resource*:
  - 1.1.8.1 a *minimum loading point*;
  - 1.1.8.2 a *minimum generation block run-time*;
  - 1.1.8.3 a *minimum generation block down-time* for each *thermal state*;
  - 1.1.8.4 a *lead time* for each *thermal state*; and
  - 1.1.8.5 ramp up energy to *minimum loading point* for each *thermal state*.



## 1.2 Energy Offers from Imports

- 1.2.1 In order for a *boundary entity resource* to provide *energy* from an import, its *registered market participant* shall submit an *offer* that includes, at a minimum, the information specified in this section 1.2.
- 1.2.2 Unique *boundary entity* identifier (*interconnection* and *boundary entity resource*).
- 1.2.3 *Registered market participant*.
- 1.2.4 *Dispatch day* and *dispatch hour(s)* for which *offer* applies.
- 1.2.5 Two to twenty *price-quantity pairs* for each *dispatch hour*, the final of which represents the maximum quantity of the *offer*.
- 1.2.6 Is this a standing *offer*? – Yes/No. If Yes, Date To: \_\_\_\_\_ For which day(s) of the week? \_\_\_\_\_
- 1.2.7 Source *control area* (determined by selecting appropriate *boundary entity resource*).
- 1.2.8 e-Tag identification.
- 1.2.9 Notwithstanding MR Ch.7 s.3.3, e-Tags shall be submitted within the times outlined in the *IESO* interchange tagging procedures and in accordance with the following:
  - 1.2.9.1 all *resources* shall be designated as firm for the Ontario flowgates and the Ontario portion of the *intertie* flowgates;
  - 1.2.9.2 each *registered market participant* shall submit its e-Tag to the *IESO* through the electronic information system sanctioned by the relevant *standards authority* or, when not available, by such alternative means as may be specified by the *IESO* consistent with the policies of the relevant *standards authority*; and
  - 1.2.9.3 interchange scheduling defaults specified by the relevant *standards authority* shall be used unless otherwise approved by the *IESO*. Transactions shall be one hour in duration, in accordance with agreements between *control areas* along the path. Transactions shall ramp in/out over the hour and shall respect a ten-minute ramp period.
- 1.2.10 Capacity transaction parameter, if applicable.

## **1.3 Energy Offers for Virtual Zonal Resources**

- 1.3.1 In order for a *virtual zonal resource* to participate in the *day-ahead market*, its *registered market participant* shall submit an *offer*, that includes, at a minimum, the information specified in this section 1.3.
- 1.3.2 *Virtual trader*.
- 1.3.3 *Virtual transaction* type indicating an *offer*.
- 1.3.4 *Virtual zonal resource*.
- 1.3.5 *Dispatch day* and *dispatch hour(s)* for which the *offer* applies.
- 1.3.6 For a *virtual zonal resource*, two to twenty *price-quantity pairs* for each *dispatch hour*, the final of which represents the maximum quantity of the *offer*.

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## Appendix 7.2 – Energy Bid Information

### 1.1 Energy Bids from Load Resources

- 1.1.1 In order for a *dispatchable load* to provide *energy* or when other *load resources* are submitting *bids*, its *registered market participant* shall submit a *bid* that includes, at a minimum, the information specified in this section 1.1.
- 1.1.2 *Resource name.*
- 1.1.3 *Registered market participant.*
- 1.1.4 *Dispatch day and dispatch hour(s)* for which *bid* applies.
- 1.1.5 Two to twenty *price-quantity pairs* for each *dispatch hour*, the final of which represents the maximum quantity of the *bid*.
- 1.1.6 For *load resources*, excluding *price responsive loads*, one to five ramp sets of ramp quantity and its corresponding ramp up and ramp down values for each *dispatch hour* applicable to the entire range of *load* contained in the *bid*.
- 1.1.7 Is this a standing *bid*? Yes/No. If Yes, Date To: \_\_\_\_\_ For which day(s) of the week? \_\_\_\_\_

### 1.2 Energy Bids from Exports

- 1.2.1 In order for a *boundary entity resource* to provide *energy* from an export, its *registered market participant* shall submit an *bid* that includes, at a minimum, the information specified in this section 1.2.
- 1.2.2 Unique *boundary entity* identifier (interconnection and *boundary entity resource*).
- 1.2.3 *Registered market participant name.*
- 1.2.4 *Dispatch day and dispatch hour(s)* for which *bid* applies.
- 1.2.5 Two to twenty *price-quantity pairs* for each *dispatch hour*, the final of which represents the maximum quantity of the *bid*.
- 1.2.6 Is this a standing *bid*? – Yes/No. If Yes, Date To: \_\_\_\_\_ For which day(s) of the week? \_\_\_\_\_
- 1.2.7 Sink *control area* (determined by selecting appropriate *boundary entity resource*).

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- 1.2.8 e-Tag identification.
- 1.2.9 Notwithstanding MR Ch.7 s.3.3, e-Tags shall be submitted within the times outlined in the *IESO* interchange tagging procedures and in accordance with the following:
- 1.2.9.1 all *resources* shall be designated as firm for the Ontario flowgates and the Ontario portion of the *intertie* flowgates;
  - 1.2.9.2 each *registered market participant* shall submit its e-Tag to the *IESO* through the electronic information system sanctioned by the relevant *standards authority* or, when not available, by such alternative means as may be specified by the *IESO* consistent with the policies of the relevant *standards authority*; and
  - 1.2.9.3 interchange scheduling defaults specified by the relevant *standards authority* shall be used unless otherwise approved by the *IESO*. Transactions shall be one hour in duration, in accordance with agreements between *control areas* along the path. Transactions shall ramp in/out over the hour and shall respect a ten-minute ramp period.
- 1.2.10 Capacity transaction parameter (if applicable)

### **1.3 Energy Bids for Virtual Zonal Resources**

- 1.3.1 In order for a *virtual zonal resource* participate in the *day-ahead market*, its *registered market participant* shall submit a *bid*, that includes, at a minimum, the information specified in this section 1.3.
- 1.3.2 *Virtual trader*.
- 1.3.3 *Virtual transaction* type indicating a *bid*.
- 1.3.4 *Virtual zonal resource*.
- 1.3.5 *Dispatch day* and *dispatch hour(s)* for which the *bid* applies.
- 1.3.6 For a *virtual zonal resource*, two to twenty *price-quantity pairs* for each *dispatch hour*, the final of which represents the maximum quantity of the *bid*.

# Appendix 7.3 – Operating Reserve Offer Information

## 1.1 Operating Reserve Offers from Generation Resources

- 1.1.1 In order for a *generation resource* to provide *operating reserve*, its *registered market participant* shall submit an *offer* that includes, at a minimum, the information specified in this section 1.1.
- 1.1.2 *Resource name.*
- 1.1.3 *Registered market participant.*
- 1.1.4 *Dispatch day and dispatch hour(s) for which offer applies.*
- 1.1.5 *Operating reserve class.*
- 1.1.6 *Reserve loading point*
- 1.1.7 Two to five *price-quantity pairs* for all classes of *operating reserve* being offered in each *dispatch hour*, the final of which represents the maximum quantity of the *offer*.
- 1.1.8 One ramp rate applicable for all classes of *operating reserve* being offered in accordance with MR Ch.7 s.3.5.8.
- 1.1.9 Is this a standing *offer*? Yes/No. If Yes, Date To: \_\_\_\_\_ For which day(s) of the week? \_\_\_\_\_

## 1.2 Operating Reserve Offers from Imports

- 1.2.1 In order for a *boundary entity resource* to provide *operating reserve* from an import, its *registered market participant* shall submit an *offer* that includes, at a minimum, the information specified in this section 1.2.
- 1.2.2 Unique *boundary entity* identifier (*interconnection* and *boundary entity resource*).
- 1.2.3 *Registered market participant.*
- 1.2.4 *Dispatch day and dispatch hour(s) for which offer applies.*
- 1.2.5 *Operating reserve class.*

- 1.2.6 Two to five *price-quantity pairs* for each *dispatch hour* for each class of *operating reserve* being offered, the final of which represents the maximum quantity of the *offer*.
- 1.2.7 Is this a standing *offer*? – Yes/No. If Yes, Date To: \_\_\_\_\_ For which day(s) of the week? \_\_\_\_\_
- 1.2.8 Source *control area* (determined by selecting appropriate *boundary entity resource*).
- 1.2.9 e-Tag identification.
- 1.2.10 Notwithstanding MR Ch.7 s.3.3, e-Tags shall be submitted within the times outlined in the *IESO* interchange tagging procedures and in accordance with the following:
  - 1.2.10.1 all *resources* shall be designated as firm for the Ontario flowgates and the Ontario portion of the *intertie* flowgates; and
  - 1.2.10.2 each *registered market participant* shall submit its e-Tag to the *IESO* through the electronic information system sanctioned by the relevant *standards authority* or, when not available, by such alternative means as may be specified by the *IESO* consistent with the policies of the relevant *standards authority*.

### **1.3 Operating Reserve Offers from Dispatchable Loads**

- 1.3.1 In order for a *dispatchable load* to provide *operating reserve*, its *registered market participant* shall submit an *offer* that includes, at a minimum, the information specified in this section 1.3.
- 1.3.2 *Resource* name.
- 1.3.3 *Registered market participant*.
- 1.3.4 *Dispatch day* and *dispatch hour(s)* for which *offer* applies.
- 1.3.5 *Operating reserve* class.
- 1.3.6 Two to five *price-quantity pairs* for each *dispatch hour* for each class of *operating reserve* being offered, the final of which represents the maximum quantity of the *offer*.
- 1.3.7 One ramping rate applicable for all classes of *operating reserve* being offered.

- 1.3.8 Is this a standing *offer*? Yes/No. If Yes, Date To: \_\_\_\_\_ For which day(s) of the week? \_\_\_\_\_

## 1.4 Operating Reserve Offers from Exports

- 1.4.1 In order for a *boundary entity resource* to provide *operating reserve* from an export, its *registered market participant* shall submit an *offer* that includes, at a minimum, the information specified in this section 1.4.
- 1.4.2 Unique *boundary entity* identifier (interconnection and *boundary entity resource*).
- 1.4.3 *Registered market participant*.
- 1.4.4 *Dispatch day* and *dispatch hour(s)* for which *offer* applies.
- 1.4.5 *Operating reserve* class.
- 1.4.6 Two to five *price-quantity pairs* for each *dispatch hour* for each class of *operating reserve* being offered, the final of which represents the maximum quantity of the *offer*.
- 1.4.7 Is this a standing *offer* – Yes/No. If Yes, Date To: \_\_\_\_\_ For which day(s) of the week? \_\_\_\_\_
- 1.4.8 Sink *control area* (determined by selecting appropriate *boundary entity resource*).
- 1.4.9 e-Tag identification.
- 1.4.10 Notwithstanding MR Ch.7 s.3.3, e-Tags shall be submitted within the times outlined in the *IESO* interchange tagging procedures and in accordance with the following:
- 1.4.10.1 all *resources* shall be designated as firm for the Ontario flowgates and the Ontario portion of the *intertie* flowgates; and
  - 1.4.10.2 each *registered market participant* shall submit its e-Tag to the *IESO* through the electronic information system sanctioned by the relevant *standards authority* or, when not available, by such alternative means as may be specified by the *IESO* consistent with the policies of the relevant *standards authority*.

# Appendix 7.4 – Transmission Information Required for Scheduling and Dispatching

## 1.1 Transmission Information Required for Scheduling and Dispatching

- 1.1.1 Full *connection-related reliability information* and *transmission system* data is required to be provided and updated to the *IESO* in accordance with MR Ch.7 s.2.2.5 and MR Ch.4 App.4.16.
- 1.1.2 Advance *outage* information is required to be provided to the *IESO* in terms of MR Ch.5.
- 1.1.3 The following information is required to be advised to the *IESO* for scheduling and *dispatch* purposes:
  - 1.1.3.1 any change to the maximum thermal rating of any transmission branch as advised by the *IESO* to be included in the *DAM calculation engine, pre-dispatch calculation engine* and *real-time calculation engine*; and
  - 1.1.3.2 any change to the proposed *outage* plan as advised to and approved by the *IESO*.



**Note: The existing Appendix 7.5- The Market Clearing and Pricing Process has been deleted in its entirety and replaced with the new Appendix 7.5- The Day-Ahead Market Calculation Process**

## **Appendix 7.5 – The Day-Ahead Market Calculation Engine Process**

### **1.1 Purpose**

- 1.1.1 This appendix describes the process used by the *day-ahead market calculation engine* to determine commitments, schedules and prices for the *day-ahead market*.

## **2 Day-Ahead Market Calculation Engine**

### **2.1 Passes of the Day-Ahead Market Calculation Engine**

- 2.1.1 The *day-ahead market calculation engine* shall execute three passes to produce day-ahead schedules, commitments and *locational marginal prices*.
  - 2.1.1.1 Pass 1, the Market Commitment and Market Power Mitigation Pass in accordance with section 7;
  - 2.1.1.2 Pass 2, the Reliability Scheduling and Commitment Pass in accordance with section 17; and
  - 2.1.1.3 Pass 3, the DAM Scheduling and Pricing Pass, in accordance with section 19.

## **3 Information Used by the Day-Ahead Market Calculation Engine**

- 3.1.1 The *day-ahead market calculation engine* shall use the information in section 3A.1 of Chapter 7.

## 4 Sets, Indices and Parameters Used in the Day-Ahead Market Calculation Engine

### 4.1 Fundamental Sets and Indices

- 4.1.1  $A$  designates the set of all *intertie zones*;
- 4.1.2  $B$  designates the set of buses identifying all *dispatchable* and *non-dispatchable resources* within Ontario;
- 4.1.3  $B^{PRL} \subseteq B$  designates the set of buses identifying *price responsive loads*;
- 4.1.4  $B^{DL} \subseteq B$  designates the set of buses identifying *dispatchable loads*;
- 4.1.5  $B^{HDR} \subseteq B$  designates the set of buses identifying *hourly demand response resources*;
- 4.1.6  $B^{NDG} \subseteq B$  designates the set of buses identifying *non-dispatchable generation resources*;
- 4.1.7  $B^{DG} \subseteq B$  designates the set of buses identifying *dispatchable generation resources*;
- 4.1.8  $B^{NQS} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable non-quick start resources*;
- 4.1.9  $B^{PSU} \subseteq B^{NQS}$  designates the subset of buses identifying *pseudo-units*;
- 4.1.10  $B^{VG} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable variable generation resources*;
- 4.1.11  $B^{ELR} \subseteq B^{DG}$  designates the subset of buses identifying *energy limited resources*;
- 4.1.12  $B^{HE} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable hydroelectric generation resources*;
- 4.1.13  $B_s^{HE} \subseteq B^{HE}$  designates the subset of buses identifying *dispatchable hydroelectric generation resources* in set  $s \in SHE$ ;
- 4.1.14  $\wp(B^{HE})$  designates the set of all subsets of the set  $B^{HE}$ ;

- 4.1.15  $B_{up}^{HE} \subseteq \mathcal{B}(B^{HE})$  designates the set of buses identifying all upstream *dispatchable* hydroelectric *generation resources* with a registered *forebay* that are linked via *time lag* and *MWh ratio dispatch data* with downstream *dispatchable* hydroelectric *generation resources* with a registered *forebay*;
- 4.1.16  $B_{dn}^{HE} \subseteq \mathcal{B}(B^{HE})$  designates the set of buses identifying all downstream *dispatchable* hydroelectric *generation resources* with a registered *forebay* that are linked via *time lag* and *MWh ratio dispatch data* with upstream *dispatchable* hydroelectric *generation resources* with a registered *forebay*;
- 4.1.17  $B_r^{REG} \subseteq B$  designates the set of internal buses in *operating reserve* region  $r \in ORREG$ ;
- 4.1.18  $B_p^{ST} \subseteq B^{PSU}$  designates the subset of buses identifying *pseudo-units* with a share of steam turbine *resource*  $p \in PST$ ;
- 4.1.19  $B^{NO10DF} \subseteq B^{PSU}$  designates the subset of buses identifying *pseudo-units* that cannot provide *ten-minute operating reserve* from the duct firing region;
- 4.1.20  $C$  designates the set of contingencies that shall be considered in the *security* assessment function;
- 4.1.21  $D$  designates the set of buses outside Ontario, corresponding to imports and exports at *intertie zones*;
- 4.1.22  $D^{GMPRef} \subseteq D$  designates the set of *global market power reference* *intertie zones*, and *boundary entity resources* for those *interties*;
- 4.1.23  $D_r^{REG} \subseteq D$  designates the set of *intertie zone* buses identifying *boundary entity resources* in *operating reserve* region  $r \in ORREG$ ;
- 4.1.24  $DX \subseteq D$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids*;
- 4.1.25  $DI \subseteq D$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers*;
- 4.1.26  $D_a \subseteq D$  designates the set of all buses identifying *boundary entity resources* in *intertie zone*  $a \in A$ ;
- 4.1.27  $DX_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids* in *intertie zone*  $a \in A$ ;

- 4.1.28  $DI_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers* in *intertie zone*  $a \in A$ ;
- 4.1.29  $DX_h^{EM} \subseteq DX$  designates the *intertie zone* buses corresponding to *emergency energy* export transactions for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.30  $DX_h^{INP} \subseteq DX$  designates the *intertie zone* buses corresponding to inadvertent *energy* payback export transactions for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.31  $DI_h^{EM} \subseteq DI$  designates the *intertie zone* buses corresponding to *emergency energy* import transactions for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.32  $DI_h^{EMNS} \subseteq DI_h^{EM}$  designates the *intertie zone* buses corresponding to *emergency energy* import transactions that do not support *emergency energy* export transactions in hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.33  $DI_h^{INP} \subseteq DI$  designates the *intertie zone* buses corresponding to inadvertent *energy* payback import transactions for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.34  $F$  designates the set of *facilities* and groups of *facilities* for which transmission constraints may be identified;
- 4.1.35  $F_h \subseteq F$  designates the set of *facilities* whose pre-contingency limit was violated in hour  $h$  as determined by a preceding *security* assessment function iteration;
- 4.1.36  $F_{h,c} \subseteq F$  designates the set of *facilities* whose post-contingency limit for contingency  $c$  is violated in hour  $h$  as determined by a preceding *security* assessment function iteration;
- 4.1.37  $J_{h,b}^E$  designates the set of *bid* laminations for *energy* at  $b \in B \cup DX \cup VB$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.38  $J_{h,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.39  $J_{h,b}^{10S}$  designates the set of *reference level value* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.40  $J_{h,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B \cup DX$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.41  $J_{h,b}^{10N}$  designates the set of *reference level value* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;

- 4.1.42  $J_{h,b}^{30R}$  designates the set of *offer* laminations for *thirty-minute operating reserve* at bus  $b \in B \cup DX$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.43  $J_{h,b}'^{30R}$  designates the set of *reference level value* laminations for *thirty-minute operating reserve* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.44  $K_{h,b}^E$  designates the set of *offer* laminations for *energy* at bus  $b \in B \cup DI \cup VO$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.45  $K_{h,b}^E$  designates the set of *reference level value* laminations for *energy* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.46  $K_{h,b}^{DF} \subseteq K_{h,b}^E$  designates the set of *offer* laminations for *energy* corresponding to the duct firing region of a *pseudo-unit* at bus  $b \in B^{PSU}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.47  $K_{h,b}^{DR} \subseteq K_{h,b}^E$  designates the set of *offer* laminations for *energy* corresponding to the *dispatchable* region of a *pseudo-unit* at bus  $b \in B^{PSU}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.48  $K_{h,b}^{LTMLP}$  designates the set of *offer* laminations for *energy* quantities up to the *minimum loading point* for a *non-quick start resource* at bus  $b \in B^{NQS}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.49  $K_{h,b}'^{LTMLP}$  designates the set of *reference level value* laminations for *energy* quantities up to the *minimum loading point reference level* for a *non-quick start resource* at bus  $b \in B^{NQS}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.50  $K_{h,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.51  $K_{h,b}^{10S}$  designates the set of *reference level value* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.52  $K_{h,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B \cup DI$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.53  $K_{h,b}^{10N}$  designates the set of *reference level value* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.54  $K_{h,b}^{30R}$  designates the set of *offer* laminations for *thirty-minute operating reserve* at bus  $b \in B \cup DI$  for hour  $h \in \{1, \dots, 24\}$ ;

- 4.1.55  $K_{h,b}^{20R}$  designates the set of *reference level value* laminations for *thirty-minute operating reserve* at bus  $b \in B$  for hour  $h \in \{1, \dots, 24\}$ ;
- 4.1.56  $L$  designates the set of buses where the *locational marginal prices* represent prices for *delivery points* associated with *non-dispatchable generation resources* and *dispatchable generation resources, dispatchable loads, hourly demand response resources, price responsive loads* and *non-dispatchable loads*;
- 4.1.57  $L_y^{NDL} \subseteq L$  designates the buses contributing to the zonal price for *non-dispatchable load zone*  $y \in Y$ ;
- 4.1.58  $L_m^{VIRT} \subseteq L$  designates the buses contributing to the *virtual zonal price* for *virtual transaction zone*  $m \in M$ ;
- 4.1.59  $M$  designates the set of *virtual transaction zones*;
- 4.1.60  $NCA$  designates the set of *narrow constrained areas*;
- 4.1.61  $DCA$  designates the set of *dynamic constrained areas*;
- 4.1.62  $BCA$  designates the set of *broad constrained areas*;
- 4.1.63  $PST$  designates the set of steam turbine *resources offered* as part of a *pseudo-unit*;
- 4.1.64  $SHE$  designates the set indexing the sets of *dispatchable hydroelectric generation resources* with a *maximum daily energy limit* or a *minimum daily energy limit* or both for a registered *forebay*;
- 4.1.65  $V$  designates the set of *offers* and *bids* for *energy* corresponding to *virtual transactions*;
- 4.1.66  $VB \subseteq V$  designates the set of *bids* for *energy* corresponding to *virtual transactions*;
- 4.1.67  $VO \subseteq V$  designates the set of *offers* for *energy* corresponding to *virtual transactions*;
- 4.1.68  $V_m \subseteq V$  designates the set of *offers* and *bids* for *energy* corresponding to *virtual transactions* at *virtual transaction zone*  $m \in M$ ;
- 4.1.69  $VB_m \subseteq V_m$  designates the set of *bids* for *energy* corresponding to *virtual transactions* at *virtual transaction zone*  $m \in M$ ;

- 4.1.70  $VO_m \subseteq V_m$  designates the set of *offers* for *energy* corresponding to *virtual transactions* at *virtual transaction zone*  $m \in M$ ;
- 4.1.71  $Y$  designates the *non-dispatchable load* zones in Ontario; and
- 4.1.72  $Z_{Sch}$  designates the set of all *intertie* limit constraints.

## 4.2 Market Participant Data Parameters

- 4.2.1 With respect to a *non-dispatchable generation resource* identified by bus  $b \in B^{NDG}$ :
  - 4.2.1.1  $QNDG_{h,b,k}$  designates the maximum incremental quantity of *energy* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$ ; and
  - 4.2.1.2  $PNDG_{h,b,k}$  designates the price for the maximum incremental quantity of *energy* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$ .
- 4.2.2 With respect to a *dispatchable generation resource* identified by bus  $b \in B^{DG}$ :
  - 4.2.2.1  $MinQDG_b$  designates the *minimum loading point*;
  - 4.2.2.2  $QDG_{h,b,k}$  designates the maximum incremental quantity of *energy* above the *minimum loading point* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$ ;
  - 4.2.2.3  $PDG_{h,b,k}$  designates the price for the maximum incremental quantity of *energy* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$ ;
  - 4.2.2.4  $Q10SDG_{h,b,k}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10S}$ ;
  - 4.2.2.5  $P10SDG_{h,b,k}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10S}$ ;
  - 4.2.2.6  $Q10NDG_{h,b,k}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10N}$ ;

- 4.2.2.7  $P10NDG_{h,b,k}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,b}^{10N}$ ;
- 4.2.2.8  $Q30RDG_{h,b,k}$  designates the maximum incremental quantity of *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,b}^{30R}$ ;
- 4.2.2.9  $P30RDG_{h,b,k}$  designates the price of the maximum incremental quantity of *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,b}^{30R}$ ;
- 4.2.2.10  $ORRDG_b$  designates the maximum *operating reserve* ramp rate in MW per minute;
- 4.2.2.11  $NumRRDG_{h,b}$  designates the number of ramp rates provided in hour  $h \in \{1, \dots, 24\}$ ;
- 4.2.2.12  $RmpRngMaxDG_{h,b,w}$  for  $w \in \{1, \dots, NumRRDG_{h,b}\}$  designates the  $w^{th}$  ramp rate break point in hour  $h \in \{1, \dots, 24\}$ ;
- 4.2.2.13  $URRDG_{h,b,w}$  for  $w \in \{1, \dots, NumRRDG_{h,b}\}$  designates the ramp rate in MW per minute at which the *resource* can increase the amount of *energy* it supplies in hour  $h \in \{1, \dots, 24\}$  while operating in the range between  $RmpRngMaxDG_{h,b,w-1}$  and  $RmpRngMaxDG_{h,b,w}$  where  $RmpRngMaxDG_{h,b,0}$  shall be equal to zero;
- 4.2.2.14  $DRRDG_{h,b,w}$  for  $w \in \{1, \dots, NumRRDG_{h,b}\}$  designates the ramp rate in MW per minute at which the *resource* can decrease the amount of *energy* it supplies in hour  $h \in \{1, \dots, 24\}$  while operating in the range between  $RmpRngMaxDG_{h,b,w-1}$  and  $RmpRngMaxDG_{h,b,w}$  where  $RmpRngMaxDG_{h,b,0}$  shall be equal to zero;
- 4.2.2.15  $RLP30R_{h,b}$  designates the *reserve loading point* for *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ ; and
- 4.2.2.16  $RLP10S_{h,b}$  designates the *reserve loading point* for synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ .
- 4.2.3 With respect to a *dispatchable non-quick start resource* identified by bus  $b \in B^{NQS}$ :
- 4.2.3.1  $SUDG_{h,b}$  designates the *start-up offer* in hour  $h \in \{1, \dots, 24\}$ ;



- 4.2.3.2  $SNL_{h,b}$  designates the *speed no-load offer* in hour  $h \in \{1, \dots, 24\}$ ;
- 4.2.3.3  $MGBRTDG_b$  designates the *minimum generation block run-time*;
- 4.2.3.4  $MGBDTDG_b$  designates the *minimum generation block down-time*;
- 4.2.3.5  $MaxStartsDG_b$  designates the *maximum number of starts per day*;
- 4.2.3.6  $RampHrs_b$  designates the *ramp hours to minimum loading point*;
- 4.2.3.7  $RampE_{b,w}$  designates the *ramp up energy to minimum loading point* for  $w \in \{1, \dots, RampHrs_b\}$ ;
- 4.2.3.8  $QLTMLP_{h,b,k}$  designates the maximum incremental quantity of *energy* up to the *minimum loading point* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,b}^{LTMLP}$ ;
- 4.2.3.9  $PLTMLP_{h,b,k}$  designates the price for the maximum incremental quantity of *energy* up to the *minimum loading point* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,b}^{LTMLP}$ ; and
- 4.2.3.10  $MGODG_{h,b}$  designates the minimum generation cost to operate at *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ . This parameter is calculated as follows:

$$MGODG_{h,b} = SNL_{h,b} + \sum_{k \in K_{h,b}^{LTMLP}} PLTMLP_{h,b,k} \cdot QLTMLP_{h,b,k}$$

- 4.2.4 With respect to an *energy limited resource* identified by bus  $b \in B^{ELR}$ :
  - 4.2.4.1  $MaxDEL_b$  designates the *maximum daily energy limit* for a single *resource* with or without out a registered *forebay*.
- 4.2.5 With respect to a *dispatchable hydroelectric generation resource* identified by bus  $b \in B^{HE}$ :
  - 4.2.5.1  $MinHMR_{h,b}$  designates the *hourly must-run* value for the *resource* in hour  $h \in \{1, \dots, 24\}$ ;
  - 4.2.5.2  $MinHO_{h,b}$  designates the *minimum hourly output* for the *resource* in hour  $h \in \{1, \dots, 24\}$ ;
  - 4.2.5.3  $MinDEL_b$  designates the *minimum daily energy limit* for a single *resource* with or without a registered *forebay*;

- 4.2.5.4  $MaxStartsHE_b$  designates the *maximum number of starts per day* for the *resource*;
- 4.2.5.5  $StartMW_{b,i}$  for  $i \in \{1, \dots, NStartMW_b\}$  designates the *start indication value* for measuring *maximum number of starts per day*; a start is counted between hours  $h$  and  $(h + 1)$  if the schedule increases from below  $StartMW_{b,i}$  to at or above  $StartMW_{b,i}$ ; and
- 4.2.5.6  $(ForL_{b,i}, ForU_{b,i})$  for  $i \in \{1, \dots, NFor_b\}$  designate the lower and upper limits of the *forbidden regions* and indicate that the *resource* cannot be scheduled between  $ForL_{b,i}$  and  $ForU_{b,i}$  for all  $i \in \{1, \dots, NFor_b\}$ .
- 4.2.6 With respect to multiple *dispatchable* hydroelectric *generation resources* with a registered *forebay*:
- 4.2.6.1  $MaxSDEL_s$  designates the *maximum daily energy limit* shared by all *dispatchable* hydroelectric *generation resources* in set  $s \in SHE$ ; and
- 4.2.6.2  $MinSDEL_s$  designates the *minimum daily energy limit* shared by all *dispatchable* hydroelectric *generation resources* in set  $s \in SHE$ .
- 4.2.7 With respect to a *dispatchable* hydroelectric *generation resource* for which a MWh ratio was respected
- 4.2.7.1  $LNK \subseteq B_{up}^{HE} \times B_{dn}^{HE}$  designates the set of linked *dispatchable* hydroelectric *generation resources*, where  $LNK$  is a set with elements of the form  $(b_1, b_2)$  and  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ ;
- 4.2.7.2  $Lag_{b_1, b_2} \in \{0, \dots, 23\}$  designates the *time lag* in hours between upstream *dispatchable* hydroelectric *generation resources*  $b_1 \in B_{up}^{HE}$  and downstream *dispatchable* hydroelectric *generation resources*  $b_2 \in B_{dn}^{HE}$  for  $(b_1, b_2) \in LNK$ ; and
- 4.2.7.3  $MWhRatio_{b_1, b_2}$  designates the *MWh ratio* between upstream *dispatchable* hydroelectric *generation resources*  $b_1 \in B_{up}^{HE}$  and downstream *dispatchable* hydroelectric *generation resources*  $b_2 \in B_{dn}^{HE}$  for  $(b_1, b_2) \in LNK$ .
- 4.2.8 With respect to a *pseudo-unit* identified by bus  $b \in B^{PSU}$ :
- 4.2.8.1  $STShareMLP_b$  designates the steam turbine *resource's* share of the *minimum loading point* region;

- 4.2.8.2  $STShareDR_b$  designates the steam turbine *resource's* share of the *dispatchable* region;
- 4.2.8.3  $RampCT_{b,w}$  designates the quantity of *energy* injected  $w$  hours before the *pseudo-unit* reaches its *minimum loading point* that is attributed to the combustion turbine *resource* for  $w \in \{1, \dots, RampHrs_b\}$ ; and
- 4.2.8.4  $RampST_{b,w}$  designates the quantity of *energy* injected  $w$  hours before the *pseudo-unit* reaches its *minimum loading point* that is attributed to the steam turbine *resource* for  $w \in \{1, \dots, RampHrs_b\}$ .
- 4.2.9 With respect to a *dispatchable load* identified by bus  $b \in B^{DL}$ :
- 4.2.9.1  $QDL_{h,b,j}$  designates the maximum incremental quantity of *energy* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,b}^E$ ;
- 4.2.9.2  $PDL_{h,b,j}$  designates the price for the maximum incremental quantity of *energy* in hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,b}^E$ ;
- 4.2.9.3  $Q10SDL_{h,b,j}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{10S}$ ;
- 4.2.9.4  $P10SDL_{h,b,j}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{10S}$ ;
- 4.2.9.5  $Q10NDL_{h,b,j}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{10N}$ ;
- 4.2.9.6  $P10NDL_{h,b,j}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{10N}$ ;
- 4.2.9.7  $Q30RDL_{h,b,j}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{30R}$ ;
- 4.2.9.8  $P30RDL_{h,b,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{30R}$ ;

- 4.2.9.9  $ORRD L_b$  designates the *operating reserve* ramp rate in MW per minute for reductions in load consumption;
- 4.2.9.10  $NumRRDL_{h,b}$  designates the number of ramp rates provided in hour  $h \in \{1, \dots, 24\}$ ;
- 4.2.9.11  $RmpRngMaxDL_{h,b,w}$  for  $w \in \{1, \dots, NumRRDL_{h,b}\}$  designates the  $w^{th}$  ramp rate break point in hour  $h \in \{1, \dots, 24\}$ ;
- 4.2.9.12  $URRDL_{h,b,w}$  for  $w \in \{1, \dots, NumRRDL_{h,b}\}$  designates the ramp rate in MW per minute at which the *dispatchable load* can increase its amount of *energy* consumption in hour  $h \in \{1, \dots, 24\}$  while operating in the range between  $RmpRngMaxDL_{h,b,w-1}$  and  $RmpRngMaxDL_{h,b,w}$  where  $RmpRngMaxDL_{h,b,0}$  shall be equal to zero;
- 4.2.9.13  $DRRDL_{h,b,w}$  for  $w \in \{1, \dots, NumRRDL_{h,b}\}$  designates the ramp rate in MW per minute at which the *dispatchable load* can decrease its amount of *energy* consumption in hour  $h \in \{1, \dots, 24\}$  while operating in the range between  $RmpRngMaxDL_{h,b,w-1}$  and  $RmpRngMaxDL_{h,b,w}$ , where  $RmpRngMaxDL_{h,b,0}$  shall be equal to zero; and
- 4.2.9.14  $QDLFIRM_{h,b}$  designates the quantity of *energy* that is *bid* at the *maximum market clearing price* in hour  $h \in \{1, \dots, 24\}$ .
- 4.2.10 With respect to an *hourly demand response resource* identified by bus  $b \in B^{HDR}$ :
- 4.2.10.1  $QHDR_{h,b,j}$  designates the maximum incremental quantity of reduction in *energy* consumption that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,b}^E$ ;
- 4.2.10.2  $PHDR_{h,b,j}$  designates the price for the maximum incremental quantity of reduction in *energy* consumption for hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,b}^E$ ;
- 4.2.10.3  $URRHDR_b$  designates the maximum rate in MW per minute at which the *hourly demand response resource* can decrease its amount of *energy* consumption; and
- 4.2.10.4  $DRRHDR_b$  designates the maximum rate in MW per minute at which the *hourly demand response resource* can increase its amount of *energy* consumption.
- 4.2.11 With respect to a *price responsive load* identified by bus  $b \in B^{PRL}$ :

- 4.2.11.1  $QPRL_{h,b,j}$  designates the maximum incremental quantity of *energy* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,b}^E$ ;
- 4.2.11.2  $PPRL_{h,b,j}$  designates the price for the maximum incremental quantity of *energy* in hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,b}^E$ ; and
- 4.2.11.3  $QPRLFIRM_{h,b}$  designates the quantity of *energy* that is *bid* at *MMCP* in hour  $h \in \{1, \dots, 24\}$ .
- 4.2.12 With respect to a *virtual transaction*:
- 4.2.12.1  $QVB_{h,v,j}$  designates the maximum incremental quantity of *energy* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  from a *virtual zonal resource*  $v \in VB$  in association with *bid* lamination  $j \in J_{h,v}^E$ ;
- 4.2.12.2  $PVB_{h,v,j}$  designates the price for the maximum incremental quantity of *energy* in hour  $h \in \{1, \dots, 24\}$  from a *virtual zonal resource*  $v \in VB$  in association with *bid* lamination  $j \in J_{h,v}^E$ ;
- 4.2.12.3  $QVO_{h,v,k}$  designates the maximum incremental quantity of *energy* that may be scheduled in hour  $h \in \{1, \dots, 24\}$  from a *virtual zonal resource*  $v \in VO$  in association with *offer* lamination  $k \in K_{h,v}^E$ ; and
- 4.2.12.4  $PVO_{h,v,k}$  designates the price for the maximum incremental quantity of *energy* in hour  $h \in \{1, \dots, 24\}$  from a *virtual zonal resource*  $v \in VO$  in association with *offer* lamination  $k \in K_{h,v}^E$ .
- 4.2.13 With respect to a *boundary entity resource* import from *intertie zone* bus  $d \in DI$ , where the *locational marginal price* represents the price for the *intertie metering point*:
- 4.2.13.1  $QIG_{h,d,k}$  designates the maximum incremental quantity of *energy* that may be scheduled to import in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^E$ ;
- 4.2.13.2  $PIG_{h,d,k}$  designates the price for the maximum incremental quantity of *energy* that may be scheduled to import in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^E$ ;
- 4.2.13.3  $Q10NIG_{h,d,k}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled to

provide in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^{10N}$ ;

4.2.13.4  $P10NIG_{h,d,k}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^{10N}$ ;

4.2.13.5  $Q30RIG_{h,d,k}$  designates the the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled to provide in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^{30R}$ ; and

4.2.13.6  $P30RIG_{h,d,k}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^{30R}$ .

4.2.14 With respect to a *boundary entity resource* export to *intertie zone* bus  $d \in DX$ , where the *locational marginal price* represents the price for the *intertie metering point*:

4.2.14.1  $QXL_{h,d,j}$  designates the maximum incremental quantity of *energy* that may be scheduled to export in hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,d}^E$ ;

4.2.14.2  $PXL_{h,d,j}$  designates the price for the maximum incremental quantity of *energy* that may be scheduled to export in hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,d}^E$ ;

4.2.14.3  $Q10NXL_{h,d,j}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled to provide in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,d}^{10N}$ ;

4.2.14.4  $P10NXL_{h,d,j}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,d}^{10N}$ ;

4.2.14.5  $Q30RXL_{h,d,j}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled to provide in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,d}^{30R}$ ; and

4.2.14.6  $P30RXL_{h,d,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,d}^{30R}$ .

4.2.15 With respect to a *linked wheeling through transaction*:

4.2.15.1  $L_h \subseteq DX \times DI$  designates the set of linked *boundary entity resource* import and export buses corresponding to *linked wheeling through transactions*, where  $L_h$  is a set with elements of the form  $(dx, di)$  and  $dx \in DX$  and  $di \in DI$ .

## 4.3 IESO Data Parameters

4.3.1 Variable Generation Forecast

4.3.1.1  $FG_{h,b}$  designates the *IESO's* centralized *variable generation* forecast for a *variable generation resource* identified by bus  $b \in B^{VG}$  in hour  $h \in \{1, \dots, 24\}$ .

4.3.2 Variable Generation Tie-Breaking

4.3.2.1  $NumVG$  designates the number of *variable generation resources* in the daily *dispatch* order; and

4.3.2.2  $TBM_b \in \{1, \dots, NumVG\}$  designates the tie-breaking modifier for the *variable generation resource* at bus  $b \in B^{VG}$ .

4.3.3 Operating Reserve Requirements

4.3.3.1  $TOT10S_h$  designates the synchronized *ten-minute operating reserve* requirement;

4.3.3.2  $TOT10R_h$  designates the total *ten-minute operating reserve* requirement;

4.3.3.3  $TOT30R_h$  designates the *thirty-minute operating reserve* requirement;

4.3.3.4  $ORREG$  designates the set of regions for which regional *operating reserve* limits have been defined;

4.3.3.5  $REGMin10R_{h,r}$  designates the minimum requirement for total *ten-minute operating reserve* in region  $r \in ORREG$  in hour  $h \in \{1, \dots, 24\}$ ;

4.3.3.6  $REGMin30R_{h,r}$  designates the minimum requirement for *thirty-minute operating reserve* in region  $r \in ORREG$  in hour  $h \in \{1, \dots, 24\}$ ;

4.3.3.7  $REGMax10R_{h,r}$  designates the maximum amount of total *ten-minute operating reserve* that may be scheduled in region  $r \in ORREG$  in hour  $h \in \{1, \dots, 24\}$ ; and

- 4.3.3.8  $REGMax30R_{h,r}$  designates the maximum amount of *thirty-minute operating reserve* that may be scheduled in region  $r \in ORREG$  in hour  $h \in \{1, \dots, 24\}$ .

#### 4.3.4 Intertie Limits

- 4.3.4.1  $EnCoeff_{a,z}$  designates the coefficient for calculating the contribution of scheduled *energy* flows and *operating reserve* inflows for *intertie zone*  $a \in A$ , which is part of *intertie* limit constraint  $z \in Z_{Sch}$ . A coefficient of +1 shall describe flows into Ontario while a coefficient of -1 shall describe flows out of Ontario;
- 4.3.4.2  $MaxExtSch_{h,z}$  designates the maximum flow limit for *intertie* flow constraint  $z \in Z_{Sch}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 4.3.4.3  $ExtDSC_h$  designates the net interchange scheduling limit for when the net flows over all *interties* from hour  $(h - 1)$  to hour  $h$  decrease; and
- 4.3.4.4  $ExtUSC_h$  designates the net interchange scheduling limit for when the net flows over all *interties* from hour  $(h - 1)$  to hour  $h$  increase.

#### 4.3.5 Resource Minimum and Maximum Constraints

- 4.3.5.1 Where applicable the minimum or maximum output of a *dispatchable generation resource* or a *non-dispatchable generation resource* and minimum or maximum consumption of a *dispatchable load* may be limited due to *reliability* constraints, applicable *contracted ancillary services*, *outages*, *derates*, and other constraints, such that:
- 4.3.5.1.1  $MinDL_{h,b}$  designates the most restrictive minimum consumption limit for the *dispatchable load* in hour  $h$  at bus  $b \in B^{DL}$ ;
- 4.3.5.1.2  $MaxDL_{h,b}$  designates the most restrictive maximum consumption limit for the *dispatchable load* in hour  $h$  at bus  $b \in B^{DL}$ ;
- 4.3.5.1.3  $MinNDG_{h,b}$  designates the most restrictive minimum output limit for the *non-dispatchable generation resource* in hour  $h$  at bus  $b \in B^{NDG}$ ;
- 4.3.5.1.4  $MaxNDG_{h,b}$  designates the most restrictive maximum output limit for the *non-dispatchable generation resource* in hour  $h$  at bus  $b \in B^{NDG}$ ;



- 4.3.5.1.5  $MinDG_{h,b}$  designates the most restrictive minimum output limit for the *dispatchable generation resource* in hour  $h$  at bus  $b \in B^{DG}$ ;
- 4.3.5.1.6  $MaxDG_{h,b}$  designates the most restrictive maximum output limit for the *dispatchable generation resource* in hour  $h$  at bus  $b \in B^{DG}$ ;
- 4.3.5.1.7  $MaxMLP_{h,b}$  designates the maximum output limit in hour  $h$  for the *minimum loading point* region of a *pseudo-unit* at bus  $b \in B^{PSU}$ ;
- 4.3.5.1.8  $MaxDR_{h,b}$  designates the maximum output limit in hour  $h$  for the *dispatchable* region of a *pseudo-unit* at bus  $b \in B^{PSU}$ ; and
- 4.3.5.1.9  $MaxDF_{h,b}$  designates the maximum output limit in hour  $h$  for the duct firing region of a *pseudo-unit* at bus  $b \in B^{PSU}$ .

#### 4.3.6 Constraint Violation Penalties

- 4.3.6.1  $(PLdViolSch_{h,i}, QLdViolSch_{h,i})$  for  $i \in \{1, \dots, N_{LdViol_h}\}$  designate the price-quantity segments of the penalty curve for under generation used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.2  $(PLdViolPrc_{h,i}, QLdViolPrc_{h,i})$  for  $i \in \{1, \dots, N_{LdViol_h}\}$  designate the price-quantity segments of the penalty curve for under generation used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.3  $(PGenViolSch_{h,i}, QGenViolSch_{h,i})$  for  $i \in \{1, \dots, N_{GenViol_h}\}$  designate the price-quantity segments of the penalty curve for over generation used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.4  $(PGenViolPrc_{h,i}, QGenViolPrc_{h,i})$  for  $i \in \{1, \dots, N_{GenViol_h}\}$  designate the price-quantity segments of the penalty curve for over generation used by the As-Offered Pricing algorithm in section 9, Reference Level

Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;

- 4.3.6.5  $(P10SViolSch_{h,i}, Q10SViolSch_{h,i})$  for  $i \in \{1, \dots, N_{10SViol_h}\}$  designate the price-quantity segments of the penalty curve for the synchronized *ten-minute operating reserve* requirement used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.6  $(P10SViolPrc_{h,i}, Q10SViolPrc_{h,i})$  for  $i \in \{1, \dots, N_{10SViol_h}\}$  designate the price-quantity segments of the penalty curve for the synchronized *ten-minute operating reserve* requirement used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.7  $(P10RViolSch_{h,i}, Q10RViolSch_{h,i})$  for  $i \in \{1, \dots, N_{10RViol_h}\}$  designate the price-quantity segments of the penalty curve for the total *ten-minute operating reserve* requirement used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.8  $(P10RViolPrc_{h,i}, Q10RViolPrc_{h,i})$  for  $i \in \{1, \dots, N_{10RViol_h}\}$  designate the price-quantity segments of the penalty curve for the total *ten-minute operating reserve* requirement used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.9  $(P30RViolSch_{h,i}, Q30RViolSch_{h,i})$  for  $i \in \{1, \dots, N_{30RViol_h}\}$  designate the price-quantity segments of the penalty curve for the total *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.10  $(P30RViolPrc_{h,i}, Q30RViolPrc_{h,i})$  for  $i \in \{1, \dots, N_{30RViol_h}\}$  designate the price-quantity segments of the penalty curve for the total *thirty-*

*minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;

- 4.3.6.11 ( $PREG10RViolSch_{h,i}, QREG10RViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{REG10RViol_h}\}$  designate the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* minimum requirements used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.12 ( $PREG10RViolPrc_{h,i}, QREG10RViolPrc_{h,i}$ ) for  $i \in \{1, \dots, N_{REG10RViol_h}\}$  designate the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* minimum requirements used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.13 ( $PREG30RViolSch_{h,i}, QREG30RViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{REG30RViol_h}\}$  designate the price-quantity segments of the penalty curve for area *thirty-minute operating reserve* minimum requirements used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.14 ( $PREG30RViolPrc_{h,i}, QREG30RViolPrc_{h,i}$ ) for  $i \in \{1, \dots, N_{REG30RViol_h}\}$  designate the price-quantity segments of the penalty curve for area *thirty-minute operating reserve* minimum requirements used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.15 ( $PXREG10RViolSch_{h,i}, QXREG10RViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{XREG10RViol_h}\}$  designate the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* maximum restrictions used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;

- 4.3.6.16 ( $PXREG10RViolPrC_{h,i}, QXREG10RViolPrC_{h,i}$ ) for  $i \in \{1, \dots, N_{XREG10RViol_h}\}$  designate the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* maximum restrictions used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.17 ( $PXREG30RViolSch_{h,i}, QXREG30RViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{XREG30RViol_h}\}$  designate the price-quantity segments of the penalty curve for area total *thirty-minute operating reserve* maximum restrictions used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.18 ( $PXREG30RViolPrC_{h,i}, QXREG30RViolPrC_{h,i}$ ) for  $i \in \{1, \dots, N_{XREG30RViol_h}\}$  designate the price-quantity segments of the penalty curve for area total *thirty-minute operating reserve* maximum restrictions used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.19 ( $PPreITLViolSch_{f,h,i}, QPreITLViolSch_{f,h,i}$ ) for  $i \in \{1, \dots, N_{PreITLViol_{f,h}}\}$  designate the price-quantity segments of the penalty curve for exceeding the pre-contingency limit of the transmission constraint for *facility*  $f \in F$  used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.20 ( $PPreITLViolPrC_{f,h,i}, QPreITLViolPrC_{f,h,i}$ ) for  $i \in \{1, \dots, N_{PreITLViol_{f,h}}\}$  designate the price-quantity segments of the penalty curve for exceeding the pre-contingency limit of the transmission constraint for *facility*  $f \in F$  used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.21 ( $PITLViolSch_{c,f,h,i}, QITLViolSch_{c,f,h,i}$ ) for  $i \in \{1, \dots, N_{ITLViol_{c,f,h}}\}$  designate the price-quantity segments of the penalty curve for exceeding the contingency  $c \in C$  post-contingency limit of the transmission constraint for *facility*  $f \in F$  used by As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;

- 4.3.6.22 ( $PITLViolPrc_{c,f,h,i}$   $QITLViolPrc_{c,f,h,i}$ ) for  $i \in \{1, \dots, N_{ITLViol_{c,f,h}}\}$  designate the price-quantity segments of the penalty curve for exceeding the contingency  $c \in C$  post-contingency limit of the transmission constraint for facility  $f \in F$  used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.23 ( $PPreXTLViolSch_{z,h,i}$   $QPreXTLViolSch_{z,h,i}$ ) for  $i \in \{1, \dots, N_{PreXTLViol_{z,h}}\}$  designate the price-quantity segments of the penalty curve for exceeding the flow limit specified by  $z \in Z_{Sch}$  used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.24 ( $PPreXTLViolPrc_{z,h,i}$   $QPreXTLViolPrc_{z,h,i}$ ) for  $i \in \{1, \dots, N_{PreXTLViol_{z,h}}\}$  designate the price-quantity segments of the penalty curve for exceeding the flow limit specified by  $z \in Z_{Sch}$  used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.25 ( $PNIUViolSch_{h,i}$   $QNIUViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{NIUViol_h}\}$  designate the price-quantity segments of the penalty curve for exceeding the hour  $h$  net interchange increase constraint between hours  $(h - 1)$  and  $h$  used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.26 ( $PNIUViolPrc_{h,i}$   $QNIUViolPrc_{h,i}$ ) for  $i \in \{1, \dots, N_{NIUViol_h}\}$  designate the price-quantity segments of the penalty curve for exceeding the hour  $h$  net interchange increase constraint between hours  $(h - 1)$  and  $h$  used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.27 ( $PNIDViolSch_{h,i}$   $QPNIDViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{NIDViol_h}\}$  designate the price-quantity segments of the penalty curve for exceeding the hour  $h$  net interchange decrease constraint between hours  $(h - 1)$  and  $h$  used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;

- 4.3.6.28 ( $PNIDViolPrc_{h,i}, QNIDViolPrc_{h,i}$ ) for  $i \in \{1, \dots, N_{NIDViol_h}\}$  designate the price-quantity segments of the penalty curve for exceeding the hour  $h$  net interchange decrease constraint between hours  $(h - 1)$  and  $h$  used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.29 ( $PMaxDelViolSch_{h,i}, QMaxDelViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{MaxDelViol_h}\}$  designate the price-quantity segments of the penalty curve for exceeding a *resource's maximum daily energy limit* used by As- Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.30 ( $PMaxDelViolPrc_{h,i}, QMaxDelViolPrc_{h,i}$ ) for  $i \in \{1, \dots, N_{MaxDelViol_h}\}$  designate the price-quantity segments of the penalty curve for exceeding a *resource's maximum daily energy limit* used by the As- Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.31 ( $PMinDelViolSch_{h,i}, QMinDelViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{MinDelViol_h}\}$  designate the price-quantity segments of the penalty curve for under-scheduling a *resource's minimum daily energy limit* used by the As- Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.32 ( $PMinDelViolPrc_{h,i}, QMinDelViolPrc_{h,i}$ ) for  $i \in \{1, \dots, N_{MinDelViol_h}\}$  designate the price-quantity segments of the penalty curve for under-scheduling a *resource's minimum daily energy limit* used by the As- Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.33 ( $PSMaxDelViolSch_{h,i}, QSMaxDelViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{SMaxDelViol_h}\}$  designate the price-quantity segments of the penalty curve for exceeding a shared *maximum daily energy limit* used by the As- Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;

- 4.3.6.34 ( $PSMaxDelViolPrc_{h,i}, QSMMaxDelViolPrc_{h,i}$ ) for  $i \in \{1, \dots, N_{MaxDelViol_h}\}$  designate the price-quantity segments of the penalty curve for exceeding a shared *maximum daily energy limit* used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.35 ( $PSMinDelViolSch_{h,i}, QSMMinDelViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{SMinDelViol_h}\}$  designate the price-quantity segments of the penalty curve for under-scheduling a shared *minimum daily energy limit* used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.36 ( $PSMinDelViolPrc_{h,i}, QSMMinDelViolPrc_{h,i}$ ) for  $i \in \{1, \dots, N_{SMinDelViol_h}\}$  designate the price-quantity segments of the penalty curve for under-scheduling a shared *minimum daily energy limit* used by the As-Offered Pricing algorithm in section 9, Reference Level Pricing algorithm in section 13, Mitigated Pricing algorithm in section 16, and DAM Pricing algorithm in section 21;
- 4.3.6.37 ( $POGenLnkViolSch_{h,i}, QOGenLnkViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{OGenLnkViol_h}\}$  designate the price-quantity segments of the penalty curve for over generation on a downstream *resource* used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20;
- 4.3.6.38 ( $PUGenLnkViolSch_{h,i}, QUGenLnkViolSch_{h,i}$ ) for  $i \in \{1, \dots, N_{UGenLnkViol_h}\}$  designate the price-quantity segments of the penalty curve for under generation on a downstream *resource* used by the As-Offered Scheduling algorithm in section 8, Reference Level Scheduling algorithm in section 12, Mitigated Scheduling algorithm in section 15, Reliability Scheduling algorithm in section 18, and DAM Scheduling algorithm in section 20; and
- 4.3.6.39  $NISLPen$  designates the net interchange scheduling limit constraint violation penalty price for *locational marginal pricing*.

#### 4.3.7 Price Bounds

- 4.3.7.1  $EngyPrcCeil$  designates and is equal to the *maximum market clearing price* for *energy*;

- 4.3.7.2 *EngyPrcFlr* designates and is equal to the *settlement floor price*;
  - 4.3.7.3 *ORPrcCeil* designates and is equal to the *maximum operating reserve price* for all classes of *operating reserve*; and
  - 4.3.7.4 *ORPrcFlr* designates the minimum price for all classes of *operating reserve* and is equal to \$0.
- 4.3.8 Ex-ante Market Power Mitigation
- 4.3.8.1 *BCACondThresh* designates the threshold for the congestion component of a *resource's locational marginal price* for *energy* and is equal to \$25/MWh;
  - 4.3.8.2 *IBPThresh* designates the *intertie border price* threshold for *energy* and is equal to \$100/MWh;
  - 4.3.8.3 *ORGCondThresh* designates the global market power condition threshold for a *resource's locational marginal price* for *operating reserve* and is equal to \$15/MW;
  - 4.3.8.4  $PDGRef_{h,b,k'}$  designates the *reference level value* for *energy* lamination  $k' \in K_{h,b}^E$  for the *resource* at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 4.3.8.5  $P10SDGRef_{h,b,k'}$  designates the *reference level value* for synchronized *ten-minute operating reserve* lamination  $k' \in K_{h,b}^{10S}$  for the *resource* at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 4.3.8.6  $P10NDGRef_{h,b,k'}$  designates the *reference level value* for non-synchronized *ten-minute operating reserve* lamination  $k' \in K_{h,b}^{10N}$  for the *resource* at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 4.3.8.7  $P30RDGRef_{h,b,k'}$  designates the *reference level value* for *thirty-minute operating reserve* lamination  $k' \in K_{h,b}^{30R}$  for the *resource* at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 4.3.8.8  $P10SDLRef_{h,b,j'}$  designates the *reference level value* for synchronized *ten-minute operating reserve* lamination  $j' \in J_{h,b}^{10S}$  for the *resource* at bus  $b \in B^{DL}$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 4.3.8.9  $P10NDLRef_{h,b,j'}$  designates the *reference level value* for non-synchronized *ten-minute operating reserve* lamination  $j' \in J_{h,b}^{10N}$  for the *resource* at bus  $b \in B^{DL}$  in hour  $h \in \{1, \dots, 24\}$ ;



- 4.3.8.10  $P30RD\text{LRef}_{h,b,j'}$  designates the *reference level value* for *thirty-minute operating reserve* lamination  $j' \in J_{h,b}^{30R}$  for the *resource* at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$
- 4.3.8.11  $SUDG\text{Ref}_{h,b}$  designates the *reference level value* for the *start-up offer* for the *resource* at bus  $b \in B^{NQS}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 4.3.8.12  $SNL\text{Ref}_{h,b}$  designates the *reference level value* for the *speed no-load offer* for the *resource* at bus  $b \in B^{NQS}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 4.3.8.13  $PLTMLP\text{Ref}_{h,b,k'}$  designates the *reference level value* for the *energy* up to the *minimum loading point reference level* lamination  $k' \in K_{h,b}^{LTMLP}$  of the *offer* for the *resource* at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 4.3.8.14  $CTEn\text{Thresh1}^{NCA}$  designates the conduct threshold for a *resource* in a *narrow constrained area* as a percent increase above the *reference level value* of the *energy offer* for the *resource* and is equal to 50%;
- 4.3.8.15  $CTEn\text{Thresh2}^{NCA}$  designates the conduct threshold for a *resource* in a *narrow constrained area* as a \$/MWh increase above the *reference level value* of the *energy offer* for the *resource* and is equal to \$25/MWh;
- 4.3.8.16  $CTSUThresh^{NCA}$  designates the conduct threshold for a *resource* in a *narrow constrained area* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 25%;
- 4.3.8.17  $CTSNLThresh^{NCA}$  designates the conduct threshold for a *resource* in a *narrow constrained area* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 25%;
- 4.3.8.18  $CTEn\text{Thresh1}^{DCA}$  designates the conduct threshold for a *resource* in a *dynamic constrained area* as a percent increase above the *reference level value* of the *energy offer* for the *resource* and is equal to 50%;
- 4.3.8.19  $CTEn\text{Thresh2}^{DCA}$  designates the conduct threshold for a *resource* in a *dynamic constrained area* as a \$/MWh increase above the *reference level value* of the *energy offer* for the *resource* and is equal to \$25/MWh;
- 4.3.8.20  $CTSUThresh^{DCA}$  designates the conduct threshold for a *resource* in a *dynamic constrained area* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 25%;

- 4.3.8.21 *CTSNLThresh<sup>DCA</sup>* designates the conduct threshold for a *resource* in a *dynamic constrained area* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 25%;
- 4.3.8.22 *CTEnThresh1<sup>BCA</sup>* designates the conduct threshold for a *resource* in a *broad constrained area* as a percent increase above the *reference level value* of the *energy offer* for the *resource* and is equal to 300%;
- 4.3.8.23 *CTEnThresh2<sup>BCA</sup>* designates the conduct threshold for a *resource* in a *broad constrained area* as a \$/MWh increase above the *reference level value* of the *energy offer* for the *resource* and is equal to \$100/MWh;
- 4.3.8.24 *CTSUThresh<sup>BCA</sup>* designates the conduct threshold for a *resource* in a *broad constrained area* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 100%;
- 4.3.8.25 *CTSNLThresh<sup>BCA</sup>* designates the conduct threshold for a *resource* in a *broad constrained area* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 100%;
- 4.3.8.26 *CTEnThresh1<sup>GMP</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *energy offer* for the *resource* and is equal to 300%;
- 4.3.8.27 *CTEnThresh2<sup>GMP</sup>* designates the global market power conduct threshold for a *resource* as a \$/MWh increase above the *reference level value* of the *energy offer* for the *resource* and is equal to \$100 MW/h;
- 4.3.8.28 *CTSUThresh<sup>GMP</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 100%;
- 4.3.8.29 *CTSNLThresh<sup>GMP</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 100%;

- 4.3.8.30 *CTORThresh1<sup>ORL</sup>* designates the local market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *operating reserve offer* for the *resource* and is equal to 10%;
- 4.3.8.31 *CTORThresh2<sup>ORL</sup>* designates the local market power conduct threshold for a *resource* as a \$/MW increase above the *reference level value* of the *operating reserve offer* for the *resource* and is equal to \$25/MW;
- 4.3.8.32 *CTEnThresh1<sup>ORL</sup>* designates the local market power conduct threshold for *energy to minimum loading point* for a *resource* as a percent increase above the *reference level value* of the *offer for energy* up to the *minimum loading point* for the *resource* and is equal to 10%;
- 4.3.8.33 *CTEnThresh2<sup>ORL</sup>* designates the local market power conduct threshold for *energy to minimum loading point* conduct threshold for a *resource* as a \$/MW increase above the *reference level value* of the *energy for energy* up to the *minimum loading point* for the *resource* and is equal to \$25/MW;
- 4.3.8.34 *CTSUThresh<sup>ORL</sup>* designates the local market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 10%;
- 4.3.8.35 *CTSNLThresh<sup>ORL</sup>* designates the local market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 10%;
- 4.3.8.36 *CTORThresh1<sup>ORG</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *operating reserve offer* for the *resource* and is equal to 50%;
- 4.3.8.37 *CTORThresh2<sup>ORG</sup>* designates the global market power conduct threshold for a *resource* as a \$/MW increase above the *reference level value* of the *operating reserve offer* for the *resource* and is equal to \$25/MW;
- 4.3.8.38 *CTEnThresh1<sup>ORG</sup>* designates the global market power conduct threshold for *energy to minimum loading point* for a *resource* as a percent increase above the *reference level value* of the *offer for energy* up to the *minimum loading point* for the *resource* and is equal to 50%;

- 4.3.8.39 *CTEnThresh2<sup>ORG</sup>* designates the global market power conduct threshold for *energy* to *minimum loading point* for a *resource* as a \$/MW increase above the *reference level value* of the *offer* for *energy* up to the *minimum loading point* for the *resource* and is equal to \$25/MW;
- 4.3.8.40 *CTSUThresh<sup>ORG</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 25%;
- 4.3.8.41 *CTSNLThresh<sup>ORG</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 25%;
- 4.3.8.42 *CTEnMinOffer* designates the minimum price for the *offer* lamination for *energy* to be included in the Conduct Test. *Offer* laminations for *energy* below this value are excluded from the Conduct Test and is equal to \$25/MWh;
- 4.3.8.43 *CTORMinOffer* designates the minimum price for the *offer* lamination for *operating reserve* to be included in the Conduct Test. *Offer* laminations for *operating reserve* below this value are excluded from the Conduct Test and is equal to \$5/MW;
- 4.3.8.44 *ITThresh1<sup>NCA</sup>* designates the price impact threshold for a *resource* in a *narrow constrained area* as a percent increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to 50%;
- 4.3.8.45 *ITThresh2<sup>NCA</sup>* designates the price impact threshold for a *resource* in a *narrow constrained area* as a \$/MWh increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to \$25/MWh;
- 4.3.8.46 *ITThresh1<sup>DCA</sup>* designates the price impact threshold for a *resource* in a *dynamic constrained area* as a percent increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to 50%;
- 4.3.8.47 *ITThresh2<sup>DCA</sup>* designates the price impact threshold for a *resource* in a *dynamic constrained area* as a \$/MWh increase in the *energy locational marginal price* output from section 9 above the *energy*

*locational marginal price* output from section 13 and is equal to \$25/MWh;

- 4.3.8.48  $ITThresh1^{BCA}$  designates the price impact threshold for a *resource* in a broad constrained area as a percent increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to 100%;
- 4.3.8.49  $ITThresh2^{BCA}$  designates the price impact threshold for a *resource* in a broad constrained area as a \$/MWh increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to \$50/MWh;
- 4.3.8.50  $ITThresh1^{GMP}$  designates the global market power price impact threshold for a *resource* as a percent increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to 100%;
- 4.3.8.51  $ITThresh2^{GMP}$  designates the global market power price impact threshold for a *resource* as a \$/MWh increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to \$50/MWh;
- 4.3.8.52  $ITThresh1^{ORG}$  designates the global market power price impact threshold for a *resource* as a percent increase in the *operating reserve locational marginal price* output from section 9 above the *operating reserve locational marginal price* output from section 13 and is equal to 50%; and
- 4.3.8.53  $ITThresh2^{ORG}$  designates the global market power price impact threshold for a *resource* as a \$/MW increase in the *operating reserve locational marginal price* output from section 9 above the *operating reserve locational marginal price* output from section 13 and is equal to \$25/MW.

#### 4.3.9 Weighting Factors for Zonal Prices

- 4.3.9.1  $WF_{h,m,b}^{VIRT}$  designates the weighting factor for bus  $b \in L_m^{VIRT}$  used to calculate the price for *virtual transaction zone*  $m \in M$  for hour  $h \in \{1, \dots, 24\}$ ;

- 4.3.9.2  $WF_{h,y,b}^{NDL}$  designates the weighting factor for bus  $b \in L_y^{NDL}$  used to calculate the price for *non-dispatchable load* zone  $y \in Y$  for hour  $h \in \{1, \dots, 24\}$ ; and
- 4.3.9.3 The weighting factors in section 4.3.9.1 and section 4.3.9.2 shall be obtained by renormalizing the load distribution factors so that for a given hour the sum of weighting factors for a *non-dispatchable load* zone or for a *virtual transaction zone* is one.

## 4.4 Other Data Parameters

### 4.4.1 Non-Dispatchable Demand Forecast

- 4.4.1.1  $AFL_h$  designates the average province-wide *non-dispatchable demand* forecast for hour  $h \in \{1, \dots, 24\}$  calculated by the *security* assessment function; and
- 4.4.1.2  $PFL_h$  designates the peak province-wide *non-dispatchable demand* forecast for hour  $h \in \{1, \dots, 24\}$  calculated by the *security* assessment function.

### 4.4.2 Variable Generation

- 4.4.2.1  $AFG_{h,b}$  designates the alternative forecast for a *variable generation resource* identified by bus  $b \in B^{VG}$  in hour  $h \in \{1, \dots, 24\}$ , which is either the *registered market participant*-submitted forecast or the *IESOs* centralized forecast.

### 4.4.3 Internal Transmission Constraints

- 4.4.3.1  $PreConSF_{h,f,b}$  designates the pre-contingency sensitivity factor for bus  $b \in B \cup D$  indicating the fraction of *energy* injected at bus  $b$  which flows on *facility*  $f$  during hour  $h$  under pre-contingency conditions;
- 4.4.3.2  $VPreConSF_{h,f,m}$  designates the pre-contingency sensitivity factor for *virtual transaction zone*  $m \in M$  indicating the effect of scheduled *energy* at  $m$  to flows on *facility*  $f \in F_h$  in hour  $h$  under pre-contingency conditions. It shall be determined as the weighted average of the pre-contingency sensitivity factors for *non-dispatchable loads*, *dispatchable loads*, *hourly demand response resources*, and *price responsive loads* within the *virtual transaction zone* using the weighting factors  $WF_{h,m,b}^{VIRT}$  for *virtual transactions*;

- 4.4.3.3  $AdjNormMaxFlow_{h,f}$  designates the limit corresponding to the maximum flow allowed on *facility*  $f$  in hour  $h$  under pre-contingency conditions;
  - 4.4.3.4  $SF_{h,c,f,b}$  designates the post-contingency sensitivity factor for bus  $b \in B \cup D$  indicating the fraction of *energy* injected at bus  $b$  which flows on *facility*  $f$  during hour  $h$  under post-contingency conditions for contingency  $c$ ;
  - 4.4.3.5  $VSF_{h,c,f,m}$  designates the post-contingency sensitivity factor for *virtual transaction zone*  $m \in M$  indicating the effect of scheduled *energy* at  $m$  to flows on *facility*  $f \in F_{h,c}$  in hour  $h$  under post-contingency conditions for contingency  $c$ . It shall be determined as the weighted average of the post-contingency sensitivity factors for *non-dispatchable loads*, *dispatchable loads*, *hourly demand response resources*, and *price responsive loads* within the *virtual transaction zone* using the weighting factors  $WF_{h,m,b}^{VIRT}$  for *virtual transactions*; and
  - 4.4.3.6  $AdjEmMaxFlow_{h,c,f}$  designates the limit corresponding to the maximum flow allowed on *facility*  $f$  in hour  $h$  under post-contingency conditions for contingency  $c$ .
- 4.4.4 Transmission Losses
- 4.4.4.1  $LossAdj_h$  designates any adjustment needed for hour  $h \in \{1, \dots, 24\}$  to correct for any discrepancy between Ontario total system losses calculated using a base case power flow from the *security* assessment function and linearized losses that would be calculated using the marginal loss factors.
  - 4.4.4.2  $MglLoss_{h,b}$  designates the marginal loss factor and represent the marginal impact on transmission losses resulting from transmitting *energy* from the *reference bus* to serve an increment of additional load at *resource* bus  $b \in B \cup D$  in hour  $h \in \{1, \dots, 24\}$ ; and
  - 4.4.4.3  $VMglLoss_{h,m}$  designates the marginal loss factor for *virtual transaction zone*  $m \in M$  in hour  $h \in \{1, \dots, 24\}$ . It shall be determined as the weighted average of the marginal loss factors for *non-dispatchable loads*, *dispatchable loads*, *hourly demand response resources*, and *price responsive loads* within the *virtual transaction zone* using the weighting factors  $WF_{h,m,b}^{VIRT}$  for *virtual transactions*.

## 5 Initialization

### 5.1 Purpose

- 5.1.1 The initialization processes set out in this section 5 shall occur prior to the execution of the *day-ahead market calculation engine* described in section 2.1.1 above.

### 5.2 Reference Bus

- 5.2.1 The *IESO* shall use Richview Transformer Station as the *day-ahead market calculation engine's* default *reference bus* for the calculation of *locational marginal prices*.
- 5.2.2 If the default *reference bus* is out of service, another in-service bus shall be selected.

### 5.3 Islanding Conditions

- 5.3.1 In the event of a network split, the *day-ahead market calculation engine* shall:
- 5.3.1.1 only evaluate *resources* that are within the *main island*;
  - 5.3.1.2 use only forecasts of *demand* forecast areas in the *main island*; and
  - 5.3.1.3 use a bus within the *main island* in place of the *reference bus* if the *reference bus* does not fall within the *main island*.

### 5.4 Variable Generation Tie-Breaking

- 5.4.1 For each hour  $h \in \{1, \dots, 24\}$ , each *variable generation resource* bus  $b \in B^{VG}$  and each *offer* lamination  $k \in K_{h,b}^E$ , the *offer* price  $PDG_{h,b,k}$  shall be modified to  $PDG_{h,b,k} - (\frac{TBM_b}{NumVG})\rho$ , where  $\rho$  is a small nominal value of order  $10^{-4}$ .

### 5.5 Pseudo-Unit Constraints

- 5.5.1 Constraints for *pseudo-units* corresponding to minimum and maximum constraints on physical *resources* shall be determined in accordance with section 22.

### 5.6 Initial Scheduling Assumptions

- 5.6.1 Initial Schedules



5.6.1.1 The following parameters designate the initial *energy* schedules used for hour 0 in the optimization of the next *dispatch day* and shall be based on the hour ending 24 schedules of the most recent execution of the *pre-dispatch calculation engine* prior to the execution of the *day-ahead market calculation engine*:

5.6.1.1.1  $SDL_{0,b,jt}$  which designates the amount of *energy* that a *dispatchable load* is scheduled to consume at bus  $b \in B^{DL}$ ;

5.6.1.1.2  $SHDR_{0,b,jt}$  which designates the amount of *energy* an *hourly demand response resource* is scheduled to reduce consumption at bus  $b \in B^{HDR}$ ;

5.6.1.1.3  $SXL_{0,d,jt}$  which designates the amount of *energy* a *boundary entity resource* is scheduled to export at bus  $d \in DX$ ;

5.6.1.1.4  $SDG_{0,b,kt}$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$ ;

5.6.1.1.5  $SCT_{0,b,t}$  which designates the schedule of the combustion turbine *resource* associated with the *pseudo-unit* at bus  $b \in B^{PSU}$ ;

5.6.1.1.6  $SST_{0,p,t}$  which designates the schedule of steam turbine *resource*  $p \in PST$ ;

5.6.1.1.7  $SIG_{0,d,kt}$  which designates the amount of *energy* that a *boundary entity resource* is scheduled to import from *intertie zone* bus  $d \in DI$ ;

5.6.1.2 The initial schedules for *non-quick start resources* shall be determined to align with the commitment status logic described in section 5.6.2.

5.6.2 The following parameters designate the initial commitment status and number of hours in operation used for hour 0 in the optimization of the next *dispatch day*:

5.6.2.1  $ODG_{0,b,t}$  which designates whether the *dispatchable generation resource* at bus  $b \in B^{NQS}$  has been scheduled at or above its *minimum loading point*;

5.6.2.2  $InitOperHrs_{b,t}$  which designates the number of consecutive hours at the end of previous day for which the *resource* at bus  $b \in B^{NQS}$  was

scheduled to operate at or above its *minimum loading point*. For *resources* with  $ODG_{0,b} = 0$  ,  $InitOperHrs_b$  shall be set to zero.

#### 5.6.3 Initial Net Interchange Schedule

- 5.6.3.1 The initial net *interchange schedule* value shall be the difference between all imports to Ontario and all exports from Ontario in the last hour of the previous day. By default, this value will be based on the most recent schedules from the *pre-dispatch calculation engine*.

## 6 Security Assessment Function

### 6.1 Interaction between the Security Assessment Function and Optimization Functions

- 6.1.1 The scheduling and pricing algorithms of the *day-ahead market calculation engine* shall perform multiple iterations of the optimization functions and the *security* assessment function to check for violations of monitored thermal limits and operating *security limits* using the schedules produced by the optimization functions.
- 6.1.2 As multiple iterations are performed, the transmission constraints produced by the *security* assessment function shall be used by the optimization functions.
- 6.1.3 All three passes of the *day-ahead market calculation engine* shall use the *security* assessment function.
- 6.1.4 The *security* assessment function shall use the physical *resource* representation of *combined cycle plants* that are registered as *pseudo-units*.

### 6.2 Inputs into the Security Assessment Function

- 6.2.1 The *security* assessment function shall use the following inputs:
- 6.2.1.1 the *IESO* average and peak *demand* forecasts; and
  - 6.2.1.2 applicable *IESO-controlled grid* information pursuant to section 3A.1 of Chapter 7.
- 6.2.2 The *security* assessment function shall also use the following outputs of the optimization functions in Pass 1 and Pass 3:

- 6.2.2.1 the schedules for *dispatchable loads, hourly demand response resources, and price responsive loads*;
  - 6.2.2.2 the schedules for *non-dispatchable generation resources and dispatchable generation resources*;
  - 6.2.2.3 the schedules for *boundary entity resources* at each *intertie zone*; and
  - 6.2.2.4 the net schedules for *virtual transactions* for each *virtual transaction zone*.
- 6.2.3 The *security* assessment function shall also use the following outputs of the optimization functions in Pass 2:
- 6.2.3.1 the schedules for *dispatchable loads and hourly demand response resources*;
  - 6.2.3.2 the schedules for *non-dispatchable generation resources and dispatchable generation resources*; and
  - 6.2.3.3 the schedules for *boundary entity resources* at each *intertie zone*.

### 6.3 Security Assessment Function Processing

- 6.3.1 In Pass 1 and Pass 3 of the *day-ahead market calculation engine*, the *security* assessment function shall determine the average province-wide non-*dispatchable demand* forecast for hour  $h$ ,  $AFL_h$ , as follows:
- 6.3.1.1 determine forecast MW quantities for all *load resources* and losses using the *IESO* average *demand* forecasts for *demand* forecast areas, load distribution factors, the total of the *bid* quantities submitted for virtual *hourly demand response resources* and physical *hourly demand response resources*; and
  - 6.3.1.2 determine  $AFL_h$  by adding the forecast MW quantities determined for each *non-dispatchable load*, including forecast MW losses in the *demand* forecast areas.
- 6.3.2 In Pass 2 of the *day-ahead market calculation engine*, the *security* assessment function shall determine the peak province-wide non-*dispatchable demand* forecast for hour  $h$ ,  $PFL_h$ , as follows:
- 6.3.2.1 determine forecast MW quantities for all *load resources* and losses using the *IESO* peak *demand* forecasts for *demand* forecast areas, load distribution factors, the total of the *bid* quantities submitted for

virtual *hourly demand response resources* and physical *hourly demand response resources*; and

- 6.3.2.2 determine  $PFL_h$  by adding the forecast MW quantities determined for each *non-dispatchable load*, each *price responsive load*, and each *dispatchable load* with no *bid* for *energy*, including forecast MW losses in the *demand* forecast areas.
- 6.3.3 In Passes 1 and 3 of the *day-ahead market calculation engine*, the security assessment function shall distribute the net schedules for *virtual transactions* in each *virtual transaction zone* to *non-dispatchable loads*, *dispatchable loads*, *hourly demand response resources*, and *price responsive loads* within the *virtual transaction zone* using the weighting factors ( $WF_{h,m,b}^{VIRT}$ ) for *virtual transactions*. In the security assessment function, the total MW quantity allocated to:
  - 6.3.3.1 a *dispatchable load*, an *hourly demand response resource* or a *price responsive load* shall be equal to the schedule determined by the optimization functions plus the amount allocated in the distribution of the net schedules for *virtual transactions*; and
  - 6.3.3.2 a *non-dispatchable load* shall be equal to its forecast MW quantity plus the amount allocated in the distribution of the net schedules for *virtual transactions*.
- 6.3.4 The *security* assessment function shall perform the following calculations and analyses:
  - 6.3.4.1 A base case solution function shall prepare a power flow solution for each hour. The base case solution function shall select the power system model state applicable to the forecast of conditions for the hour and input schedules.
  - 6.3.4.2 The base case solution function shall use an AC power flow analysis. If the AC power flow analysis fails to converge, the base case solution function shall use a non-linear DC power flow analysis. If the non-linear DC power flow analysis fails to converge, the base case solution function shall use a linear DC power flow analysis.
  - 6.3.4.3 If the AC or non-linear DC power flow analysis converges, continuous thermal limits for all monitored equipment and operating *security limits* shall be monitored to check for pre-contingency limit violations.
  - 6.3.4.4 Violated pre-contingency limits shall be linearized using pre-contingency sensitivity factors and incorporated as constraints for use by the optimization functions.

- 6.3.4.5 If the linear DC power flow analysis is used, the pre-contingency *security* assessment may develop linear constraints to facilitate the convergence of the AC or non-linear DC power flow analysis in the subsequent iterations.
- 6.3.4.6 A linear power flow analysis shall be used to simulate contingencies, calculate post-contingency flows and check all monitored equipment for limited-time thermal limit violations.
- 6.3.4.7 Violated post-contingency limits shall be linearized using post-contingency sensitivity factors and incorporated as constraints for use by the optimization functions.
- 6.3.4.8 The base case solution shall be used to calculate Ontario *transmission system* losses, marginal loss factors and loss adjustment for each hour. The impact of losses on branches between the *resource* bus and the *resource connection point* to the *IESO-controlled grid* and losses on branches outside Ontario shall be excluded when determining marginal loss factors.
- 6.3.4.9 The As-Offered Scheduling, Reference Level Scheduling, Mitigated Scheduling, Reliability Scheduling and DAM Scheduling algorithms described in sections 8, 12, 15, 18 and 20, respectively, shall use the marginal loss factors for each hour calculated by the *security* assessment function.
- 6.3.4.10 The As-Offered Pricing, Reference Level Pricing, Mitigated Pricing, and DAM Pricing algorithms described in sections 9, 13, 16 and 21, respectively, shall use the marginal loss factors used in the last iteration of the optimization function in the corresponding scheduling algorithm.

## **6.4 Outputs from the Security Assessment Function**

- 6.4.1 The outputs of the *security* assessment function used in the optimization functions include the following:
  - 6.4.1.1 a set of linearized constraints for all violated pre-contingency and post-contingency limits for each hour. The sensitivities and limits associated with the constraints shall be those provided by the most recent *security* assessment function iteration;
  - 6.4.1.2 pre-contingency and post-contingency sensitivity factors for each hour;

6.4.1.3 the marginal loss factors as described in sections 6.3.4.8-6.3.4.10;  
and

6.4.1.4 loss adjustment quantity for each hour.

## 7 Pass 1: Market Commitment and Market Power Mitigation Pass

7.1.1 Pass 1 shall use *market participant* and *IESO* inputs and *resource* and system constraints to determine a set of *resource* schedules and commitments. Pass 1 shall consist of the following algorithms and tests:

- the As-Offered Scheduling algorithm described in section 8;
- the As-Offered Pricing algorithm described in section 9;
- the Constrained Area Conditions Test described in section 10;
- the Conduct Test described in section 11;
- the Reference Level Scheduling algorithm described in section 12;
- the Reference Level Pricing algorithm described in section 13;
- the Price Impact Test described in section 14;
- the Mitigated Scheduling algorithm described in section 15; and
- the Mitigated Pricing algorithm described in section 16.

## 8 As-Offered Scheduling

### 8.1 Purpose

8.1.1 The As-Offered Scheduling algorithm shall perform a *security*-constrained unit commitment and economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants* to meet the *IESO's* average province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the next *dispatch day*.

## 8.2 Information, Sets, Indices and Parameters

8.2.1 Information, sets, indices and parameters used by the As-Offered Scheduling algorithm are described in sections 3 and 4.

## 8.3 Variables and Objective Function

8.3.1 The As-Offered Scheduling algorithm shall solve for the following variables:

- 8.3.1.1  $SPRL_{h,b,j}$ , which designates the amount of *energy* that a *price responsive load* is scheduled to consume at bus  $b \in B^{PRL}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,b}^E$ ;
- 8.3.1.2  $SDL_{h,b,j}$ , which designates the amount of *energy* that a *dispatchable load* is scheduled to consume at bus  $b \in B^{DL}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,b}^E$ ;
- 8.3.1.3  $S10SDL_{h,b,j}$ , which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,b}^{10S}$ ;
- 8.3.1.4  $S10NDL_{h,b,j}$ , which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,b}^{10N}$ ;
- 8.3.1.5  $S30RDL_{h,b,j}$ , which designates the amount of *thirty-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,b}^{30R}$ ;
- 8.3.1.6  $SHDR_{h,b,j}$ , which designates the amount of *energy* reduction scheduled for an *hourly demand response resource* at bus  $b \in B^{HDR}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,b}^E$ ;
- 8.3.1.7  $SVB_{h,v,j}$ , which designates the amount of *energy* a *virtual zonal resource*  $v \in VB$  is scheduled to withdraw in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,v}^E$ ;
- 8.3.1.8  $SXL_{h,d,j}$ , which designates the amount of *energy* a *boundary entity resource* is scheduled to export at bus  $d \in DX$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,d}^E$ ;

- 8.3.1.9  $S10NXL_{h,d,j}$  which designates the amount of non-synchronized *ten-minute operating reserve* scheduled that a *boundary entity resource* is scheduled to provide at bus  $d \in DX$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,d}^{10N}$ ;
- 8.3.1.10  $S30RXL_{h,d,j}$  which designates the amount of *thirty-minute operating reserve* scheduled that a *boundary entity resource* is scheduled to provide at bus  $d \in DX$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,d}^{30R}$ ;
- 8.3.1.11  $SNDG_{h,b,k}$  which designates the amount of *energy* that a *non-dispatchable generation resource* is scheduled to provide at bus  $b \in B^{NDG}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^E$ ;
- 8.3.1.12  $SDG_{h,b,k}$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide above  $MinQDG_b$  at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^E$ ;
- 8.3.1.13  $ODG_{h,b}$  which designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  has been scheduled at or above its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ ;
- 8.3.1.14  $IDG_{h,b}$  which designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  has been scheduled to reach its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ ;
- 8.3.1.15  $S10SDG_{h,b,k}$  , which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10S}$ ;
- 8.3.1.16  $S10NDG_{h,b,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10N}$ ;
- 8.3.1.17  $S30RDG_{h,b,k}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{30R}$ ;



- 8.3.1.18  $SCT_{h,b}$  which designates the schedule of the combustion turbine *resource* associated with the *pseudo-unit* at bus  $b \in B^{PSU}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 8.3.1.19  $SST_{h,p}$  which designates the schedule of steam turbine *resource*  $p \in PST$  in hour  $h \in \{1, \dots, 24\}$ ;
- 8.3.1.20  $O10R_{h,b}$  which designates whether the *pseudo-unit* at bus  $b \in B^{NO10DF}$  has been scheduled for *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ ;
- 8.3.1.21  $OHO_{h,b}$  which designates whether the *dispatchable* hydroelectric *generation resource* at bus  $b \in B^{HE}$  has been scheduled at or above  $MinHO_{h,b}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 8.3.1.22  $OFR_{h,b,i}$  for  $i \in \{1, \dots, NFor_b\}$ , which designates whether the *dispatchable* hydroelectric *generation resource* at bus  $b \in B^{HE}$  has been scheduled at or below  $ForL_{b,i}$  or, at or above  $ForU_{b,i}$  in hour  $h \in \{1, \dots, 24\}$ ;
- 8.3.1.23  $IHE_{h,b,i}$  which designates whether the *dispatchable* hydroelectric *generation resource* at bus  $b \in B^{HE}$  registered a start between hours  $(h - 1)$  and  $h \in \{1, \dots, 24\}$  as a result of its schedule increasing from below  $StartMW_{b,i}$  to at or above  $StartMW_{b,i}$  for  $i \in \{1, \dots, NStartMW_b\}$ ;
- 8.3.1.24  $SVO_{h,v,k}$  which designates the amount of *energy* a *virtual zonal resource*  $v \in VO$  is scheduled to inject in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,v}^E$ ;
- 8.3.1.25  $SIG_{h,d,k}$ , which designates the amount of *energy* that a *boundary entity resource* is scheduled to import from *intertie zone* bus  $d \in DI$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,d}^E$ ;
- 8.3.1.26  $S10NIG_{h,d,k}$ , which designates the amount of non-synchronized *ten-minute operating reserve* that a *boundary entity resource* is scheduled to provide from *intertie zone* bus  $d \in DI$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,d}^{10N}$ ;
- 8.3.1.27  $S30RIG_{h,d,k}$  which designates the amount of *thirty-minute operating reserve* that a *boundary entity resource* is scheduled to provide from *intertie zone* bus  $d \in DI$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,d}^{30R}$ ;

8.3.1.28  $TB_h$ , which designates any adjustment to the objective function to facilitate pro-rata tie-breaking in hour  $h \in \{1, \dots, 24\}$ , as described in section 8.3.2.1; and

8.3.1.29  $ViolCost_h$ , which designates the cost incurred in order to avoid having the schedules violate constraints for hour  $h \in \{1, \dots, 24\}$ , as described in section 8.3.2.3.

8.3.2 The objective function for the As-Offered Scheduling algorithm shall maximize gains from trade by maximizing the following expression:

$$\sum_{h=1, \dots, 24} \left( ObjPRL_h + ObjDL_h - ObjHDR_h + ObjVB_h + ObjXL_h - ObjNDG_h - ObjDG_h - ObjVO_h - ObjIG_h - TB_h - ViolCost_h \right)$$

Where

$$\begin{aligned} ObjPRL_h &= \sum_{b \in B^{PRL}} \left( \sum_{j \in J_{h,b}^E} SPRL_{h,b,j} \cdot PPRL_{h,b,j} \right) \\ ObjDL_h &= \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^E} SDL_{h,b,j} \cdot PDL_{h,b,j} - \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \cdot P10SDL_{h,b,j} - \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \cdot P10NDL_{h,b,j} - \sum_{j \in J_{h,b}^{30R}} S30RD_{h,b,j} \cdot P30RD_{h,b,j} \right) \\ ObjHDR_h &= \sum_{b \in B^{HDR}} \left( \sum_{j \in J_{h,b}^E} SHDR_{h,b,j} \cdot PHDR_{h,b,j} \right) \\ ObjVB_h &= \sum_{v \in VB} \left( \sum_{j \in J_{h,v}^E} SVB_{h,v,j} \cdot PVB_{h,v,j} \right) \\ ObjXL_h &= \sum_{d \in DX} \left( \sum_{j \in J_{h,d}^E} SXL_{h,d,j} \cdot PXL_{h,d,j} - \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \cdot P10NXL_{h,d,j} - \sum_{j \in J_{h,d}^{30R}} S30RXL_{h,d,j} \cdot P30RXL_{h,d,j} \right) \\ ObjNDG_h &= \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{h,b}^E} SNDG_{h,b,k} \cdot PNDG_{h,b,k} \right) \end{aligned}$$

$$\begin{aligned}
ObjDG_h &= \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \cdot PDG_{h,b,k} + \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \cdot P10SDG_{h,b,k} + \right. \\
&\quad \left. \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \cdot P10NDG_{h,b,k} + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \cdot P30RDG_{h,b,k} \right) \\
&\quad + \sum_{b \in B^{NQS}} (ODG_{h,b} \cdot MGODG_{h,b} + IDG_{h,b} \cdot SUDG_{h,b}) \\
ObjVO_h &= \sum_{v \in VO} \left( \sum_{k \in K_{h,v}^E} SVO_{h,v,k} \cdot PVO_{h,v,k} \right) \\
ObjIG_h &= \sum_{d \in DI} \left( \sum_{k \in K_{h,d}^E} SIG_{h,d,k} \cdot PIG_{h,d,k} + \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \cdot P10NIG_{h,d,k} \right. \\
&\quad \left. + \sum_{k \in K_{h,d}^{30R}} S30RIG_{h,d,k} \cdot P30RIG_{h,d,k} \right)
\end{aligned}$$

8.3.2.1 The tie-breaking term ( $TB_h$ ) shall sum a term for each *bid* or *offer* lamination. For each lamination, this term shall be the product of a small penalty cost and the quantity of the lamination scheduled. The penalty cost shall be calculated by multiplying a base penalty cost of  $TBPen$  by the amount of the lamination scheduled and then dividing by the maximum amount that could have been scheduled. That is:

$$TB_h = TBPRL_h + TBDL_h + TBHDR_h + TBVB_h + TBXL_h + TBNDG_h + TBDG_h + TBVO_h + TBIG_h$$

Where:

$$TBPRL_h = \sum_{b \in B^{PRL}} \left( \sum_{j \in J_{h,b}^E} \frac{(SPRL_{h,b,j})^2 \cdot TBPen}{QPRL_{h,b,j}} \right);$$

$$TBDL_h = \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^E} \left( \frac{(SDL_{h,b,j})^2 \cdot TBPen}{QDL_{h,b,j}} \right) + \sum_{j \in J_{h,b}^{10S}} \left( \frac{(S10SDL_{h,b,j})^2 \cdot TBPen}{Q10SDL_{h,b,j}} \right) + \right. \\ \left. \sum_{j \in J_{h,b}^{10N}} \left( \frac{(S10NDL_{h,b,j})^2 \cdot TBPen}{Q10NDL_{h,b,j}} \right) + \sum_{j \in J_{h,b}^{30R}} \left( \frac{(S30RDL_{h,b,j})^2 \cdot TBPen}{Q30RDL_{h,b,j}} \right) \right);$$

$$TBHDR_h = \sum_{b \in B^{HDR}} \left( \sum_{j \in J_{h,b}^E} \frac{(SHDR_{h,b,j})^2 \cdot TBPen}{QHDR_{h,b,j}} \right);$$

$$TBVB_h = \sum_{v \in VB} \left( \sum_{j \in J_{h,v}^E} \frac{(SVB_{h,v,j})^2 \cdot TBPen}{QVB_{h,v,j}} \right);$$

$$TBXL_h = \sum_{d \in DX} \left( \sum_{j \in J_{h,d}^E} \left( \frac{(SXL_{h,d,j})^2 \cdot TBPen}{QXL_{h,d,j}} \right) + \sum_{j \in J_{h,d}^{10N}} \left( \frac{(S10NXL_{h,d,j})^2 \cdot TBPen}{Q10NXL_{h,d,j}} \right) \right. \\ \left. + \sum_{j \in J_{h,d}^{30R}} \left( \frac{(S30RXL_{h,d,j})^2 \cdot TBPen}{Q30RXL_{h,d,j}} \right) \right);$$

$$TBNDG_h = \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{h,b}^E} \left( \frac{(SNDG_{h,b,k})^2 \cdot TBPen}{QNDG_{h,b,k}} \right) \right);$$

$$TBDG_h = \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^E} \left( \frac{(SDG_{h,b,k})^2 \cdot TBPen}{QDG_{h,b,k}} \right) + \sum_{k \in K_{h,b}^{10S}} \left( \frac{(S10SDG_{h,b,k})^2 \cdot TBPen}{Q10SDG_{h,b,k}} \right) + \right. \\ \left. \sum_{k \in K_{h,b}^{10N}} \left( \frac{(S10NDG_{h,b,k})^2 \cdot TBPen}{Q10NDG_{h,b,k}} \right) + \sum_{k \in K_{h,b}^{30R}} \left( \frac{(S30RDG_{h,b,k})^2 \cdot TBPen}{Q30RDG_{h,b,k}} \right) \right);$$

$$TBVO_h = \sum_{v \in VO} \left( \sum_{k \in K_{h,v}^E} \frac{(SVO_{h,v,k})^2 \cdot TBPen}{QVO_{h,v,k}} \right);$$

and

$$TBIG_h = \sum_{d \in DI} \left( \sum_{k \in K_{h,d}^E} \left( \frac{(SIG_{h,d,k})^2 \cdot TBPen}{QIG_{h,d,k}} \right) + \sum_{k \in K_{h,d}^{10N}} \left( \frac{(S10NIG_{h,d,k})^2 \cdot TBPen}{Q10NIG_{h,d,k}} \right) + \sum_{k \in K_{h,d}^{30R}} \left( \frac{(S30RIG_{h,d,k})^2 \cdot TBPen}{Q30RIG_{h,d,k}} \right) \right).$$

8.3.2.2  $ViolCost_h$  shall be calculated for hour  $h \in \{1, \dots, 24\}$  using the following variables:

- 8.3.2.2.1  $SLdViol_{h,i}$  which designates the violation variable associated with segment  $i \in \{1, \dots, N_{LdViol_h}\}$  of the penalty curve for the *energy* balance constraint allowing under-generation;
- 8.3.2.2.2  $SGenViol_{h,i}$  which designates the violation variable associated with segment  $i \in \{1, \dots, N_{GenViol_h}\}$  of the penalty curve for the *energy* balance constraint allowing over-generation;
- 8.3.2.2.3  $S10SViol_{h,i}$  which designates the violation variable associated with segment  $i \in \{1, \dots, N_{10SViol_h}\}$  of the penalty curve for the synchronized *ten-minute operating reserve* requirement;
- 8.3.2.2.4  $S10RViol_{h,i}$  which designates the violation variable associated with segment  $i \in \{1, \dots, N_{10RViol_h}\}$  of the penalty curve for the total *ten-minute operating reserve* requirement;
- 8.3.2.2.5  $S30RViol_{h,i}$  which designates the violation variable associated with segment  $i \in \{1, \dots, N_{30RViol_h}\}$  of the penalty curve for the *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement;
- 8.3.2.2.6  $SREG10RViol_{r,h,i}$  which designates the violation variable associated with segment  $i \in \{1, \dots, N_{REG10RViol_h}\}$  of the penalty curve for violating the area total *ten-minute*

*operating reserve* minimum requirement in region  $r \in ORREG$ ;

- 8.3.2.2.7  $SREG30RViol_{r,h,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{REG30RViol_h}\}$  of the penalty curve for violating the area *thirty-minute operating reserve* minimum requirement in region  $r \in ORREG$ ;
- 8.3.2.2.8  $SXREG10RViol_{r,h,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{XREG10RViol_h}\}$  of the penalty curve for violating the area total *ten-minute operating reserve* maximum restriction in region  $r \in ORREG$ ;
- 8.3.2.2.9  $SXREG30RViol_{r,h,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{XREG30RViol_h}\}$  of the penalty curve for violating the area *thirty-minute operating reserve* maximum restriction in region  $r \in ORREG$ ;
- 8.3.2.2.10  $SPreITLViol_{f,h,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{PreITLViol_{f,h}}\}$  of the penalty curve for violating the pre-contingency transmission limit for *facility*  $f \in F$ ;
- 8.3.2.2.11  $SITLViol_{c,f,h,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{ITLViol_{c,f,h}}\}$  of the penalty curve for violating the post-contingency transmission limit for *facility*  $f \in F$  and contingency  $c \in C$ ;
- 8.3.2.2.12  $SPreXTLViol_{z,h,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{PreXTLViol_{z,h}}\}$  of the penalty curve for violating the import/export limit associated with *intertie* limit constraint  $z \in Z_{Sch}$ ;
- 8.3.2.2.13  $SNIUViol_{h,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{NIUViol_h}\}$  of the penalty curve for exceeding the net interchange increase limit between hours  $(h - 1)$  and  $h$ ;
- 8.3.2.2.14  $SNIDViol_{h,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{NIDViol_h}\}$  of the penalty curve for exceeding the net interchange decrease limit between hours  $(h - 1)$  and  $h$ ;

- 8.3.2.2.15  $SMaxDelViol_{h,b,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{MaxDelViol_h}\}$  of the penalty curve for exceeding the *maximum daily energy limit* constraint for a *resource* at bus  $b \in B^{ELR}$ ;
- 8.3.2.2.16  $SMinDelViol_{h,b,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{MinDelViol_h}\}$  of the penalty curve for violating the *minimum daily energy limit* constraint for a *resource* at bus  $b \in B^{HE}$ ;
- 8.3.2.2.17  $SSMaxDelViol_{h,s,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{SSMaxDelViol_h}\}$  of the penalty curve for exceeding the shared *maximum daily energy limit* constraint for *dispatchable* hydroelectric *generation resources* in set  $s \in SHE$ ;
- 8.3.2.2.18  $SSMinDelViol_{h,s,i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{SSMinDelViol_h}\}$  of the penalty curve for violating the shared *minimum daily energy limit* constraint for *dispatchable* hydroelectric *generation resources* in set  $s \in SHE$ ;
- 8.3.2.2.19  $SOGenLnkViol_{h,(b_1,b_2),i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{OGenLnkViol_h}\}$  of the penalty curve for violating the linked *dispatchable* hydroelectric *generation resources* constraint by over-generating the downstream *resource*, for  $(b_1,b_2) \in LNK$  such that  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ ; and
- 8.3.2.2.20  $SUGenLnkViol_{h,(b_1,b_2),i}$ , which designates the violation variable associated with segment  $i \in \{1, \dots, N_{UGenLnkViol_h}\}$  of the penalty curve for violating the linked *dispatchable* hydroelectric *generation resources* constraint by under-generating the downstream *resource*, for  $(b_1,b_2) \in LNK$  such that  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ .

8.3.2.3  $ViolCost_h$  shall be calculated as follows:

$$\begin{aligned}
 ViolCost_h = & \sum_{i=1..N_{LdViol_h}} S_{LdViol_h,i} \cdot P_{LdViolSch_h,i} \\
 & - \sum_{i=1..N_{GenViol_h}} S_{GenViol_h,i} \cdot P_{GenViolSch_h,i} \\
 & + \sum_{i=1..N_{10SViol_h}} S_{10SViol_h,i} \cdot P_{10SViolSch_h,i} \\
 & + \sum_{i=1..N_{10RViol_h}} S_{10RViol_h,i} \cdot P_{10RViolSch_h,i} \\
 & + \sum_{i=1..N_{30RViol_h}} S_{30RViol_h,i} \cdot P_{30RViolSch_h,i} \\
 & + \sum_{r \in ORREG} \left( \sum_{i=1..N_{REG10RViol_h}} S_{REG10RViol_{r,h,i}} \right. \\
 & \quad \left. \cdot P_{REG10RViolSch_{h,i}} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{i=1..N_{REG30RViol_h}} S_{REG30RViol_{r,h,i}} \right. \\
 & \quad \left. \cdot P_{REG30RViolSch_{h,i}} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{i=1..N_{XREG10RViol_h}} S_{XREG10RViol_{r,h,i}} \right. \\
 & \quad \left. \cdot P_{XREG10RViolSch_{h,i}} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{i=1..N_{XREG30RViol_h}} S_{XREG30RViol_{r,h,i}} \right. \\
 & \quad \left. \cdot P_{XREG30RViolSch_{h,i}} \right) \\
 & + \sum_{f \in F_h} \left( \sum_{i=1..N_{PreITLViol_{f,h}}} S_{PreITLViol_{f,h,i}} \right. \\
 & \quad \left. \cdot P_{PreITLViolSch_{f,h,i}} \right) \\
 & + \sum_{c \in C} \sum_{f \in F_{h,c}} \left( \sum_{i=1..N_{ITLViol_{c,f,h}}} S_{ITLViol_{c,f,h,i}} \right)
 \end{aligned}$$



$$\begin{aligned}
& \cdot PITLViolSch_{c,f,h,i} \Big) \\
& + \sum_{z \in Z_{Sch}} \left( \sum_{i=1..N_{PreXTLViol_{z,h}}} SPreXTLViol_{z,h,i} \right. \\
& \quad \cdot PPreXTLViolSch_{z,h,i} \Big) \\
& + \sum_{i=1..N_{NIUViol_h}} SNIUViol_{h,i} \cdot PNIUViolSch_{h,i} \\
& + \sum_{i=1..N_{NIDViol_h}} SNIDViol_{h,i} \cdot PNIDViolSch_{h,i} \\
& + \sum_{b \in B^{ELR}} \left( \sum_{i=1..N_{MaxDelViol_h}} SMaxDelViol_{h,b,i} \right. \\
& \quad \cdot PMaxDelViolSch_{h,i} \Big) \\
& + \sum_{b \in B^{HE}} \left( \sum_{i=1..N_{MinDelViol_h}} SMinDelViol_{h,b,i} \cdot PMinDelViolSch_{h,i} \right) \\
& + \sum_{s \in SHE} \left( \sum_{i=1..N_{SMaxDelViol_h}} SSMaxDelViol_{h,s,i} \cdot PSMaxDelViolSch_{h,i} \right) \\
& + \sum_{s \in SHE} \left( \sum_{i=1..N_{SMinDelViol_h}} SSMinDelViol_{h,s,i} \cdot PSMinDelViolSch_{h,i} \right) \\
& + \sum_{(b_1,b_2) \in LNK} \left( \sum_{i=1..N_{OGenLnkViol_h}} SOGenLnkViol_{h,(b_1,b_2),i} \right. \\
& \quad \cdot POGenLnkViolSch_{h,i} \Big) \\
& + \sum_{(b_1,b_2) \in LNK} \left( \sum_{i=1..N_{UGenLnkViol_h}} SUGenLnkViol_{h,(b_1,b_2),i} \right. \\
& \quad \cdot PUGenLnkViolSch_{h,i} \Big).
\end{aligned}$$

## 8.4 Constraints

8.4.1 The constraints described in sections 8.5, 8.6 and 8.7 apply to the optimization function in the As-Offered Scheduling algorithm.

## 8.5 Dispatch Data Constraints Applying to Individual Hours

### 8.5.1 Scheduling Variable Bounds

8.5.1.1 A Boolean variable,  $ODG_{h,b}$ , shall indicate whether the *resource* at bus  $b \in B^{DG}$  is committed in hour  $h \in \{1, \dots, 24\}$ . A value of zero shall indicate that a *resource* is not committed, while a value of one shall indicate that it is committed. Therefore:

8.5.1.1.1  $ODG_{h,b} \in \{0,1\}$  for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ .

8.5.1.2 *Reliability must-run resources* shall be considered committed for all must-run hours.

8.5.1.3 *Resources* providing *regulation* are considered committed for all the hours that they are regulating.

8.5.1.4 *Dispatchable generation resources* that have *minimum loading points*, *start-up offers*, *speed no-load offers*, *minimum generation block run-times* and *minimum generation block down-times* equal to zero shall be considered committed for all hours.

8.5.1.5 If the *dispatchable generation resource* at bus  $b \in B^{DG}$  is considered committed according to the requirements in sections 8.5.1.2, 8.5.1.3, and 8.5.1.4 in hour  $h \in \{1, \dots, 24\}$ , then:

$$ODG_{h,b} = 1.$$

8.5.1.6 No schedule shall be negative, nor shall any schedule exceed the quantity *offered* for the respective *energy* and *operating reserve* market. Therefore:

$$0 \leq SPRL_{h,b,j} \leq QPRL_{h,b,j} \quad \text{for all } b \in B^{PRL}, j \in J_{h,b}^E;$$

$$0 \leq SDL_{h,b,j} \leq QDL_{h,b,j} \quad \text{for all } b \in B^{DL}, j \in J_{h,b}^E;$$

$$0 \leq S10SDL_{h,b,j} \leq Q10SDL_{h,b,j} \quad \text{for all } b \in B^{DL}, j \in J_{h,b}^{10S};$$

$$0 \leq S10NDL_{h,b,j} \leq Q10NDL_{h,b,j} \quad \text{for all } b \in B^{DL}, j \in J_{h,b}^{10N};$$

$$\begin{aligned}
0 \leq S30RDL_{h,b,j} &\leq Q30RDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^{30R}; \\
0 \leq SHDR_{h,b,j} &\leq QHDR_{h,b,j} && \text{for all } b \in B^{HDR}, j \in J_{h,b}^E; \\
0 \leq SVB_{h,v,j} &\leq QVB_{h,v,j} && \text{for all } v \in VB, j \in J_{h,v}^E; \\
0 \leq SXL_{h,d,j} &\leq QXL_{h,d,j} && \text{for all } d \in DX, j \in J_{h,d}^E; \\
0 \leq S10NXL_{h,d,j} &\leq Q10NXL_{h,d,j} && \text{for all } d \in DX, j \in J_{h,d}^{10N}; \\
0 \leq S30RXL_{h,d,j} &\leq Q30RXL_{h,d,j} && \text{for all } d \in DX, j \in J_{h,d}^{30R}; \\
0 \leq SNDG_{h,b,k} &\leq QNDG_{h,b,k} && \text{for all } b \in B^{NDG}, k \in K_{h,b}^E; \\
0 \leq SVO_{h,v,k} &\leq QVO_{h,v,k} && \text{for all } v \in VO, k \in K_{h,v}^E; \\
0 \leq SIG_{h,d,k} &\leq QIG_{h,d,k} && \text{for all } d \in DI, k \in K_{h,d}^E; \\
0 \leq S10NIG_{h,d,k} &\leq Q10NIG_{h,d,k} && \text{for all } d \in DI, k \in K_{h,d}^{10N}; \text{ and} \\
0 \leq S30RIG_{h,d,k} &\leq Q30RIG_{h,d,k} && \text{for all } d \in DI, k \in K_{h,d}^{30R} \\
&&& \text{for all hours } h \in \{1, \dots, 24\}.
\end{aligned}$$

8.5.1.7 *Generation resources may be scheduled for energy and/or operating reserve only if  $ODG_{h,b} = 1$ . Therefore, for all hours  $h \in \{1, \dots, 24\}$ :*

$$\begin{aligned}
0 \leq SDG_{h,b,k} &\leq ODG_{h,b} \cdot QDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^E; \\
0 \leq S10SDG_{h,b,k} &\leq ODG_{h,b} \cdot Q10SDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{10S}; \\
0 \leq S10NDG_{h,b,k} &\leq ODG_{h,b} \cdot Q10NDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{10N}; \text{ and} \\
0 \leq S30RDG_{h,b,k} &\leq ODG_{h,b} \cdot Q30RDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{30R}.
\end{aligned}$$

## 8.5.2 Resource Minimums and Maximums for Energy

8.5.2.1 The non-*dispatchable* portion of *price responsive loads* shall always be scheduled. For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{PRL}$ :

$$\sum_{j \in J_{h,b}^E} SPRL_{h,b,j} \geq QPRLFIRM_{h,b}.$$

- 8.5.2.2 A constraint shall limit schedules for *dispatchable loads* within their minimum and maximum consumption for an hour. For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DL}$ :

$$MinDL_{h,b} \leq \sum_{j \in J_{h,b}^E} SDL_{h,b,j} \leq MaxDL_{h,b}.$$

- 8.5.2.3 The non-*dispatchable* portion of *dispatchable loads* shall always be scheduled. For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{h,b}^E} SDL_{h,b,j} \geq QDLFIRM_{h,b}.$$

- 8.5.2.4 A constraint shall limit schedules for *non-dispatchable generation resources* within their minimum and maximum output for an hour. For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{NDG}$ :

$$MinNDG_{h,b} \leq \sum_{k \in K_{h,b}^E} SNDG_{h,b,k} \leq MaxNDG_{h,b}.$$

- 8.5.2.5 A constraint shall limit schedules for *dispatchable generation resources* within their minimum and maximum output for an hour. For a *dispatchable variable generation resource*, the maximum schedule shall be limited by its forecast. That is:

For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ ,

$$AdjMaxDG_{h,b} = \begin{cases} \min(MaxDG_{h,b}, AFG_{h,b}) & \text{if } b \in B^{VG} \\ MaxDG_{h,b} & \text{otherwise} \end{cases}$$

and

$$AdjMinDG_{h,b} = \min(MinDG_{h,b}, AdjMaxDG_{h,b}).$$

For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

$$\begin{aligned} AdjMinDG_{h,b} &\leq MinQDG_b \cdot ODG_{h,b} + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \\ &\leq AdjMaxDG_{h,b}. \end{aligned}$$

- 8.5.2.6 If the commitment status,  $ODG_{h,b'}$  of a *dispatchable generation resource* is equal to 1 and if this status is inconsistent with the adjusted minimum and maximum constraints,  $MinQDG_b > AdjMaxDG_{h,b'}$ , then  $ODG_{h,b}$  shall be changed to a value between 0 and 1.
- 8.5.2.7 If the total *offered* quantity does not exceed the minimum constraint for the *resource*,  $MinQDG_b + \sum_{k \in K_{h,b}^E} QDG_{h,b,k} < AdjMinDG_{h,b'}$ , then the *resource* shall receive a schedule of zero.

### 8.5.3 Off-Market Transactions

- 8.5.3.1 For all hours  $h \in \{1, \dots, 24\}$  and all *intertie zone* buses corresponding to an inadvertent *energy* payback export transaction  $d \in DX_h^{INP}$ :

$$\sum_{j \in J_{h,d}^E} SXL_{h,d,j} = \sum_{j \in J_{h,d}^E} QXL_{h,d,j}.$$

- 8.5.3.2 For all hours  $h \in \{1, \dots, 24\}$  and all *intertie zone* buses corresponding to an inadvertent *energy* payback import transaction  $d \in DI_h^{INP}$ :

$$\sum_{k \in K_{h,d}^E} SIG_{h,d,k} = \sum_{k \in K_{h,d}^E} QIG_{h,d,k}.$$

- 8.5.3.3 For all hours  $h \in \{1, \dots, 24\}$  and all *intertie zone* buses corresponding to an *emergency energy* export  $d \in DX_h^{EM}$ :

$$\sum_{j \in J_{h,d}^E} SXL_{h,d,j} = \sum_{j \in J_{h,d}^E} QXL_{h,d,j}.$$

- 8.5.3.4 For all hours  $h \in \{1, \dots, 24\}$  and all *intertie zone* buses corresponding to *emergency energy* import  $d \in DI_h^{EM}$ :

$$\sum_{k \in K_{h,d}^E} SIG_{h,d,k} = \sum_{k \in K_{h,d}^E} QIG_{h,d,k}.$$

## 8.5.4 Operating Reserve Requirements

8.5.4.1 The total synchronized *ten-minute operating reserve*, non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* scheduled from a *dispatchable load* shall not exceed:

- 8.5.4.1.1 the *dispatchable load's* ramp capability over 30 minutes;
- 8.5.4.1.2 the total scheduled load less the non-*dispatchable* portion; and
- 8.5.4.1.3 the remaining portion of its capacity that is *dispatchable* after considering minimum load consumption constraints.

These restrictions shall be enforced by the following constraints for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} + \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} + \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,j} \leq 30 \cdot ORRD L_b;$$

$$\sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} + \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} + \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,j} \leq \sum_{j \in J_{h,b}^E} SDL_{h,b,j} - QDLFIRM_{h,b};$$

and

$$\sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} + \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} + \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,j} \leq \sum_{j \in J_{h,b}^E} SDL_{h,b,j} - MinDL_{h,b}$$

8.5.4.2 The amount of both synchronized and non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide shall not exceed the amount by which the *dispatchable load* can decrease its load over 10 minutes, as limited by its *operating reserve* ramp rate. This restriction shall be enforced by the following constraint for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} + \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \leq 10 \cdot ORRD L_b$$

- 8.5.4.3 The total non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* scheduled for an hour shall not exceed total scheduled exports. This restriction shall be enforced by the following constraint for all hours  $h \in \{1, \dots, 24\}$  and all *intertie zone* export buses  $d \in DX$ :

$$\sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} + \sum_{j \in J_{h,d}^{30R}} S30RXL_{h,d,j} \leq \sum_{j \in J_{h,d}^E} SXL_{h,d,j}$$

- 8.5.4.4 The total *operating reserve* scheduled from a committed *dispatchable generation resource* shall not exceed that *resource's*: (i) ramp capability over 30 minutes; (ii) remaining capacity; and (iii) unscheduled capacity. These restrictions shall be enforced by the following constraints for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \leq 30 \cdot ORRD G_b;$$

$$\sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \leq \sum_{k \in K_{h,b}^E} (QDG_{h,b,k} - SDG_{h,b,k});$$

and

$$\sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \leq AdjMaxDG_{h,b} - \sum_{k \in K_{h,b}^E} SDG_{h,b,k} - MinQDG_b$$

- 8.5.4.5 The amount of both synchronized and non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall not exceed the amount by which the *resource* can increase its output over 10 minutes, as limited by its *operating reserve* ramp rate. This restriction shall be enforced by the

following constraint for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \leq 10 \cdot ORRDG_b$$

- 8.5.4.6 The amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* may be scheduled to provide shall be limited by its *reserve loading point* for synchronized *ten-minute operating reserve*. This restriction shall be enforced by the following constraint for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$  with  $RLP10S_{h,b} > 0$ :

$$\begin{aligned} \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} &\leq \left( MinQDG_b \cdot ODG_{h,b} + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \right) \\ &\cdot \left( \frac{1}{RLP10S_{h,b}} \right) \\ &\cdot \left( \min \left\{ 10 \cdot ORRDG_b, \sum_{k \in K_{h,b}^{10S}} Q10SDG_{h,b,k} \right\} \right) \end{aligned}$$

- 8.5.4.7 The amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall be limited by its *reserve loading point* for *thirty-minute operating reserve*. This restriction shall be enforced by the following constraint for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$  with  $RLP30R_{h,b} > 0$ :

$$\begin{aligned} \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} &\leq \left( MinQDG_b \cdot ODG_{h,b} + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \right) \cdot \left( \frac{1}{RLP30R_{h,b}} \right) \\ &\cdot \left( \min \left\{ 30 \cdot ORRDG_b, \sum_{k \in K_{h,b}^{30R}} Q30RDG_{h,b,k} \right\} \right) \end{aligned}$$



- 8.5.4.8 The total non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* scheduled for an hour shall not exceed the remaining maximum import *offers* minus scheduled *energy* imports. This restriction shall be enforced by the following constraint for all hours  $h \in \{1, \dots, 24\}$  and all *intertie zone* import buses  $d \in DI$ :

$$\sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} + \sum_{k \in K_{h,d}^{30R}} S30RIG_{h,d,k} \leq \sum_{k \in K_{h,d}^E} (QIG_{h,d,k} - SIG_{h,d,k})$$

## 8.5.5 Pseudo-Units

- 8.5.5.1 A constraint shall be required to calculate physical *generation resource* schedules from *pseudo-unit* schedules using the steam turbine *resource* shares in the operating regions of the *pseudo-unit* determined in section 22. For all hours  $h \in \{1, \dots, 24\}$  and *pseudo-unit* buses  $b \in B^{PSU}$ :

$$SCT_{h,b} = (1 - STShareMLP_b) \cdot MinQDG_b \cdot ODG_{h,b} + (1 - STShareDR_b) \cdot \left( \sum_{k \in K_{h,b}^{DR}} SDG_{h,b,k} \right),$$

and for all hours  $h \in \{1, \dots, 24\}$  and steam turbine *resources*  $p \in PST$ :

$$SST_{h,p} = \sum_{b \in B_p^{ST}} \left( STShareMLP_b \cdot MinQDG_b \cdot ODG_{h,b} + STShareDR_b \cdot \left( \sum_{k \in K_{h,b}^{DR}} SDG_{h,b,k} \right) + \sum_{k \in K_{h,b}^{DF}} SDG_{h,b,k} \right)$$

- 8.5.5.2 Maximum constraints shall be enforced on the operating region to which they apply for both *energy* and *operating reserve* schedules. For all hours  $h \in \{1, \dots, 24\}$  and *pseudo-unit* buses  $b \in B^{PSU}$ :

$$MinQDG_b \cdot ODG_{h,b} \leq MaxMLP_{h,b},$$

$$\sum_{k \in K_{h,b}^{DR}} SDG_{h,b,k} \leq MaxDR_{h,b},$$

$$\sum_{k \in K_{h,b}^{DF}} SDG_{h,b,k} \leq MaxDF_{h,b},$$

and

$$\begin{aligned} \sum_{k \in K_{h,b}^E} SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \\ + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \leq MaxDR_{h,b} + MaxDF_{h,b} \end{aligned}$$

- 8.5.5.3 For a *pseudo-unit* that cannot provide *ten-minute operating reserve* from its duct firing region, constraints shall limit the *pseudo-unit* from being scheduled in its duct firing region whenever the *pseudo-unit* is scheduled for *ten-minute operating reserve*. For all hours  $h \in \{1, \dots, 24\}$  and *pseudo-unit* buses  $b \in B^{NO10DF}$ :

$$O10R_{h,b} \in \{0,1\}$$

$$\begin{aligned} \sum_{k \in K_{h,b}^E} SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \\ \leq MaxDR_{h,b} + (1 - O10R_{h,b}) \cdot MaxDF_{h,b} \end{aligned}$$

and

- 8.5.5.4 For all hours  $h \in \{1, \dots, 24\}$ , *pseudo-unit* buses  $b \in B^{NO10DF}$ , and laminations  $k \in K_{h,b}^{10S}$ :

$$S10SDG_{h,b,k} \leq O10R_{h,b} \cdot Q10SDG_{h,b,k}$$

- 8.5.5.5 For all hours  $h \in \{1, \dots, 24\}$ , *pseudo-unit* buses  $b \in B^{NO10DF}$ , and laminations  $k \in K_{h,b}^{10N}$ :

$$S10NDG_{h,b,k} \leq O10R_{h,b} \cdot Q10NDG_{h,b,k}$$

- 8.5.5.6 For the purposes of the *energy* balance constraint in section 8.7.1 and the transmission constraints in section 8.7.3, the combustion turbine

*resource's* schedule for the *pseudo-unit* at bus  $b \in B^{PSU}$  in hour  $h \in \{1, \dots, 24\}$  shall be equal to:

8.5.5.6.1  $SCT_{h,b}$  if the *pseudo-unit* is scheduled at or above *minimum loading point*,

8.5.5.6.2  $RampCT_{b,w}$  if the *pseudo-unit* is scheduled to reach *minimum loading point* in hour  $(h + w)$  for  $w \in \{1, \dots, RampHrs_b\}$ , or

8.5.5.6.3 0 otherwise.

8.5.5.7 For the purposes of the *energy* balance constraint in section 8.7.1 and the transmission constraints in section 8.7.3, the steam turbine *resource's* schedule for  $p \in PST$  shall be equal to  $SST_{h,p}$  plus any contribution from *pseudo-unit*  $b \in B_p^{ST}$  ramping to *minimum loading point* as given by  $RampST_{b,w}$  for a *pseudo-unit* scheduled to reach *minimum loading point* in hour  $(h + w)$  for  $w \in \{1, \dots, RampHrs_b\}$ .

## 8.5.6 Dispatchable Hydroelectric Generation Resources

8.5.6.1 A *dispatchable* hydroelectric *generation resource* shall be scheduled to at least its *hourly must run* quantity. For all hours  $h \in \{1, \dots, 24\}$  and *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$ :

$$ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \geq MinHMR_{h,b}$$

8.5.6.2 A *dispatchable* hydroelectric *generation resource* shall either be scheduled to 0 or to at least its *minimum hourly output*. For all hours  $h \in \{1, \dots, 24\}$  and all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$

$$OHO_{h,b} \in \{0,1\};$$

$$ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \geq MinHO_{h,b} \cdot OHO_{h,b};$$

and for all  $k \in K_{h,b}^E$ :

$$0 \leq SDG_{h,b,k} \leq OHO_{h,b} \cdot QDG_{h,b,k}$$

- 8.5.6.3 A *dispatchable* hydroelectric *generation resource* shall not be scheduled within its *forbidden regions*. For all hours  $h \in \{1, \dots, 24\}$ , all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$  and all  $i \in \{1, \dots, NFor_b\}$ :

$$OFR_{h,b,i} \in \{0,1\};$$

$$\begin{aligned} ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \\ \leq OFR_{h,b,i} \cdot ForL_{b,i} + (1 - OFR_{h,b,i}) \\ \cdot \left( MinQDG_b + \sum_{k \in K_{h,b}^E} QDG_{h,b,k} \right); \end{aligned}$$

and

$$ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \geq (1 - OFR_{h,b,i}) \cdot ForU_{b,i}$$

## 8.5.7 Linked Wheeling Through Transactions

- 8.5.7.1 The amount of scheduled export *energy* must be equal to the amount of scheduled import *energy* for *linked wheeling through transactions*. For all hours  $h \in \{1, \dots, 24\}$  and all linked *boundary entity resource* buses  $(dx, di) \in L_h$ :

$$\sum_{j \in J_{h,dx}^E} SXL_{h,dx,j} = \sum_{k \in K_{h,di}^E} SIG_{h,di,k}$$

## 8.6 Dispatch Data Inter-Hour/Multi-Hour Constraints

### 8.6.1 Energy Ramping

- 8.6.1.1 For *dispatchable loads*, the constraints in section 8.6.1.5 and section 8.6.2.1 use  $URRDL_b$  to represent a ramp up rate selected from  $URRDL_{h,b,w}$  and use  $DRRDL_b$  to represent a ramp down rate selected from  $DRRDL_{h,b,w}$ .
- 8.6.1.2 For *dispatchable generation resources*, the constraints in section 8.6.1.7 and section 8.6.2.2 use  $URRDG_b$  to represent a ramp up rate selected from  $URRDG_{h,b,w}$  and use  $DRRDG_b$  to represent a ramp down rate selected from  $DRRDG_{h,b,w}$ .

- 8.6.1.3 The *day-ahead market calculation engine* shall respect the ramping restrictions determined by the up to five *offered* MW quantity, ramp up rate and ramp down rate value sets.
- 8.6.1.4 In all ramping constraints, the schedules for hour 0 are obtained from the initial scheduling assumptions in section 5.6. For all hours  $h \in \{1, \dots, 24\}$  the ramping rates in all ramping constraints must be adjusted to allow the applicable *resource* to:
- 8.6.1.4.1 ramp down from its lower limit in hour  $(h - 1)$  to its upper limit in hour  $h$ ; and
- 8.6.1.4.2 ramp up from its upper limit in hour  $(h - 1)$  to its lower limit in hour  $h$ .
- 8.6.1.5 *Energy* schedules for *dispatchable loads* cannot vary by more than an hour's ramping capability for the applicable *resource*. This constraint shall be enforced by the following for all hours  $h \in \{1, \dots, 24\}$  and buses  $b \in B^{DL}$ :

$$\begin{aligned} \sum_{j \in J_{h-1,b}^E} SDL_{h-1,b,j} - 60 \cdot DRRDL_b &\leq \sum_{j \in J_{h,b}^E} SDL_{h,b,j} \\ &\leq \sum_{j \in J_{h-1,b}^E} SDL_{h-1,b,j} + 60 \cdot URRDL_b \end{aligned}$$

- 8.6.1.6 *Energy* schedules for *hourly demand response resources* cannot vary by more than an hour's ramping capability for the applicable *resource*. This constraint shall be enforced by the following for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{HDR}$ :

$$\begin{aligned} \sum_{j \in J_{h-1,b}^E} (QHDR_{h-1,b,j} - SHDR_{h-1,b,j}) - 60 \cdot URRHDR_b &\leq \sum_{j \in J_{h,b}^E} (QHDR_{h,b,j} - SHDR_{h,b,j}) \\ &\leq \sum_{j \in J_{h-1,b}^E} (QHDR_{h-1,b,j} - SHDR_{h-1,b,j}) + 60 \cdot DRRHDR_b \end{aligned}$$

- 8.6.1.7 *Energy* schedules for a *dispatchable generation resource* cannot vary by more than an hour's ramping capability for the applicable *resource*. For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

- 8.6.1.7.1 For the first hour a *resource* reaches its *minimum loading point*, where  $ODG_{h,b} = 1$ ,  $ODG_{h-1,b} = 0$ , the following constraint shall be applied:

$$0 \leq \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \leq 30 \cdot URRDG_b$$

8.6.1.7.2 If the *resource* stays on at or above *minimum loading point* and  $ODG_{h,b} = 1$ ,  $ODG_{h-1,b} = 1$ , the following constraint shall be applied:

$$\begin{aligned} \sum_{k \in K_{h-1,b}^E} SDG_{h-1,b,k} - 60 \cdot DRRDG_b &\leq \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \\ &\leq \sum_{k \in K_{h-1,b}^E} SDG_{h-1,b,k} + 60 \cdot URRDG_b \end{aligned}$$

8.6.1.7.3 For the last hour the *resource* is scheduled at or above *minimum loading point* before being scheduled off, where  $ODG_{h,b} = 1$ ,  $ODG_{h+1,b} = 0$ , the following constraint shall be applied:

$$0 \leq \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \leq 30 \cdot DRRDG_b$$

8.6.1.8 The constraints in sections 8.6.1.6.1 and 8.6.1.6.3 do not apply to a *quick start resource*.

8.6.1.9 For hours where *non-quick start resources* are ramping up to *minimum loading point*, *energy* shall be scheduled using the submitted *ramp up energy to minimum loading point*.

## 8.6.2 Operating Reserve Ramping

8.6.2.1 The total synchronized *ten-minute operating reserve*, non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* from *dispatchable loads* shall not exceed their ramp capability to decrease load consumption and for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DL}$ :

$$\begin{aligned} \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} + \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} + \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,j} \\ \leq \sum_{j \in J_{h,b}^E} SDL_{h,b,j} - \sum_{j \in J_{h-1,b}^E} SDL_{h-1,b,j} + 60 \cdot DRRDL_b \end{aligned}$$

- 8.6.2.2 The total synchronized *ten-minute operating reserve*, non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* from a committed *dispatchable generation resource* shall not exceed its ramp capability to increase generation and for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

$$\begin{aligned} & \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \\ & + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \leq \sum_{k \in K_{h-1,b}^E} SDG_{h-1,b,k} \\ & - \sum_{k \in K_{h,b}^E} SDG_{h,b,k} + 60 \cdot URRDG_b; \\ & \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \\ & + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \\ & \leq [(h - n) \cdot 60 + 30] \cdot URRDG_b \cdot ODG_{h,b} \end{aligned}$$

where  $n$  is the hour of the last start before or in hour  $h$ ; and

$$\begin{aligned} & \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \\ & + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \\ & \leq [(m - h) \cdot 60 + 30] \cdot DRRDG_b \cdot ODG_{h,b} \end{aligned}$$

where  $m$  is the hour of the last shutdown in or after hour  $h$ .

### 8.6.3 Non-Quick Start Resources

- 8.6.3.1 Schedules for *non-quick start resources* shall not violate such *resources' minimum generation block run-times, minimum generation block down-times* and *maximum number of starts per day*.
- 8.6.3.2 A *resource's* previous day's schedule shall be evaluated to determine any remaining *minimum generation block run-time* constraints to enforce and determine the commitment status of the *resource* in hour 0. If  $0 < \text{InitOperHrs}_b < \text{MGBRTDG}_b$ , then the *resource* at bus  $b \in B^{NQS}$  has yet to complete its *minimum generation block run-time*, and:

$$ODG_{1,b}, ODG_{2,b}, \dots, ODG_{\min(24, \text{MGBRTDG}_b - \text{InitOperHrs}_b), b} = 1$$

- 8.6.3.3 If  $ODG_{h-1,b} = 0$ ,  $ODG_{h,b} = 1$ , and  $MGBRTDG_b > 1$  for hour  $h \in \{1, \dots, 24\}$ , then the *resource* at bus  $b \in B^{NQS}$  has been scheduled to start up during hour  $h$  and shall be scheduled to remain in operation until it has completed its *minimum generation block run-time* or to the end of the day. Therefore:

$$ODG_{h+1,b}, ODG_{h+2,b}, \dots, ODG_{\min(24, h + MGBRTDG_b - 1), b} = 1$$

- 8.6.3.4 If  $ODG_{h-1,b} = 1$ ,  $ODG_{h,b} = 0$ , and  $MGBDTDG_b > 1$  for hour  $h \in \{1, \dots, 24\}$ , then the *resource* at bus  $b \in B^{NQS}$  has been scheduled to shut down during hour  $h$  and shall be scheduled to remain off until it has completed its *minimum generation block down-time* or to the end of the day. Therefore:

$$ODG_{h+1,b}, ODG_{h+2,b}, \dots, ODG_{\min(24, h + MGBDTDG_b - 1), b} = 0$$

- 8.6.3.5 *The day-ahead market calculation engine shall not consider start-up offers for non-quick start resources to be scheduled in the first hour of the day if the resource is expected to be scheduled as a result of an operational constraint.*
- 8.6.3.6 A Boolean variable,  $IDG_{h,b}$  indicates that the *non-quick start resource* at bus  $b \in B^{NQS}$  is scheduled to reach its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$  after being scheduled below its *minimum loading point* in the preceding hour. A value of zero shall indicate that a *resource* is not scheduled to reach its *minimum loading point*, while a value of one indicates that it is scheduled to reach its *minimum loading point*. For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{NQS}$ :

$$IDG_{h,b} = \begin{cases} 1 & \text{if } ODG_{h-1,b} = 0 \text{ and } ODG_{h,b} = 1 \\ 0 & \text{otherwise.} \end{cases}$$

- 8.6.3.7 A *non-quick start resource* shall not be scheduled more than its *maximum number of starts per day*. For all buses  $b \in B^{NQS}$ :

$$\sum_{h=1..24} IDG_{h,b} \leq MaxStartsDG_b$$

#### 8.6.4 Energy Limited Resources



8.6.4.1 An *energy limited resource* shall not be scheduled to provide:

8.6.4.1.1 more *energy* than the *maximum daily energy limit* specified for such *resource*; or

8.6.4.1.2 *energy* in amounts that would preclude such *resource* from providing *operating reserve* when activated, for all buses  $b \in B^{ELR}$  where an *energy limited resource* is located and all hours  $H \in \{1, \dots, 24\}$ :

$$\begin{aligned} \sum_{h=1..H} \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \right) \\ + 10ORConv \left( \sum_{k \in K_{H,b}^{10S}} S10SDG_{H,b,k} \right. \\ \left. + \sum_{k \in K_{H,b}^{10N}} S10NDG_{H,b,k} \right) \\ + 30ORConv \left( \sum_{k \in K_{H,b}^{30R}} S30RDG_{H,b,k} \right) \\ - \sum_{i=1..N_{MaxDelViol_H}} SMaxDelViol_{H,b,i} \leq MaxDEL_b \end{aligned}$$

where the factors  $10ORConv$  and  $30ORConv$  are applied to scheduled *ten-minute operating reserve* and *thirty-minute operating reserve* for *energy limited resources* to convert MW into MWh. Violation variables for over-scheduling a *resource's maximum daily energy limit* may be used to allow the *day-ahead market calculation engine* to find a solution.

8.6.5 Dispatchable Hydroelectric Generation Resources

8.6.5.1 *Dispatchable hydroelectric generation resources* shall be scheduled for at least their *minimum daily energy limit*. Violation variables for under-scheduling a *resource's minimum daily energy limit* may be used to allow the *day-ahead market calculation engine* to find a

solution. For all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$ :

$$\sum_{h=1..24} \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} + \sum_{i=1..N_{MinDelViol_h}} SMinDelViol_{h,b,i} \right) \geq MinDEL_b$$

- 8.6.5.2 A Boolean variable,  $IHE_{h,b,i}$  shall indicate that a start for the *dispatchable* hydroelectric *generation resource* at bus  $b \in B^{HE}$  was counted in hour  $h \in \{1, \dots, 24\}$  as a result of the *resource* schedule increasing from below its  $i$ -th *start indication value* to at or above its  $i$ -th *start indication value* for  $i \in \{1, \dots, NStartMW_b\}$ . A value of zero shall indicate that a start was not counted, while a value of one indicates that a start was counted.

Therefore, for all hours  $h \in \{1, \dots, 24\}$ , buses  $b \in B^{HE}$  and start indication values  $i \in \{1, \dots, NStartMW_b\}$ :

$$IHE_{h,b,i} = \begin{cases} 1 & \text{if } \left( ODG_{h-1,b} \cdot MinQDG_b + \sum_{k \in K_{h-1,b}^E} SDG_{h-1,b,k} < StartMW_{b,i} \right) \\ & \text{and } \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \geq StartMW_{b,i} \right) \\ 0 & \text{otherwise.} \end{cases}$$

- 8.6.5.3 *Dispatchable* hydroelectric *generation resources* shall not be scheduled to be started more times than permitted by their *maximum number of starts per day*. The following constraint shall apply for all buses  $b \in B^{HE}$ :

$$\sum_{h=1..24} \left( \sum_{i=1..NStartMW_b} IHE_{h,b,i} \right) \leq MaxStartsHE_b$$

- 8.6.5.4 The schedules for multiple *dispatchable* hydroelectric *generation resources* with a registered *forebay* shall not exceed shared *maximum daily energy limits*. Violation variables for over-scheduling the *maximum daily energy limit* may be used to allow the *day-ahead*

*market calculation engine* to find a solution. For all sets  $s \in SHE$  and all hours  $H \in \{1,..,24\}$ :

$$\begin{aligned}
& \sum_{h=1..H} \left( \sum_{b \in B_S^{HE}} \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \right) \right) \\
& + \sum_{b \in B_S^{HE}} \left( 10ORConv \left( \sum_{k \in K_{H,b}^{10S}} S10SDG_{H,b,k} \right) \right. \\
& \left. + \sum_{k \in K_{H,b}^{10N}} S10NDG_{H,b,k} \right) \\
& + 30ORConv \left( \sum_{k \in K_{H,b}^{30R}} S30RDG_{H,b,k} \right) \\
& - \sum_{i=1..N_{SMaxDelViol_H}} SMaxDelViol_{H,s,i} \\
& \leq MaxSDEL_s
\end{aligned}$$

where the factors  $10ORConv$  and  $30ORConv$  shall be applied to scheduled *ten-minute operating reserve* and *thirty-minute operating reserve* to convert MW into MWh.

- 8.6.5.5 Schedules for multiple *dispatchable hydroelectric generation resources* with a registered *forebay* shall respect shared *minimum daily energy limits*. Violation variables for under-scheduling the *minimum daily energy limit* may be used to allow the *day-ahead market calculation engine* to find a solution. For all sets  $s \in SHE$ :

$$\begin{aligned}
& \sum_{h=1..24} \left( \sum_{b \in B_S^{HE}} \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \right) \right. \\
& \left. + \sum_{i=1..N_{SMinDelViol_h}} SMinDelViol_{h,s,i} \right) \\
& \geq MinSDEL_s
\end{aligned}$$

- 8.6.5.6 For linked *dispatchable hydroelectric generation resources* with a registered *forebay*, *energy* scheduled at the upstream *resources* in one hour shall result in a proportional amount of *energy* being

scheduled at the linked downstream *resources* in the hour determined by the *time lag*.

- 8.6.5.7 For all linked *dispatchable* hydroelectric *generation resources* between upstream *resources*  $b_1 \in B_{up}^{HE}$  and downstream *resources*  $b_2 \in B_{dn}^{HE}$  for  $(b_1, b_2) \in LNK$  and hours  $h \in \{1, \dots, 24\}$  such that  $h + Lag_{b_1, b_2} \leq 24$ :

$$\begin{aligned} \sum_{b_2 \in B_{dn}^{HE}} & \left( ODG_{h+Lag_{b_1, b_2}, b_2} \cdot MinQDG_{b_2} + \sum_{k \in K_{b_2, h+Lag_{b_1, b_2}}^E} SDG_{k, h+Lag_{b_1, b_2}, b_2} \right) \\ & - \sum_{i=1..N_{OGenLnkViol_{h+Lag_{b_1, b_2}}}} SOGenLnkViol_{h+Lag_{b_1, b_2}, (b_1, b_2), i} \\ & + \sum_{i=1..N_{UGenLnkViol_{h+Lag_{b_1, b_2}}}} SUGenLnkViol_{h+Lag_{b_1, b_2}, (b_1, b_2), i} \\ & = MWhRatio_{b_1, b_2} \\ & \cdot \sum_{b_1 \in B_{up}^{HE}} \left( ODG_{h, b_1} \cdot MinQDG_{b_1} + \sum_{k \in K_{b_1, h}^E} SDG_{k, h, b_1} \right) \end{aligned}$$

## 8.7 Constraints for Reliability Requirements

### 8.7.1 Energy Balance

- 8.7.1.1 The total amount of *energy* withdrawals scheduled at load bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ ,  $With_{h,b}$  shall be:

$$With_{h,b} = \begin{cases} \sum_{j \in J_{h,b}^E} SPRL_{h,b,j} & \text{if } b \in B^{PRL} \\ \sum_{j \in J_{h,b}^E} SDL_{h,b,j} & \text{if } b \in B^{DL} \\ \sum_{j \in J_{h,b}^E} (QHDR_{h,b,j} - SHDR_{h,b,j}) & \text{if } b \in B^{HDR} \end{cases}$$

- 8.7.1.2 The net *energy* withdrawal for *virtual transaction zone*  $m \in M$  in hour  $h \in \{1, \dots, 24\}$ ,  $VWith_{h,m}$ , as all *bids* scheduled from *virtual*

*transactions* for *energy* less all *offers* scheduled from *virtual transaction* for *energy* shall be:

$$VWith_{h,m} = \left( \sum_{v \in VB_m} \sum_{j \in J_{h,v}^E} SVB_{h,v,j} \right) - \left( \sum_{v \in VO_m} \sum_{k \in K_{h,v}^E} SVO_{h,v,k} \right)$$

- 8.7.1.3 The total amount of export *energy* scheduled at *intertie zone* bus  $d \in DX$  in hour  $h \in \{1, \dots, 24\}$ ,  $With_{h,d}$ , as the exports from Ontario to the *intertie zone* bus shall be:

$$With_{h,d} = \sum_{j \in J_{h,d}^E} SXL_{h,d,j}$$

- 8.7.1.4 The total amount of injections scheduled at internal bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ ,  $Inj_{h,b}$ , shall be:

$$Inj_{h,b} = OfferInj_{h,b} + RampInj_{h,b}$$

where

$$OfferInj_{h,b} = \begin{cases} \sum_{k \in K_{h,b}^E} SNDG_{h,b,k} & \text{if } b \in B^{NDG} \\ ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} & \text{if } b \in B^{DG} \end{cases}$$

and

$$RampInj_{h,b} = \begin{cases} \sum_{w=1..min(RampHrs_b, 24-h)} RampE_{b,w} \cdot IDG_{h+w,b} & \text{if } b \in B^{NQS} \\ 0 & \text{otherwise} \end{cases}$$

- 8.7.1.5 The total amount of import *energy* scheduled at *intertie zone* bus  $d \in DI$  in hour  $h \in \{1, \dots, 24\}$ ,  $Inj_{h,d}$ , as the imports into Ontario from that *intertie zone* bus shall be:

$$Inj_{h,d} = \sum_{k \in K_{h,d}^E} SIG_{h,d,k}$$

- 8.7.1.6 Injections and withdrawals at each bus shall be multiplied by one plus the marginal loss factor calculated by the *security* assessment function to reflect the losses or reduction in losses that result when injections or withdrawals occur at locations other than the *reference bus*. These loss-adjusted injections and withdrawals must then be equal to each other after taking into account the adjustment for any discrepancy between total and marginal losses. Load or generation reduction associated with the *demand* constraint violation shall be subtracted from the total load or generation for the *day-ahead market calculation engine* to produce a solution. For hour  $h \in \{1, \dots, 24\}$ , the *energy* balance shall be:

$$\begin{aligned} AFL_h + & \sum_{b \in B^{PRL} \cup B^{DL} \cup B^{HDR}} (1 + MglLoss_{h,b}) \cdot With_{h,b} \\ & + \sum_{m \in M} (1 + VMglLoss_{h,m}) \cdot VWith_{h,m} \\ & + \sum_{d \in DX} (1 + MglLoss_{h,d}) \cdot With_{h,d} \\ & - \sum_{i=1..N_{LdViol_h}} SLdViol_{h,i} \\ = & \sum_{b \in B^{NDG} \cup B^{DG}} (1 + MglLoss_{h,b}) \cdot Inj_{h,b} \\ & + \sum_{d \in DI} (1 + MglLoss_{h,d}) \cdot Inj_{h,d} \\ & - \sum_{i=1..N_{GenViol_h}} SGenViol_{h,i} + LossAdj_h \end{aligned}$$

## 8.7.2 Operating Reserve Requirements

- 8.7.2.1 *Operating reserve* shall be scheduled to meet system-wide requirements for synchronized *ten-minute operating reserve*, total *ten-minute operating reserve*, and *thirty-minute operating reserve*

while respecting all applicable regional minimum requirements and regional maximum restrictions for *operating reserve*.

- 8.7.2.2 Constraint violation penalty curves shall be used to impose a penalty cost for not meeting the *IESOs* system-wide *operating reserve* requirements, not meeting a regional minimum requirement, or not adhering to a regional maximum restriction. Full *operating reserve* requirements shall be scheduled unless the cost of doing so would be higher than the applicable penalty cost.

For each hour  $h \in \{1, \dots, 24\}$ :

$$\sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \right) + \sum_{i=1..N_{10SViol_h}} S10SViol_{h,i} \geq TOT10S_h;$$

$$\begin{aligned} & \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \right) \\ & + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \right) + \sum_{d \in DX} \left( \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \right) \\ & + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \right) + \sum_{d \in DI} \left( \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \right) \\ & + \sum_{i=1..N_{10RViol_h}} S10RViol_{h,i} \geq TOT10R_h; \end{aligned}$$

and

$$\begin{aligned}
& \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \right) \\
& + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \right) + \sum_{d \in DX} \left( \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \right) \\
& + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \right) + \sum_{d \in DI} \left( \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \right) \\
& + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,j} \right) + \sum_{d \in DX} \left( \sum_{j \in J_{h,d}^{30R}} S30RXL_{h,d,j} \right) \\
& + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \right) + \sum_{d \in DI} \left( \sum_{k \in K_{h,d}^{30R}} S30RIG_{h,d,k} \right) \\
& + \sum_{i=1..N_{30RViol_h}} S30RViol_{h,i} \geq TOT30R_h
\end{aligned}$$

8.7.2.3 The following constraints shall be applied for each hour  $h \in \{1, . . . 24\}$  and each region  $r \in ORREG$ :

$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \right) \\
& + \sum_{i=1..N_{REG10RViol_h}} SREG10RViol_{r,h,i} \geq REGMin10R_{h,r};
\end{aligned}$$



$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \right) \\
& + \sum_{d \in D_r^{REG} \cap D^X} \left( \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap D^I} \left( \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \right) \\
& - \sum_{i=1..N_{XREG10RViol_h}} SXREG10RViol_{r,h,i} \\
& \leq REGMax10R_{h,r};
\end{aligned}$$


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$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,j} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{h,d}^{30R}} S30RXL_{h,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{h,d}^{30R}} S30RIG_{h,d,k} \right) \\
& + \sum_{i=1..N_{REG30RViol_h}} SREG30RViol_{r,h,i} \geq REGMin30R_{h,r};
\end{aligned}$$

and

$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{h,d}^{30R}} S30RXL_{h,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{h,d}^{30R}} S30RIG_{h,d,k} \right) \\
& - \sum_{i=1..N_{XREG30RViol_h}} SXREG30RViol_{r,h,i} \\
& \leq REGMax30R_{h,r}.
\end{aligned}$$

### 8.7.3 IESO Internal Transmission Limits

8.7.3.1 A set of *energy* schedules shall be produced that do not violate any *security limits* in the pre-contingency state and the post-contingency state subject to the remainder of this section 8.7.3. The total amount of *energy* scheduled to be injected and withdrawn at each bus used by the *energy* balance constraint in section 8.7.1.6, shall be used to produce these schedules.

- 8.7.3.2 Pre-contingency,  $S\text{PreITL}Viol_{f,h,i}$  and post-contingency,  $SITLViol_{c,f,h,i}$  transmission limit violation variables shall allow the *day-ahead market calculation engine* to find a solution.
- 8.7.3.3 For all hours  $h \in \{1, \dots, 24\}$  and facilities  $f \in F_h$ , the linearized constraints for violated pre-contingency limits obtained from the *security* assesment function shall take the form:

$$\begin{aligned}
& \sum_{b \in B^{NDG} \cup B^{DG}} \text{PreConSF}_{h,f,b} \cdot \text{Inj}_{h,b} \\
& - \sum_{b \in B^{PRL} \cup B^{DL} \cup B^{HDR}} \text{PreConSF}_{h,f,b} \cdot \text{With}_{h,b} \\
& - \sum_{m \in M} V\text{PreConSF}_{h,f,m} \cdot V\text{With}_{h,m} \\
& + \sum_{d \in DI} \text{PreConSF}_{h,f,d} \cdot \text{Inj}_{h,d} \\
& - \sum_{d \in DX} \text{PreConSF}_{h,f,d} \cdot \text{With}_{h,d} \\
& - \sum_{i=1..N_{\text{PreITL}Viol_{f,h}}} S\text{PreITL}Viol_{f,h,i} \\
& \leq \text{AdjNormMaxFlow}_{h,f}
\end{aligned}$$

- 8.7.3.4 For all hours  $h \in \{1, \dots, 24\}$ , contingencies  $c \in C$ , and facilities  $f \in F_{h,c}$  the linearized constraints for violated post-contingency limits obtained from the *security* assesment function shall take the form:

$$\begin{aligned}
& \sum_{b \in B^{NDG} \cup B^{DG}} \text{SF}_{h,c,f,b} \cdot \text{Inj}_{h,b} - \sum_{b \in B^{PRL} \cup B^{DL} \cup B^{HDR}} \text{SF}_{h,c,f,b} \cdot \text{With}_{h,b} \\
& - \sum_{m \in M} V\text{SF}_{h,c,f,m} \cdot V\text{With}_{h,m} + \sum_{d \in DI} \text{SF}_{h,c,f,d} \\
& \cdot \text{Inj}_{h,d} - \sum_{d \in DX} \text{SF}_{h,c,f,d} \cdot \text{With}_{h,d} \\
& - \sum_{i=1..N_{\text{ITL}Viol_{c,f,h}}} \text{SITL}Viol_{c,f,h,i} \\
& \leq \text{AdjEmMaxFlow}_{h,c,f}
\end{aligned}$$

#### 8.7.4 Intertie Limits

- 8.7.4.1 A set of *energy* and *operating reserve* schedules shall be produced that respect any *security limits* associated with *interties* between

Ontario and *intertie zones*. For all hours  $h \in \{1, \dots, 24\}$  and all constraints  $z \in Z_{Sch}$ :

$$\begin{aligned}
 & \sum_{a \in A: EnCoeff_{a,z} \neq 0} \left[ \begin{aligned} & EnCoeff_{a,z} \left( \sum_{d \in DI_a} \sum_{k \in K_{h,d}^E} SIG_{h,d,k} - \sum_{d \in DX_a} \sum_{j \in J_{h,d}^E} SXL_{h,d,j} \right) \\ & + 0.5 \cdot (EnCoeff_{a,z} + 1) \left( \sum_{d \in DI_a} \left( \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} + \sum_{k \in K_{h,d}^{30R}} S30RIG_{h,d,k} \right) + \right. \\ & \left. \sum_{d \in DX_a} \left( \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} + \sum_{j \in J_{h,d}^{30R}} S30RXL_{h,d,j} \right) \right) \end{aligned} \right] \\
 & - \sum_{i=1..N_{PreXTLViol_{z,h}}} SPreXTLViol_{z,h,i} \leq MaxExtSch_{h,z}
 \end{aligned}$$

where for out-of-service *intertie zones*, the *intertie* limits shall be set to zero and all *boundary entity resources* shall receive a zero schedule for *energy* and *operating reserve*.

8.7.4.2 Changes in the hour-to-hour net *energy* schedule over all *intertie zones* shall not exceed the net interchange scheduling limit. The net import schedule shall be summed over all *intertie zones* for a given hour to obtain the net *interchange schedule* for the hour as follows:

8.7.4.2.1 It shall not exceed the net *interchange schedule* for the previous hour plus the net interchange scheduling limit;

8.7.4.2.2 It shall not be less than the net *interchange schedule* for the previous hour minus the net interchange scheduling limit; and

8.7.4.3 Violation variables may be used for both the up and down ramp limits to allow the *day-ahead market calculation engine* to find a solution and for all hours  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned}
& \sum_{d \in DI} \sum_{k \in K_{h-1,d}^E} SIG_{h-1,d,k} - \sum_{d \in DX} \sum_{j \in J_{h-1,d}^E} SXL_{h-1,d,j} - ExtDSC_h \\
& \quad - \sum_{i=1..N_{NIDViol_h}} SNIDViol_{h,i} \\
& \leq \sum_{d \in DI} \sum_{k \in K_{h,d}^E} SIG_{h,d,k} - \sum_{d \in DX} \sum_{j \in J_{h,d}^E} SXL_{h,d,j} \\
& \leq \sum_{d \in DI} \sum_{k \in K_{h-1,d}^E} SIG_{h-1,d,k} - \sum_{d \in DX} \sum_{j \in J_{h-1,d}^E} SXL_{h-1,d,j} \\
& \quad + ExtUSC_h + \sum_{i=1..N_{NIUViol_h}} SNIUViol_{h,i}
\end{aligned}$$

## 8.7.5 Penalty Price Variable Bounds

8.7.5.1 Penalty price variables shall be restricted to the ranges determined by the constraint violation penalty curves for the As-Offered Scheduling algorithm and for all hours  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned}
 0 \leq SLdViol_{h,i} \leq QLdViolSch_{h,i} & \quad \text{for all } i \in \{1, \dots, N_{LdViol_h}\}; \\
 0 \leq SGenViol_{h,i} \leq QGenViolSch_{h,i} & \quad \text{for all } i \in \{1, \dots, N_{GenViol_h}\}; \\
 0 \leq S10SViol_{h,i} \leq Q10SViolSch_{h,i} & \quad \text{for all } i \in \{1, \dots, N_{10SViol_h}\}; \\
 0 \leq S10RViol_{h,i} \leq Q10RViolSch_{h,i} & \quad \text{for all } i \in \{1, \dots, N_{10RViol_h}\}; \\
 0 \leq S30RViol_{h,i} \leq Q30RViolSch_{h,i} & \quad \text{for all } i \in \{1, \dots, N_{30RViol_h}\}; \\
 0 \leq SREG10RViol_{r,h,i} \leq QREG10RViolSch_{h,i} & \quad \text{for all } r \in ORREG, \\
 i \in \{1, \dots, N_{REG10RViol_h}\}; \\
 0 \leq SREG30RViol_{r,h,i} \leq QREG30RViolSch_{h,i} & \quad \text{for all } r \in ORREG, \\
 i \in \{1, \dots, N_{REG30RViol_h}\}; \\
 0 \leq SXREG10RViol_{r,h,i} \leq QXREG10RViolSch_{h,i} & \quad \text{for all } r \in ORREG, \\
 i \in \{1, \dots, N_{XREG10RViol_h}\}; \\
 0 \leq SXREG30RViol_{r,h,i} \leq QXREG30RViolSch_{h,i} & \quad \text{for all } r \in ORREG, \\
 i \in \{1, \dots, N_{XREG30RViol_h}\}; \\
 0 \leq SPreITLViol_{f,h,i} \leq QPreITLViolSch_{f,h,i} & \quad \text{for all } f \in F_h, \\
 i \in \{1, \dots, N_{PreITLViol_{f,h}}\};
 \end{aligned}$$

$$\begin{aligned}
0 \leq SITLViol_{c,f,h,i} &\leq QITLViolSch_{c,f,h,i} && \text{for all } c \in C, f \in F_{h,c}, \\
i \in \{1, \dots, N_{ITLViol_{c,f,h}}\}; \\
0 \leq SPreXTLViol_{z,h,i} &\leq QPreXTLViolSch_{z,h,i} && \text{for all } z \in Z_{Sch}, \\
i \in \{1, \dots, N_{PreXTLViol_{z,h}}\}; \\
0 \leq SNIUViol_{h,i} &\leq QNIUViolSch_{h,i} && \text{for all } i \in \{1, \dots, N_{NIUViol_h}\}; \\
0 \leq SNIDViol_{h,i} &\leq QNIDViolSch_{h,i} && \text{for all } i \in \{1, \dots, N_{NIDViol_h}\}; \\
0 \leq SMaxDelViol_{h,b,i} &\leq QMaxDelViolSch_{h,i} && \text{for all } b \in B^{ELR}, \\
i \in \{1, \dots, N_{MaxDelViol_h}\}; \\
0 \leq SMinDelViol_{h,b,i} &\leq QMinDelViolSch_{h,i} && \text{for all } b \in B^{HE}, \\
i \in \{1, \dots, N_{MinDelViol_h}\}; \\
0 \leq SMaxDelViol_{h,s,i} &\leq QMaxDelViolSch_{h,i} && \text{for all } s \in SHE, \\
i \in \{1, \dots, N_{SMaxDelViol_h}\}; \\
0 \leq SMinDelViol_{h,s,i} &\leq QMinDelViolSch_{h,i} && \text{for all } s \in SHE, \\
i \in \{1, \dots, N_{SMinDelViol_h}\}; \\
0 \leq SOGenLnkViol_{h,(b_1,b_2),i} &\leq QOGenLnkViol_{h,i} && \text{for all } (b_1, b_2) \in LNK, \\
i \in \{1, \dots, N_{OGenLnkViol_h}\}; \text{ and} \\
0 \leq SUGenLnkViol_{h,(b_1,b_2),i} &\leq QUGenLnkViol_{h,i} && \text{for all } (b_1, b_2) \in LNK, \\
i \in \{1, \dots, N_{UGenLnkViol_h}\}
\end{aligned}$$

## 8.8 Outputs

- 8.8.1 Outputs for the As-Offered Scheduling algorithm include *resource* schedules and commitments.



## 9 As-Offered Pricing

### 9.1 Purpose

- 9.1.1 The As-Offered Pricing algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, including *resource* schedules and commitments produced by the As-Offered Scheduling algorithm, to meet the *IESO's* average province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the next *dispatch day*.

### 9.2 Information, Sets, Indices and Parameters

- 9.2.1 Information sets, indices and parameters used by the As-Offered Pricing algorithm are described in sections 3 and 4. In addition, the following *resource* schedules and commitments from the As-Offered Scheduling algorithm in section 8 shall be used by the As-Offered Pricing algorithm:

- 9.2.1.1  $SDG_{h,b,k}^{AOS}$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide above  $MinQDG_b$  at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^E$ ;
- 9.2.1.2  $ODG_{h,b}^{AOS}$ , which designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  was scheduled at or above its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ ;
- 9.2.1.3  $S10SDG_{h,b,k}^{AOS}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10S}$ ;
- 9.2.1.4  $S10NDG_{h,b,k}^{AOS}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10N}$ ;
- 9.2.1.5  $S30RDG_{h,b,k}^{AOS}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to

provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{20R}$ ; and

- 9.2.1.6  $OHO_{h,b}^{AOS}$ , which designates whether the *dispatchable* hydroelectric *generation resource* at bus  $b \in B^{HE}$  has been scheduled at or above  $MinHO_{h,b}$  in hour  $h \in \{1, \dots, 24\}$ .

### 9.3 Variables and Objective Function

- 9.3.1 The *day-ahead market calculation engine* shall solve for the same variables as in the As-Offered Scheduling algorithm, section 8.3.1, with the following exceptions:

- 9.3.1.1  $IDG_{h,b}$  for bus  $b \in B^{DG}$  and hour  $h \in \{1, \dots, 24\}$  shall not appear in the formulation;
- 9.3.1.2  $ODG_{h,b}$  for bus  $b \in B^{DG}$  and hour  $h \in \{1, \dots, 24\}$  shall be fixed to a constant value;
- 9.3.1.3  $OHO_{h,b}$  for bus  $b \in B^{HE}$  and hour  $h \in \{1, \dots, 24\}$  shall be fixed to a constant value;
- 9.3.1.4  $IHE_{h,b,i}$  for bus  $b \in B^{HE}$ , hour  $h \in \{1, \dots, 24\}$  and *start indication value*  $i \in \{1, \dots, NStartMW_b\}$  shall not appear in the formulation;
- 9.3.1.5  $SOGenLnkViol_{h,(b_1,b_2),i}$  for  $(b_1, b_2) \in LNK$  such that  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ , hour  $h \in \{1, \dots, 24\}$  and  $i \in \{1, \dots, N_{OGenLnkViol_h}\}$  shall not appear in the formulation; and
- 9.3.1.6  $SUGenLnkViol_{h,(b_1,b_2),i}$  for  $(b_1, b_2) \in LNK$  such that  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ , hour  $h \in \{1, \dots, 24\}$  and  $i \in \{1, \dots, N_{UGenLnkViol_h}\}$  shall not appear in the formulation.

- 9.3.2 The objective function for the As-Offered Pricing algorithm shall maximize gains from trade by maximizing the following expression:

$$\sum_{h=1, \dots, 24} \left( ObjPRL_h + ObjDL_h - ObjHDR_h + ObjVB_h + ObjXL_h - ObjNDG_h \right. \\ \left. - ObjDG_h - ObjVO_h - ObjIG_h - TB_h - ViolCost_h \right)$$

where:

$$\begin{aligned}
ObjPRL_h &= \sum_{b \in B^{PRL}} \left( \sum_{j \in J_{h,b}^E} SPRL_{h,b,j} \cdot PPRL_{h,b,j} \right) \\
ObjDL_h &= \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^E} SDL_{h,b,j} \cdot PDL_{h,b,j} - \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \cdot P10SDL_{h,b,j} - \right. \\
&\quad \left. \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \cdot P10NDL_{h,b,j} - \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,j} \cdot P30RDL_{h,b,j} \right) \\
ObjHDR_h &= \sum_{b \in B^{HDR}} \left( \sum_{j \in J_{h,b}^E} SHDR_{h,b,j} \cdot PHDR_{h,b,j} \right) \\
ObjVB_h &= \sum_{v \in VB} \left( \sum_{j \in J_{h,v}^E} SVB_{h,v,j} \cdot PVB_{h,v,j} \right) \\
ObjXL_h &= \sum_{d \in DX} \left( \sum_{j \in J_{h,d}^E} SXL_{h,d,j} \cdot PXL_{h,d,j} - \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \cdot P10NXL_{h,d,j} \right. \\
&\quad \left. - \sum_{j \in J_{h,d}^{30R}} S30RXL_{h,d,j} \cdot P30RXL_{h,d,j} \right) \\
ObjNDG_h &= \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{h,b}^E} SNDG_{h,b,k} \cdot PNDG_{h,b,k} \right) \\
ObjDG_h &= \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \cdot PDG_{h,b,k} + \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \cdot P10SDG_{h,b,k} + \right. \\
&\quad \left. \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \cdot P10NDG_{h,b,k} + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \cdot P30RDG_{h,b,k} \right) \\
ObjVO_h &= \sum_{v \in VO} \left( \sum_{k \in K_{h,v}^E} SVO_{h,v,k} \cdot PVO_{h,v,k} \right)
\end{aligned}$$

$$ObjIG_h = \sum_{d \in DI} \left( \sum_{k \in K_{h,d}^E} SIG_{h,d,k} \cdot PIG_{h,d,k} + \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \cdot P10NIG_{h,d,k} \right. \\ \left. + \sum_{k \in K_{h,d}^{30R}} S30IG_{h,d,k} \cdot P30RIG_{h,d,k} \right)$$

9.3.2.1 The tie-breaking term ( $TB_h$ ) shall be the same term described in section 8.3.2.1.

9.3.2.2  $ViolCost_h$  shall be calculated as follows:

$$ViolCost_h = \sum_{i=1..N_{LdViol_h}} SLdViol_{h,i} \cdot PLdViolPrc_{h,i} \\ - \sum_{i=1..N_{GenViol_h}} SGenViol_{h,i} \cdot PGenViolPrc_{h,i} \\ + \sum_{i=1..N_{10SViol_h}} S10SViol_{h,i} \cdot P10SViolPrc_{h,i} \\ + \sum_{i=1..N_{10RViol_h}} S10RViol_{h,i} \cdot P10RViolPrc_{h,i} \\ + \sum_{i=1..N_{30RViol_h}} S30RViol_{h,i} \cdot P30RViolPrc_{h,i} \\ + \sum_{r \in ORREG} \left( \sum_{i=1..N_{REG10RViol_h}} SREG10RViol_{r,h,i} \right. \\ \left. \cdot PREG10RViolPrc_{h,i} \right)$$

$$\begin{aligned}
& + \sum_{r \in ORREG} \left( \sum_{i=1..N_{REG30RViol_h}} SREG30RViol_{r,h,i} \right. \\
& \quad \cdot PREG30RViolPrC_{h,i} \Bigg) \\
& + \sum_{r \in ORREG} \left( \sum_{i=1..N_{XREG10RViol_h}} SXREG10RViol_{r,h,i} \right. \\
& \quad \cdot PXREG10RViolPrC_{h,i} \Bigg) \\
& + \sum_{r \in ORREG} \left( \sum_{i=1..N_{XREG30RViol_h}} SXREG30RViol_{r,h,i} \right. \\
& \quad \cdot PXREG30RViolPrC_{h,i} \Bigg) \\
& + \sum_{f \in F_h} \left( \sum_{i=1..N_{PreITLViol_{f,h}}} SPreITLViol_{f,h,i} \right. \\
& \quad \cdot PPreITLViolPrC_{f,h,i} \Bigg) \\
& + \sum_{c \in C} \sum_{f \in F_{h,c}} \left( \sum_{i=1..N_{ITLViol_{c,f,h}}} SITLViol_{c,f,h,i} \right. \\
& \quad \cdot PITLViolPrC_{c,f,h,i} \Bigg) \\
& + \sum_{z \in Z_{Sch}} \left( \sum_{i=1..N_{PreXTLViol_{z,h}}} SPreXTLViol_{z,h,i} \right. \\
& \quad \cdot PPreXTLViolPrC_{z,h,i} \Bigg)
\end{aligned}$$

$$\begin{aligned}
& + \sum_{i=1..N_{NIUViol_h}} SNIUViol_{h,i} \cdot PNIUViolPrc_{h,i} \\
& + \sum_{i=1..N_{NIDViol_h}} SNIDViol_{h,i} \cdot PNIDViolPrc_{h,i} \\
& + \sum_{b \in B^{ELR}} \left( \sum_{i=1..N_{MaxDelViol_h}} SMaxDelViol_{h,b,i} \cdot PMaxDelViolPrc_{h,i} \right) \\
& + \sum_{b \in B^{HE}} \left( \sum_{i=1..N_{MinDelViol_h}} SMinDelViol_{h,b,i} \cdot PMinDelViolPrc_{h,i} \right) \\
& + \sum_{s \in SHE} \left( \sum_{i=1..N_{SMaxDelViol_h}} SSMaxDelViol_{h,s,i} \cdot PSMaxDelViolPrc_{h,i} \right) \\
& + \sum_{s \in SHE} \left( \sum_{i=1..N_{SMinDelViol_h}} SSMinDelViol_{h,s,i} \cdot PSMinDelViolPrc_{h,i} \right)
\end{aligned}$$

## 9.4 Constraints

9.4.1 The constraints described in sections 9.5, 9.6, 9.7 and 9.8 apply to the optimization function in the As-Offered Pricing algorithm.

## 9.5 Dispatch Data Constraints Applying to Individual Hours

9.5.1 Scheduling Variable Bounds

9.5.1.1 No schedule shall be negative, nor shall any schedule exceed the quantity respectively *offered* for *energy* and *operating reserve*. For all hours  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned}
0 \leq SPRL_{h,b,j} &\leq QPRL_{h,b,j} && \text{for all } b \in B^{PRL}, j \in J_{h,b}^E; \\
0 \leq SDL_{h,b,j} &\leq QDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^E; \\
0 \leq S10SDL_{h,b,j} &\leq Q10SDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^{10S}; \\
0 \leq S10NDL_{h,b,j} &\leq Q10NDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^{10N}; \\
0 \leq S30RDL_{h,b,j} &\leq Q30RDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^{30R}; \\
0 \leq SHDR_{h,b,j} &\leq QHDR_{h,b,j} && \text{for all } b \in B^{HDR}, j \in J_{h,b}^E; \\
0 \leq SVB_{h,v,j} &\leq QVB_{h,v,j} && \text{for all } v \in VB, j \in J_{h,v}^E; \\
0 \leq SXL_{h,d,j} &\leq QXL_{h,d,j} && \text{for all } d \in DX, j \in J_{h,d}^E; \\
0 \leq S10NXL_{h,d,j} &\leq Q10NXL_{h,d,j} && \text{for all } d \in DX, j \in J_{h,d}^{10N}; \\
0 \leq S30RXL_{h,d,j} &\leq Q30RXL_{h,d,j} && \text{for all } d \in DX, j \in J_{h,d}^{30R}; \\
0 \leq SNDG_{h,b,k} &\leq QNDG_{h,b,k} && \text{for all } b \in B^{NDG}, k \in K_{h,b}^E; \\
0 \leq SVO_{h,v,k} &\leq QVO_{h,v,k} && \text{for all } v \in VO, k \in K_{h,v}^E; \\
0 \leq SIG_{h,d,k} &\leq QIG_{h,d,k} && \text{for all } d \in DI, k \in K_{h,d}^E; \\
0 \leq S10NIG_{h,d,k} &\leq Q10NIG_{h,d,k} && \text{for all } d \in DI, k \in K_{h,d}^{10N}; \text{ and} \\
0 \leq S30RIG_{h,d,k} &\leq Q30RIG_{h,d,k} && \text{for all } d \in DI, k \in K_{h,d}^{30R}
\end{aligned}$$

9.5.1.2 A *dispatchable generation resource* can be scheduled for *energy* and *operating reserve* only if its commitment status variable is equal to 1. For all hours  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned}
0 \leq SDG_{h,b,k} &\leq ODG_{h,b} \cdot QDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^E; \\
0 \leq S10SDG_{h,b,k} &\leq ODG_{h,b} \cdot Q10SDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{10S}; \\
0 \leq S10NDG_{h,b,k} &\leq ODG_{h,b} \cdot Q10NDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{10N}; \\
&\text{and} \\
0 \leq S30RDG_{h,b,k} &\leq ODG_{h,b} \cdot Q30RDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{30R}
\end{aligned}$$

where:

$ODG_{h,b}$  is a fixed constant in the above constraints as per section 9.8.1.

## 9.5.2 Resource Minimums and Maximums

9.5.2.1 The constraints in section 8.5.2 shall apply in the As-Offered Pricing algorithm.

## 9.5.3 Off-Market Transactions

9.5.3.1 The constraints in section 8.5.3.1 and 8.5.3.2 shall apply in the As-Offered Pricing algorithm.

9.5.3.2 In the case of *emergency energy* transactions, subject to section 9.5.3.3, the constraints in sections 8.5.3.3 and 8.5.3.4 shall apply in As-Offered Pricing algorithm.

9.5.3.3 For all hours  $h \in \{1, \dots, 24\}$  and all *intertie zone* buses scheduled to import *emergency energy* that does not support an export  $d \in DI_h^{EMNS}$ :

$$\sum_{k \in K_{h,d}^E} SIG_{h,d,k} = 0.$$

## 9.5.4 Operating Reserve Requirements

9.5.4.1 The constraints in section 8.5.4 shall apply in the As-Offered Pricing algorithm.

## 9.5.5 Pseudo-Units

9.5.5.1 The constraints in section 8.5.5 shall apply in the As-Offered Pricing algorithm.

## 9.5.6 Dispatchable Hydroelectric Generation Resources

9.5.6.1 The constraints in section 8.5.6 shall apply in the As-Offered Pricing algorithm, with the following exceptions:

9.5.6.1.1 *offer* laminations for *energy* corresponding to the *hourly must-run* amount shall be ineligible to set prices;

9.5.6.1.2 *minimum hourly output* constraints shall be replaced by the constraints in section 9.8; and



9.5.6.1.3 a *dispatchable* hydroelectric *generation resource's* schedule shall respect its *forbidden regions* and may only set prices within the operating range determined by the adjacent *forbidden regions* between which the *resource* was scheduled.

## 9.5.7 Linked Wheeling Through Transactions

9.5.7.1 The constraints in section 8.5.7 shall apply in the As-Offered Pricing algorithm.

## 9.6 Dispatch Data Inter-Hour/Multi-Hour Constraints

### 9.6.1 Energy Ramping

9.6.1.1 The constraints in section 8.6.1 shall apply in the As-Offered Pricing algorithm.

### 9.6.2 Operating Reserve Ramping

9.6.2.1 The constraints in section 8.6.2 shall apply in the As-Offered Pricing algorithm.

### 9.6.3 Energy Limited Resources

9.6.3.1 The constraints in section 8.6.4 shall apply to *energy limited resources*. If the *maximum daily energy limit* is binding, then the constraints in section 9.8 shall apply.

### 9.6.4 Dispatchable Hydroelectric Generation Resources

9.6.4.1 A *dispatchable* hydroelectric *generation resource* shall be scheduled for *energy* to at least its *minimum daily energy limit*. Violation variables for scheduling a *resource* below its *minimum daily energy limit* may be used to allow the *day-ahead market calculation engine* to find a solution. For all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$ :

$$\sum_{h=1..24} \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} + \sum_{i=1..N_{MinDelViol_h}} SMinDelViol_{h,b,i} \right) \geq MinDEL_b$$

- 9.6.4.2 The constraints in section 9.8.3.3 shall apply to a *dispatchable* hydroelectric *generation resource* with a binding *minimum daily energy limit* in the As-Offered Scheduling algorithm in section 8.
- 9.6.4.3 The schedules for multiple *dispatchable* hydroelectric *generation resources* with a registered *forebay* shall respect shared *maximum daily energy limits*. Violation variables for scheduling *resources* above the *maximum daily energy limit* may be used to allow the *day-ahead market calculation engine* to find a solution. For all sets  $s \in SHE$  and all hours  $H \in \{1, \dots, 24\}$ :

$$\begin{aligned}
& \sum_{h=1..H} \left( \sum_{b \in B_s^{HE}} \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \right) \right) \\
& + \sum_{b \in B_s^{HE}} \left( 10ORConv \left( \sum_{k \in K_{H,b}^{10S}} S10SDG_{H,b,k} \right) \right. \\
& \left. + \sum_{k \in K_{H,b}^{10N}} S10NDG_{H,b,k} \right) \\
& + 30ORConv \left( \sum_{k \in K_{H,b}^{30R}} S30RDG_{H,b,k} \right) \\
& - \sum_{i=1..N_{SMaxDelViol_H}} SSMaxDelViol_{H,s,i} \\
& \leq MaxSDEL_s
\end{aligned}$$

where the factors  $10ORConv$  and  $30ORConv$  shall be applied to scheduled *ten-minute operating reserve* and *thirty-minute operating reserve* for *energy limited resources* to convert MW into MWh.

- 9.6.4.4 The schedules for multiple *dispatchable* hydroelectric *generation resources* with a registered *forebay* shall not violate shared *minimum daily energy limits*. Violation variables for scheduling *resources* below the *minimum daily energy limit* may be used to allow the *day-ahead market calculation engine* to find a solution. For all sets  $s \in SHE$ :

$$\sum_{h=1..24} \left( \sum_{b \in B_s^{HE}} \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \right) + \sum_{i=1..N_{SMinDelViol_h}} SMinDelViol_{h,s,i} \right) \geq MinSDEL_s$$

## 9.7 Constraints for Reliability Requirements

### 9.7.1 Energy Balance

9.7.1.1 The constraint in section 8.7.1 shall apply in the As-Offered Pricing algorithm, except the marginal loss factors used in the *energy* balance constraint in the As-Offered Pricing algorithm shall be fixed to the marginal loss factors used in the last optimization function iteration of the As-Offered Scheduling algorithm.

### 9.7.2 Operating Reserve Requirements

9.7.2.1 The constraints in section 8.7.2 shall apply in the As-Offered Pricing algorithm.

### 9.7.3 IESO Internal Transmission Limits

9.7.3.1 The constraints in section 8.7.3 shall apply in the As-Offered Pricing algorithm, except the sensitivities and limits considered shall be those provided by the most recent *security* assessment function iteration of the As-Offered Pricing algorithm.

### 9.7.4 Intertie Limits

9.7.4.1 The constraints in section 8.7.4 shall apply in the As-Offered Pricing algorithm.

### 9.7.5 Penalty Price Variable Bounds

9.7.5.1 The following constraints shall restrict the penalty price variables to the ranges determined by the constraint violation penalty curves for the pricing algorithm. For all  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned}
0 \leq SLdViol_{h,i} &\leq QLdViolPrc_{h,i} && \text{for all } i \in \{1, \dots, N_{LdViol_h}\}; \\
0 \leq SGenViol_{h,i} &\leq QGenViolPrc_{h,i} && \text{for all } i \in \{1, \dots, N_{GenViol_h}\}; \\
0 \leq S10SViol_{h,i} &\leq Q10SViolPrc_{h,i} && \text{for all } i \in \{1, \dots, N_{10SViol_h}\}; \\
0 \leq S10RViol_{h,i} &\leq Q10RViolPrc_{h,i} && \text{for all } i \in \{1, \dots, N_{10RViol_h}\}; \\
0 \leq S30RViol_{h,i} &\leq Q30RViolPrc_{h,i} && \text{for all } i \in \{1, \dots, N_{30RViol_h}\}; \\
0 \leq SREG10RViol_{r,h,i} &\leq QREG10RViolPrc_{h,i} && \text{for all } r \in ORREG, i \in \{1, \dots, \\
&N_{REG10RViol_h}\}; \\
0 \leq SREG30RViol_{r,h,i} &\leq QREG30RViolPrc_{h,i} && \text{for all } r \in ORREG, i \in \{1, \dots, \\
&N_{REG30RViol_h}\}; \\
0 \leq SXREG10RViol_{r,h,i} &\leq QXREG10RViolPrc_{h,i} && \text{for all } r \in ORREG, i \in \{1, \dots, \\
&N_{XREG10RViol_h}\}; \\
0 \leq SXREG30RViol_{r,h,i} &\leq QXREG30RViolPrc_{h,i} && \text{for all } r \in ORREG, i \in \{1, \dots, \\
&N_{XREG30RViol_h}\}; \\
0 \leq SPreITLViol_{f,h,i} &\leq QPreITLViolPrc_{f,h,i} && \text{for all } f \in F_h, i \in \{1, \dots, \\
&N_{PreITLViol_{f,h}}\}; \\
0 \leq SITLViol_{c,f,h,i} &\leq QITLViolPrc_{c,f,h,i} && \text{for all } c \in C, f \in F_{h,c}, i \in \\
&\{1, \dots, N_{ITLViol_{c,f,h}}\}; \\
0 \leq SPreXTLViol_{z,h,i} &\leq QPreXTLViolPrc_{z,h,i} && \text{for all } z \in Z_{Sch}, i \in \{1, \dots, \\
&N_{PreXTLViol_{z,h}}\}; \\
0 \leq SNIUViol_{h,i} &\leq QNIUViolPrc_{h,i} && \text{for all } i \in \{1, \dots, N_{NIUViol_h}\}; \\
0 \leq SNIDViol_{h,i} &\leq QNIDViolPrc_{h,i} && \text{for all } i \in \{1, \dots, N_{NIDViol_h}\}; \\
0 \leq SMaxDelViol_{h,b,i} &\leq QMaxDelViolPrc_{h,i} && \text{for all } b \in B^{ELR}, i \in \{1, \dots, \\
&N_{MaxDelViol_h}\}; \\
0 \leq SMinDelViol_{h,b,i} &\leq QMinDelViolPrc_{h,i} && \text{for all } b \in B^{HE}, i \in \{1, \dots, \\
&N_{MinDelViol_h}\}; \\
0 \leq SSMaXDelViol_{h,s,i} &\leq QSMaXDelViolPrc_{h,i} && \text{for all } s \in SHE, i \in \{1, \dots, \\
&N_{SMaXDelViol_h}\}; \text{ and} \\
0 \leq SSMinDelViol_{h,s,i} &\leq QSSMinDelViolPrc_{h,i} && \text{for all } s \in SHE, i \in \{1, \dots, \\
&N_{SSMinDelViol_h}\}.
\end{aligned}$$

## 9.8 Constraints to Ensure the Price Setting Eligibility Reflect Offer/Bid Laminations

### 9.8.1 Commitment Status Variables

9.8.1.1 Commitment decisions shall be fixed to the commitment statuses of *resources* calculated by the As-Offered Scheduling algorithm in section 8. For all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

$$ODG_{h,b} = ODG_{h,b}^{AOS}$$

### 9.8.2 Energy Limited Resources

9.8.2.1 For an *energy limited resource* with a *maximum daily energy limit* that was binding in the As-Offered Scheduling algorithm in section 8, the schedules calculated in the As-Offered Scheduling algorithm shall determine the price-setting eligibility of the *resource's energy* and *operating reserve offer* laminations. In each hour, *energy* or *operating reserve* laminations up to the total amount of *energy* and *operating reserve* scheduled in the As-Offered Scheduling algorithm shall be eligible to set prices. For bus  $b \in B^{ELR}$ , if there exists an hour  $H \in \{1, \dots, 24\}$  such that:

$$\begin{aligned} \sum_{h=1..H} \left( ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} \right) \\ + 10ORConv \left( \sum_{k \in K_{H,b}^{10S}} S10SDG_{H,b,k}^{AOS} \right. \\ \left. + \sum_{k \in K_{H,b}^{10N}} S10NDG_{H,b,k}^{AOS} \right) \\ + 30ORConv \left( \sum_{k \in K_{H,b}^{30R}} S30RDG_{H,b,k}^{AOS} \right) = MaxDEL_b, \end{aligned}$$

then the *maximum daily energy limit* constraint shall be considered binding in the As-Offered Scheduling algorithm. In such circumstances, the following constraints must hold for bus  $b \in B^{ELR}$  for all hours  $h \in \{1, \dots, 24\}$ :

$$\sum_{k \in K_{h,b}^E} SDG_{h,b,k} \leq \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} + \epsilon$$

$$\sum_{k \in K_{h,b}^E} SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \leq MaxDEL_b - \sum_{\tau=1}^{h-1} \sum_{k \in K_{h,b}^E} SDG_{\tau,b,k}^{AOS}$$

where  $\epsilon$  is a small positive constant.

### 9.8.3 Dispatchable Hydroelectric Generation Resources

9.8.3.1 If a *dispatchable hydroelectric generation resource* is scheduled to provide *energy* at or above its *minimum hourly output* in the As-Offered Scheduling algorithm in section 8, such *resource* shall also be scheduled at or above its *minimum hourly output* in the As-Offered Pricing algorithm. The *energy offer* laminations corresponding to the *minimum hourly output* amount shall be ineligible to set prices. If a *dispatchable hydroelectric generation resource* with a *minimum hourly output* amount receives a zero schedule in the As-Offered Scheduling algorithm, the *resource* shall also receive a zero schedule in the As-Offered Pricing algorithm and shall be ineligible to set prices in the *energy market*. For all hours  $h \in \{1, \dots, 24\}$  and *dispatchable hydroelectric generation resource* buses  $b \in B^{HE}$ :

$$ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \geq MinHO_{h,b} \cdot OHO_{h,b}^{AOS}$$

and for all  $k \in K_{h,b}^E$ :

$$0 \leq SDG_{h,b,k} \leq OHO_{h,b}^{AOS} \cdot QDG_{h,b,k}$$

9.8.3.2 For a *dispatchable hydroelectric generation resource* with a limited number of starts, such *resource* shall be scheduled such that it is limited to set prices within an operating range consistent with the number of starts utilized by the *resource's* schedule determined by the As-Offered Scheduling algorithm in section 8. The *resource's* schedule shall be between the same *start indication values* as determined in the As-Offered Scheduling algorithm. For all hydroelectric buses  $b \in B^{HE}$  and all hours  $h \in \{1, \dots, 24\}$ :

If  $0 \leq ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} < StartMW_{b,1}$ ,

then

$$0 \leq ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \leq StartMW_{b,1} - 0.1$$

If  $StartMW_{b,i} \leq ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} < StartMW_{b,i+1}$  for  $i \in \{1, \dots, (NStartMW_b - 1)\}$ ,

then

$$StartMW_{b,i} \leq ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \leq StartMW_{b,i+1} - 0.1$$

If  $ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} \geq StartMW_{b,NStartMW_b}$ ,

then

$$ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \geq StartMW_{b,NStartMW_b}$$

- 9.8.3.3 For a *dispatchable* hydroelectric *generation resource* with a *minimum daily energy limit* that was binding in the As-Offered Scheduling algorithm in section 8, the *energy* schedules calculated in the As-Offered Scheduling algorithm shall be ineligible to set prices. For all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$  such that  $MinDEL_b > 0$  and

$$\sum_{h=1..24} \left( ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} \right) \leq MinDEL_b$$

the following constraints shall apply for all hours  $h \in \{1, \dots, 24\}$  and offer laminations  $k \in K_{h,b}^E$ :

$$SDG_{h,b,k} \geq SDG_{h,b,k}^{AOS}$$

- 9.8.3.4 For a *dispatchable* hydroelectric *generation resource* with a shared *minimum daily energy limit* that was binding in the As-Offered Scheduling algorithm in section 8, the *energy* schedules calculated for all *resources* in the set  $s \in SHE$  in the As-Offered Scheduling

algorithm shall be ineligible to set prices. Thus, for all sets  $s \in SHE$  such that:

$$\sum_{h=1..24} \left( \sum_{b \in B_s^{HE}} \left( ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} \right) \right) \leq MinSDEL_s$$

the following constraints shall apply for all hours  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned} \sum_{b \in B_s^{HE}} \left( ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \right) \\ \geq \sum_{b \in B_s^{HE}} \left( ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} \right) \end{aligned}$$

- 9.8.3.5 For a *dispatchable* hydroelectric *generation resource* with a binding *maximum daily energy limit* in the As-Offered Scheduling algorithm in section 8, the schedules calculated in the As-Offered Scheduling algorithm shall determine the price-setting eligibility of the *resource's energy* and *operating reserve offer* laminations as described in section 9.8.2.
- 9.8.3.6 For a *dispatchable* hydroelectric *generation resource* with with a shared *maximum daily energy limit* that was binding in the As-Offered Scheduling algorithm in section 8, the schedules calculated in the As-Offered Scheduling algorithm shall determine the price-setting eligibility of the *resource's offer* laminations for *energy* and *operating reserve*. In each hour, the sum of *energy* schedules calculated in As-Offered Scheduling algorithm for all *resources* in each set  $s \in SHE$



will be eligible to set prices. For each set  $s \in SHE$ , if there exists  $H \in \{1, \dots, 24\}$  such that:

$$\begin{aligned}
& \sum_{h=1..H} \left( \sum_{b \in B_s^{HE}} \left( ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} \right) \right) \\
& + \sum_{b \in B_s^{HE}} \left( 10ORConv \left( \sum_{k \in K_{H,b}^{10S}} S10SDG_{H,b,k}^{AOS} \right. \right. \\
& \left. \left. + \sum_{k \in K_{H,b}^{10N}} S10NDG_{H,b,k}^{AOS} \right) \right) \\
& + 30ORConv \left( \sum_{k \in K_{H,b}^{30R}} S30RDG_{H,b,k}^{AOS} \right) \\
& = MaxSDEL_s
\end{aligned}$$

then the *maximum daily energy limit* constraint shall be considered binding in the As-Offered Scheduling algorithm in section 8. In such circumstances, the following constraints shall apply for hours  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned}
& \sum_{b \in B_s^{HE}} \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \leq \sum_{b \in B_s^{HE}} \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} + \epsilon, \\
& \sum_{b \in B_s^{HE}} \left( \sum_{k \in K_{h,b}^E} SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \right. \\
& \left. + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \right) \\
& \leq MaxSDEL_s - \sum_{b \in B_s^{HE}} \sum_{\tau=2}^{h-1} \sum_{k \in K_{h,b}^E} SDG_{\tau,b,k}^{AOS}.
\end{aligned}$$

where  $\epsilon$  is a small positive constant.

- 9.8.3.7 For a *dispatchable* hydroelectric *generation resource* for which a *MWh ratio* was respected in the As-Offered Scheduling algorithm in section 8, such *resource* shall be scheduled between its As-Offered Scheduling algorithm schedule plus or minus a tolerance  $\Delta$  specified by the *IESO*. The *resource* schedule shall continue to be limited by its *offer* quantity bounds, in section 9.5.1, and any applicable *resource* minimum or maximum constraints, in section 9.5.2. For all hours  $h \in \{1, \dots, 24\}$  and *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$  such  $b \in \{b_1, b_2\}$  where  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$  for some  $(b_1, b_2) \in LNK$  with  $h + Lag_{b_1, b_2} \leq 24$ :

$$\begin{aligned}
 & \max \left( 0, ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} - \Delta, AdjMinDG_{h,b} \right) \\
 & \leq ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \\
 & \leq \min \left( MinQDG_b + \sum_{k \in K_{h,b}^E} QDG_{h,b,k}, ODG_{h,b}^{AOS} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k}^{AOS} + \Delta, AdjMaxDG_{h,b} \right)
 \end{aligned}$$

## 9.9 Outputs

- 9.9.1 Outputs for the As-Offered Pricing algorithm include the following:
- 9.9.1.1 shadow prices;
  - 9.9.1.2 *locational marginal prices* and their components; and
  - 9.9.1.3 sensitivity factors.

# 10 Constrained Area Conditions Test

## 10.1 Purpose

- 10.1.1 The Constrained Area Conditions Test shall:
- 10.1.1.1 identify when and where competition is restricted; and
  - 10.1.1.2 determine which *resources* shall have their *financial dispatch data parameters* be subject to the Conduct Test in section 11 and the

thresholds above the *reference levels* that shall be used in the Conduct Test.

## 10.2 Information, Sets, Indices and Parameters

- 10.2.1 The sets and parameters associated with *narrow constrained areas* and *dynamic constrained areas* shall be identified in accordance with Appendix 7.8 and used by the Constrained Area Conditions Test.
- 10.2.2 Information, sets, indices and parameters for the Constrained Area Conditions Test are described in sections 3 and 4. In addition, the following prices produced by the As-Offered Pricing algorithm shall be used by the Constrained Area Conditions Test:
- 10.2.2.1  $LMP_{h,b}^{AOP}$ , which designates the *locational marginal price* for bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.2.2.2  $PCong_{h,b}^{AOP}$ , which designates the congestion component of the *locational marginal price* for bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.2.2.3  $ExtLMP_{h,d}^{AOP}$ , which designates the *locational marginal price* for *intertie zone* bus  $d \in D$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.2.2.4  $PExtCong_{h,d}^{AOP}$ , which designates the *intertie* congestion component of the *locational marginal price* for *intertie zone* bus  $d \in D$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.2.2.5  $PIntCong_{h,d}^{AOP}$ , which designates the internal congestion component of the *locational marginal price* for *intertie zone* bus  $d \in D$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.2.2.6  $IntLMP_{h,d}^{AOP}$ , which designates the *intertie border price* for *intertie zone* bus  $d \in D$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.2.2.7  $SPNormT_{h,f}^{AOP}$ , which designates the shadow price for the pre-contingency transmission constraint for *facility*  $f \in F$  in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.2.2.8  $SPEmT_{h,c,f}^{AOP}$ , which designates the shadow price for the post-contingency transmission constraint for *facility*  $f \in F$  in contingency  $c \in C$  in hour  $h$ ;

- 10.2.2.9  $SPNIUExtBwdT_h^{AOP}$ , which designates the shadow price for the net interchange scheduling limit constraint limiting increases in net imports between hour  $(h - 1)$  and hour  $h$ ;
- 10.2.2.10  $L30RP_{h,b}^{AOP}$ , which designates the *locational marginal price* for *thirty-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ ;
- 10.2.2.11  $L10NP_{h,b}^{AOP}$ , which designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ ; and
- 10.2.2.12  $L10SP_{h,b}^{AOP}$ , which designates the *locational marginal price* for synchronized *ten-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ .

## 10.3 Variables

- 10.3.1 The *day-ahead market calculation engine* shall use the constrained area conditions in sections 10.4 and 10.5 to identify the *resources* that are part of the following data sets:
  - 10.3.1.1  $BCond_h^{NCA}$ , which designates the *resources* in a *narrow constrained area* that must be checked for local market power for *energy* in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.3.1.2  $BCond_h^{DCA}$ , which designates the *resources* in a *dynamic constrained area* that must be checked for local market power for *energy* in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.3.1.3  $BCond_h^{BCA}$ , which designates the *resources* in a broad constrained area that must be checked for local market power for *energy* in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.3.1.4  $BCond_h^{GMP}$ , which designates the *resources* that must be checked for global market power for *energy* in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.3.1.5  $BCond_h^{10S}$ , which designates the *resources* that must be checked for local market power for synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ ;
  - 10.3.1.6  $BCond_h^{10N}$ , which designates the *resources* that must be checked for local market power for non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ ;

- 10.3.1.7  $BCond_h^{30R}$ , which designates the *resources* that must be checked for local market power for *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ ;
- 10.3.1.8  $BCond_h^{GMP10S}$ , which designates the *resources* that must be checked for global market power for synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ ;
- 10.3.1.9  $BCond_h^{GMP10N}$ , which designates the *resources* that must be checked for global market power for non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ ; and
- 10.3.1.10  $BCond_h^{GMP30R}$ , which designates the *resources* that must be checked for global market power for *thirty minute operating reserve* in hour  $h \in \{1, \dots, 24\}$ .

## 10.4 Constrained Area Conditions Test for Local Market Power (Energy)

### 10.4.1 Constrained Area Conditions Test for Narrow Constrained Areas and Dynamic Constrained Areas

- 10.4.1.1 If at least one transmission constraint for a *narrow constrained area* or *dynamic constrained area* is binding in the As-Offered Pricing algorithm, then all *resources* identified within the *narrow constrained area* or *dynamic constrained area* shall undergo the applicable Conduct Test in section 11 and:

10.4.1.1.1 For each  $n \in NCA$  and hour  $h \in \{1, \dots, 24\}$ : For each transmission *facility* that transmits flow into  $n$ ,  $f \in F_n^{NCA}$ , check if  $SPNormT_{h,f}^{AOP} \neq 0$  or  $SPEmT_{h,c,f}^{AOP} \neq 0$  for the inbound flow limit, the *day-ahead market calculation engine* will place  $n$  in the set  $NCA_h'$  and assign the *resources* in  $n$  to the set  $BCond_h^{NCA}$ ; and

10.4.1.1.2 For each  $d \in DCA$  and hour  $h \in \{1, \dots, 24\}$ : For each transmission *facility* that transmits flow into  $d$ ,  $f \in F_d^{DCA}$ , check if  $SPNormT_{h,f}^{AOP} \neq 0$  or  $SPEmT_{h,c,f}^{AOP} \neq 0$  for the inbound flow limit, the *day-ahead market calculation engine* will place  $d$  in the set  $DCA_h'$  and assign the *resources* in  $d$  to the set  $BCond_h^{DCA}$ .

10.4.1.2 Each *narrow constrained area* and *dynamic constrained area* that meets the criteria in section 10.4.1.1 shall be assigned to one of the following subsets, as appropriate:

10.4.1.2.1  $NCA_h$  'designates the *narrow constrained areas* that qualify for market power mitigation for *energy* in hour  $h \in \{1, \dots, 24\}$ ; and

10.4.1.2.2  $DCA_h$  'designates the *dynamic constrained areas* that qualify for market power mitigation for *energy* in hour  $h \in \{1, \dots, 24\}$ .

#### 10.4.2 Constrained Area Conditions Test for Broad Constrained Areas

10.4.2.1 If the congestion component of the *locational marginal price* for a *resource* is greater than  $BCACondThresh$ , and the *resource* is not part of a *narrow constrained area* or *dynamic constrained area* that has a binding transmission constraint, then the *resource* shall be tested for Conduct Test under the broad constrained area thresholds. For each hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DG}$  such that  $b \notin BCond_h^{NCA} \cup BCond_h^{DCA}$ , if  $PCong_{h,b}^{AOP} > BCACondThresh$ , the day-ahead market calculation engine will place *resource*  $b$  in the set  $BCond_h^{BCA}$ .

### 10.5 Constrained Area Conditions Test for Global Market Power (Energy)

10.5.1 The *day-ahead market calculation engine* shall test *resources* that can meet incremental load within Ontario for global market power, subject to 10.5.2, if:

10.5.1.1 the *intertie border prices* at the *global market power reference intertie zones* are greater than the specified threshold value, indicated in hour  $h \in \{1, \dots, 24\}$  by  $IntLMP_{h,d}^{AOP} > IBPThresh$  for *bids* and *offers*,  $d \in D^{GMPRef}$ , corresponding to the *boundary entity resource* bus for the *global market power reference intertie zone*; and

10.5.1.2 at least one of the following conditions is met:

10.5.1.2.1 import congestion, represented by a negative *intertie* congestion component, is present on all of the *global market power reference interties*, indicated in hour  $h \in \{1, \dots, 24\}$  by:  $PExtCong_{h,d}^{AOP} < 0$  for *bids* and *offers*,  $d \in D^{GMPRef}$ , corresponding to the *boundary entity resource* bus for the *global market power reference intertie zone*; or

10.5.1.2.2 the net interchange schedule limit is binding for imports, represented by a non-zero net interchange schedule limit shadow price for incremental imports, indicated in hour  $h \in \{1, \dots, 24\}$  by:  $SPNIUExtBwdT_h^{AOP} \neq 0$ .

10.5.2 If the conditions in sections 10.5.1 are met, then the *day-ahead market calculation engine* shall test *resources* that can meet incremental load within Ontario for global market power, for each hour  $h \in \{1, \dots, 24\}$ , place all  $b \in B^{DG}$  in the set  $BCond_h^{GMP}$ , unless they are excluded because of one of the following two conditions:

10.5.2.1 the *resources* in any zone have congestion components at least \$1/MWh below the internal congestion component at all of the *global market power reference intertie zones*:

10.5.2.1.1 if  $PCong_{h,b}^{AOP} < PIntCong_{h,d}^{AOP} - \$1/\text{MWh}$  where  $d \in D^{GMPRef}$  is true for all *global market power reference intertie zones*, or

10.5.2.2 the *resources* can not meet the incremental load because of a binding transmission constraint:

10.5.2.2.1 if *resources* can not meet incremental load because of any binding transmission *facility* where  $SPNormT_{h,f}^{AOP} \neq 0$  or  $SPEmT_{h,c,f}^{AOP} \neq 0$ .

## 10.6 Constrained Area Conditions Test for Local Market Power (Operating Reserve)

10.6.1 Subject to section 10.6.1.3 for a regional minimum requirement of greater than zero for a specific class of *operating reserve*, then all *resources* within the region with *offers* for classes of *operating reserve* that can satisfy the requirements of the specific class of *operating reserve* shall be tested for local market power:

10.6.1.1 A *resource* shall not qualify for local market power mitigation test for *operating reserve* if the *resource* is located in a region with a binding maximum constraint and for each *resource*  $b \in B^{DG} \cup B^{DL}$  and hour  $h \in \{1, \dots, 24\}$ :

10.6.1.2 subject to section 10.6.1.3, if  $b$  is in a region with a non-zero minimum requirement, then  $b$  is subject to the Conduct Test and is placed in the set  $BCond_h^{10S}$ ,  $BCond_h^{10N}$ , or  $BCond_h^{30R}$ ; and

- 10.6.1.3 if  $b$  is in a region with a binding maximum restriction constraint, then  $b$  is exempt from the Conduct Test.

## 10.7 Constrained Area Conditions Test for Global Market Power (Operating Reserve)

- 10.7.1 A *resource* shall be subject to global market power mitigation testing for *operating reserve* if its *offers* for a class of *operating reserve* where the *locational marginal price* for that class of *operating reserve* is greater than *ORGCondThresh*.
- 10.7.2 Subject to section 10.7.3, if the condition in section 10.7.1 has been met for a class of *operating reserve*, then all *resources* with *offers* for classes of *operating reserve* that can satisfy the requirements of that class of *operating reserve* shall be tested and for each  $b \in B^{DG} \cup B^{DL}$  and hour  $h \in \{1, \dots, 24\}$ :
- 10.7.2.1 if  $L10SP_{t,b}^{PDP} > \text{ORGCondThresh}$ , the *day-ahead market calculation engine* shall add *resource*  $b$  to  $B\text{Cond}_t^{\text{GMP10S}}$ ;
- 10.7.2.2 if  $L10NP_{t,b}^{PDP} > \text{ORGCondThresh}$ , the *day-ahead market calculation engine* shall add *resource*  $b$  to  $B\text{Cond}_t^{\text{GMP10N}}$ ; and
- 10.7.2.3 if  $L30RP_{t,b}^{PDP} > \text{ORGCondThresh}$ , the *day-ahead market calculation engine* shall add *resource*  $b$  to  $B\text{Cond}_t^{\text{GMP30R}}$ .
- 10.7.3 If  $b$  is in a region with a binding maximum constraint, then  $b$  shall be exempt from the Conduct Test.
- 10.7.3.1 If a *resource* is located in a region with a binding regional maximum constraint, then the *resource* shall not qualify for global market power mitigation testing for *operating reserve*.

## 10.8 Outputs

- 10.8.1 Outputs of the Constrained Area Conditions Test include the list of *resources* that will be subject to the Conduct Test in section 11 and the thresholds that will be used in the Conduct Test for those *resources*.



# 11 Conduct Test

## 11.1 Purpose

- 11.1.1 The Conduct Test shall verify whether the *financial dispatch data parameter* values submitted by *registered market participants* for *resources* identified in section 10.8.1 are within the applicable threshold level of the corresponding *reference level values* for those *resources*.

## 11.2 Information, Sets, Indices and Parameters

- 11.2.1 Information, sets, indices and parameters used by the Conduct Test in section 11 are described in section 3. In addition, the list of *resources* produced pursuant to section 10.8.1 shall also be used by the Conduct Test.

## 11.3 Variables

- 11.3.1 The *day-ahead market calculation engine* shall apply the Conduct Test set out in sections 11.4 and 11.5 to the *resources* identified by the Constrained Area Conditions Test in accordance with section 10.8, to identify the following data sets:
- 11.3.1.1 The sets of *resources* that failed the Conduct Test for at least one *financial dispatch data parameter*, where:
- 11.3.1.1.1  $BCT_h^{NCA}$  designates the *resources* in a *narrow constrained area* that failed the Conduct Test for at least one *financial dispatch data parameter* in hour  $h \in \{1, \dots, 24\}$ ;
- 11.3.1.1.2  $BCT_h^{DCA}$  designates the *resources* in a *dynamic constrained area* that failed the Conduct Test for at least one *financial dispatch data parameter* in hour  $h \in \{1, \dots, 24\}$ ;
- 11.3.1.1.3  $BCT_h^{BCA}$  designates the *resources* in a *broad constrained area* that failed the Conduct Test for at least one *financial dispatch data parameter* in hour  $h \in \{1, \dots, 24\}$ ;
- 11.3.1.1.4  $BCT_h^{GMP}$  designates the *resources* that failed the global market power for *energy* Conduct Test for at least one *financial dispatch data parameter* in hour  $h \in \{1, \dots, 24\}$ ;
- 11.3.1.1.5  $BCT_h^{ORL}$  designates the *resources* that failed the local market power for *operating reserve* Conduct Test for at

least one *financial dispatch data parameter* in hour  $h \in \{1, \dots, 24\}$ ; and

11.3.1.1.6  $BCT_h^{ORG}$  designates the *resources* that failed the global market power Conduct Test for *operating reserve* for at least one *financial dispatch data parameter* in hour  $h \in \{1, \dots, 24\}$ ;

11.3.1.2 The following *financial dispatch data parameters* for all hours  $h \in \{1, \dots, 24\}$ :

11.3.1.2.1  $PARAME_{h,b}$  designates the set of *dispatch data* parameters that failed the *energy* Conduct Test at bus  $b \in BCT_h^{NCA} \cup BCT_h^{DCA} \cup BCT_h^{BCA} \cup BCT_h^{GMP}$  in hour  $h$ , and may include the following *dispatch data* parameters:

11.3.1.2.1.1  $EnergyOffer_k$  designates the non-zero quantity of *energy* above the *minimum loading point* in association with *offer* lamination  $k \in K_{h,b}^E$  failed the Conduct Test;

11.3.1.2.2 For all hours prior to and including the last hour where conditions are met for the *energy* Conduct Test:

11.3.1.2.2.1  $EnergyToMLP_k$  designates the non-zero quantity of *energy* up to the *minimum loading point* in association with *offer* lamination  $k \in K_{h,b}^{LTMPLP}$  failed the Conduct Test;

11.3.1.2.2.2  $SUOffer$  designates the *start-up offer* failed the Conduct Test; and

11.3.1.2.2.3  $SNLOffer$  designates the *speed no-load offer* failed the Conduct Test;

11.3.1.2.3  $PARAMOR_{h,b}$  designates the set of *dispatch data* parameters that failed the *operating reserve* Conduct Test at bus  $b \in BCT_h^{ORL} \cup BCT_h^{ORG}$  in hour  $h$ , and may include the following *dispatch data* parameters:

11.3.1.2.3.1  $OR10SOffer_k$  designates the non-zero quantity of *synchronized ten-minute operating reserve* in association with *offer* lamination  $k \in K_{h,b}^{AOS}$  failed the Conduct Test;

11.3.1.2.3.2  $OR10NOffer_k$  designates the non-zero quantity of non-synchronized *ten-minute operating reserve* in association with *offer* lamination  $k \in K_{h,b}^{10N}$  failed the Conduct Test;

11.3.1.2.3.3  $OR30ROffer_k$  designates the non-zero quantity of *thirty-minute operating reserve* in association with *offer* lamination  $k \in K_{h,b}^{30R}$  failed the Conduct Test; and

11.3.1.2.4 For all hours prior to and including the last hour where conditions are met for the *operating reserve* Conduct Test:

11.3.1.2.4.1  $SUOffer$  designates the *start-up offer* failed the Conduct Test;

11.3.1.2.4.2  $SNLOffer$  designates the *speed no-load offer* failed the Conduct Test; and

11.3.1.2.4.3  $EnergyToMLP_k$  designates the non-zero quantity of *energy* up to the *minimum loading point* in association with *offer* lamination  $k \in K_{h,b}^E$  failed the Conduct Test.

## 11.4 Conduct Test for Energy

11.4.1 The *day-ahead market calculation engine* shall perform the Conduct Test for *energy* for *resources* in a *narrow constrained area* that were identified pursuant to section 10.8.1 as follows, subject to sections 11.4.2 and 11.4.3. For each hour  $h \in \{1, \dots, 24\}$  and  $b \in BCond_h^{NCA}$ , the *day-ahead market calculation engine* shall:

11.4.1.1 Evaluate *offers* for *energy* above the *minimum loading point*: For all  $k \in K_{h,b}^E$ , if  $PDG_{h,b,k} > CTEnMinOffer$  and  $PDG_{h,b,k} > \min(PDGRef_{h,b,k} + (abs(PDGRef_{h,b,k}) * CTEnThresh1^{NCA}), PDGRef_{h,b,k} + CTEnThresh2^{NCA})$ , where  $k' \in K_{h,b}^E$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{NCA}$  and add  $EnergyOffer_k$  to  $PARAME_{h,b}$ ;

11.4.1.2 Evaluate *offers* for *energy* for the range of production up to the *minimum loading point*: For all hours prior to and including the hour that qualified to be tested under the Constrained Area Conditions Test, for all  $k \in K_{h,b}^{LTMPL}$ , if  $PLTMLP_{h,b,k} > CTEnMinOffer$  and

$PLTMLP_{h,b,k} > \min(PLTMLP_{ref_{h,b,k}} + (abs(PLTMLP_{ref_{h,b,k}}) * CTEnThresh1^{NCA}), PLTMLP_{ref_{h,b,k}} + CTEnThresh2^{NCA})$ , where  $k' \in K_{h,b}^E$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{NCA}$  and add  $EnergyToMLP_k$  to  $PARAME_{h,b}$  and  $PARAMOR_{h,b}$ ;

11.4.1.3 Evaluate *start-up offers*. For all hours prior to and including the hour where conditions are met for the Constrained Area Conditions Test in section 10, if  $SUDG_{h,b} > SUDG_{ref_{h,b}} + (abs(SUDG_{ref_{h,b}}) * CTSUThresh^{NCA})$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{NCA}$  and add  $SUOffer$  to  $PARAME_{h,b}$  and  $PARAMOR_{h,b}$ ; and

11.4.1.4 Evaluate *speed no-load offers*. For all hours prior to and including the hour that meets the conditions test, if  $SNL_{h,b} > SNL_{ref_{h,b}} + (abs(SNL_{ref_{h,b}}) * CTSNLThresh^{NCA})$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{NCA}$  and add  $SNLOffer$  to  $PARAME_{h,b}$  and  $PARAMOR_{h,b}$ .

11.4.2 For *resources* identified pursuant to section 10.8.1 in a *dynamic constrained area* or broad constrained area, the *day-ahead market calculation engine* shall use the steps in section 11.4.1, using *resources* in  $BCond_h^{DCA}$  or  $BCond_h^{BCA}$ , as the case may be, in place of  $BCond_h^{NCA}$  and using the applicable Conduct Test thresholds  $CTEnThresh1^{DCA}$ ,  $CTEnThresh2^{DCA}$ ,  $CTEnThresh1^{BCA}$ ,  $CTEnThresh2^{BCA}$ ,  $CTSUThresh^{DCA}$ ,  $CTSUThresh^{BCA}$ ,  $CTSNLThresh^{DCA}$ ,  $CTSNLThresh^{BCA}$ . If any of the *financial dispatch data parameters* of a *resource* fail the Conduct Test, the *resource* shall be assigned to subset  $BCT_h^{DCA}$  or  $BCT_h^{BCA}$ , as the case may be.

11.4.3 For *resources* identified pursuant to section 10.8.1 that were selected for global market power mitigation testing for *energy*, the *day-ahead market calculation engine* shall use the steps in section 11.4.1, using *resources* in  $BCond_h^{GMP}$  in place of  $BCond_h^{NCA}$  and the applicable global market power Conduct Test thresholds  $CTEnThresh1^{GMP}$ ,  $CTEnThresh2^{GMP}$ ,  $CTSUThresh^{GMP}$ ,  $CTSNLThresh^{GMP}$ . If any of the applicable *financial dispatch data parameters* of a *resource* fails the Conduct Test, the *resource* shall be assigned to subset  $BCT_h^{GMP}$ .

11.4.4 If a *resource* is assigned to more than one of the sets,  $BCond_h^{NCA}$ ,  $BCond_h^{DCA}$ ,  $BCond_h^{BCA}$ , and  $BCond_h^{GMP}$ , only the Conduct Test with the most restrictive threshold levels shall be performed for that *resource*.

## 11.5 Conduct Test for Operating Reserve

11.5.1 The *day-ahead market calculation engine* shall perform the Conduct Test for local market power for *operating reserve* for *resources* that were identified pursuant to section 10.8.1, as follows, subject to 11.5.3. For each hour  $h \in \{1, \dots, 24\}$  and  $b \in BCond_h^{10S} \cup BCond_h^{10N} \cup BCond_h^{30R}$ , the *day-ahead market calculation engine* shall:

11.5.1.1 Evaluate *offers* for *operating reserve* as follows:

11.5.1.1.1 for all  $k \in K_{h,b}^{10S}$  if  $P10SDG_{h,b,k} > CTORMinOffer$  and  $P10SDG_{h,b,k} > \min(P10SDGRef_{h,b,k'} + (abs(P10SDGRef_{h,b,k'}) * CTORThresh1^{ORL}), P10SDGRef_{h,b,k'} + CTORThresh2^{ORL})$ , where  $k' \in K_{h,b}^{10S}$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $OR10SOffer_k$  to  $PARAMOR_{h,b}$ ;

11.5.1.1.2 for all  $k \in K_{h,b}^{10N}$  if  $P10NDG_{h,b,k} > CTORMinOffer$  and  $P10NDG_{h,b,k} > \min(P10NDGRef_{h,b,k'} + (abs(P10NDGRef_{h,b,k'}) * CTORThresh1^{ORL}), P10NDGRef_{h,b,k'} + CTORThresh2^{ORL})$ , where  $k' \in K_{h,b}^{10N}$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $OR10NOffer_k$  to  $PARAMOR_{h,b}$ ; and

11.5.1.1.3 for all  $k \in K_{h,b}^{30R}$  if  $P30RDG_{h,b,k} > CTORMinOffer$  and  $P30RDG_{h,b,k} > \min(P30RDGRef_{h,b,k'} + (abs(P30RDGRef_{h,b,k'}) * CTORThresh1^{ORL}), P30RDGRef_{h,b,k'} + CTORThresh2^{ORL})$ , where  $k' \in K_{h,b}^{30R}$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $OR30ROffer_k$  to  $PARAMOR_{h,b}$ ;

11.5.1.1.4 for all  $j \in J_{h,b}^{10S}$  if  $P10SDL_{h,b,j} > CTORMinOffer$  and  $P10SDL_{h,b,j} > \min(P10SDLRef_{h,b,j'} + (abs(P10SDLRef_{h,b,j'}) * CTORThresh1^{ORL}), P10SDLRef_{h,b,j'} + CTORThresh2^{ORL})$ , where  $j' \in J_{h,b}^{10S}$ , then the Conduct Test was failed for the

*dispatchable load* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $OR10SOffer_k$  to  $PARAMOR_{h,b}$ ;

11.5.1.1.5 for all  $j \in J_{h,b}^{10N}$  if  $P10NDL_{h,b,j} > CTORMinOffer$  and  $P10NDL_{h,b,j} > \min(P10NDLRef_{h,b,j'} + (abs(P10NDLRef_{h,b,j'}) * CTORThresh1^{ORL}), P10NDLRef_{h,b,j'} + CTORThresh2^{ORL})$ , where  $j' \in J_{h,b}^{10N}$ , then the Conduct Test was failed for the *dispatchable load* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $OR10NOffer_k$  to  $PARAMOR_{h,b}$ ; and

11.5.1.1.6 for all  $j \in J_{h,b}^{30R}$  if  $P30RDL_{h,b,j} > CTORMinOffer$  and  $P30RDL_{h,b,j} > \min(P30RDLRef_{h,b,j'} + (abs(P30RDLRef_{h,b,j'}) * CTORThresh1^{ORL}), P30RDLRef_{h,b,j'} + CTORThresh2^{ORL})$ , where  $j' \in J_{h,b}^{30R}$ , then the Conduct Test was failed for the *dispatchable load* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $OR30ROffer_k$  to  $PARAMOR_{h,b}$ ;

11.5.1.2 Evaluate *start-up offers*. For all hours prior to and including the hour that meets the Constrained Area Conditions Test, if  $SUDG_{h,b} > SUDGRef_{h,b} + (abs(SUDGRef_{h,b}) * CTSUThresh^{ORL})$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $SUOffer$  to  $PARAMOR_{h,b}$  and  $PARAME_{h,b}$ ;

11.5.1.3 Evaluate *speed no-load offers*. For all hours prior to and including the hour that meets the conditions test, if  $SNL_{h,b} > SNLRef_{h,b} + (abs(SNLRef_{h,b}) * CTSNLThresh^{ORL})$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $SNLOffer$  to  $PARAMOR_{h,b}$  and  $PARAME_{h,b}$ ; and

11.5.1.4 Evaluate *offers for energy* for the range of production up to the *minimum loading point*. For all hours prior to and including the hour that meets the conditions test, for all  $k \in K_{h,b}^{LTMLP}$ , if  $PLTMLP_{h,b,k} > CTEnMinOffer$  and  $PLTMLP_{h,b,k} > \min(PLTMLPRef_{h,b,k'} + (abs(PLTMLPRef_{h,b,k'}) * CTEnThresh1^{ORL}), PLTMLPRef_{h,b,k'} + CTEnThresh2^{ORL})$ , where  $k' \in$

$K_{h,b}^{'E}$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_h^{ORL}$  and add  $EnergyToMLP_k$  to  $PARAMOR_{h,b}$  and  $PARAME_{h,b}$ .

- 11.5.2 The *day-ahead market calculation engine* shall perform the Conduct Test for global market power for *operating reserve* for *resources* that were identified pursuant to section 10.8.1. The *day-ahead market calculation engine* shall use the steps set out in section 11.5.1 using *resources* in  $BCond_h^{GMP10S}$ ,  $BCond_h^{GMP10N}$ , and  $BCond_h^{GMP30R}$  in place of  $BCond_h^{10S}$ ,  $BCond_h^{10N}$ , and  $BCond_h^{30R}$ , respectively, and the applicable Conduct Test thresholds  $CTORThresh1^{ORG}$ ,  $CTORThresh2^{ORG}$ ,  $CTSUThresh^{ORG}$ ,  $CTSNLThresh^{ORG}$ ,  $CTEnThresh1^{ORG}$ ,  $CTEnThresh2^{ORG}$ . The *resources* shall be assigned to the subset  $BCT_h^{ORG}$ .
- 11.5.3 If a *resource* is assigned to more than one of  $BCond_h^{GMP10S}$ ,  $BCond_h^{GMP10N}$ , and  $BCond_h^{GMP30R}$ , only the Conduct Test with the most restrictive threshold levels shall be performed for that *resource*.

## 11.6 Outputs

- 11.6.1 Subject to section 11.6.2, the outputs of the Conduct Test shall include the following for each hour  $h \in \{1, \dots, 24\}$ :
- 11.6.1.1 The set of *resources* that failed the Conduct Test for at least one *financial dispatch data parameter* by condition type;
  - 11.6.1.2 The *financial dispatch data parameters* that failed the Conduct Test for the *resource* at bus  $b$ ; and
  - 11.6.1.3 A revised set of *financial dispatch data parameters* for *resources* that failed a Conduct Test with *dispatch data parameters* that failed the Conduct Test replaced with *reference level values*. For *offers* for *energy* and *operating reserve* with multiple laminations:
    - 11.6.1.3.1 if the *offer lamination* for *energy* that corresponds to the *minimum loading point* fails the Conduct Test, the *day-ahead market calculation engine* shall replace all *offer laminations* for *energy* up to the *minimum loading point*;
    - 11.6.1.3.2 if one or more *offer laminations* for *energy* above the *minimum loading point* fails the Conduct Test, the *day-ahead market calculation engine* shall replace all *offer laminations* for *energy* up to and above the *minimum loading point*; and

11.6.1.3.3 if one or more *offer* laminations for *operating reserve* fails the Conduct Test, the *day-ahead market calculation engine* shall replace all *offer* laminations for *operating reserve*.

11.6.2 The *day-ahead market calculation engine* shall not replace the *financial dispatch data parameter* for a *resource* with that *resource's* applicable *reference level value* if the *financial dispatch data parameter* is less than the corresponding *reference level value*.

## 12 Reference Level Scheduling

### 12.1 Purpose

12.1.1 The *day-ahead market calculation engine* shall perform the Reference Level Scheduling algorithm where at least one *financial dispatch data parameter* for a *resource* failed the Conduct Test in section 11.

12.1.2 The Reference Level Scheduling algorithm shall perform a *security*-constrained unit commitment and economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, including *reference level value* for *resources* subject to section 12.2.2, to meet the *IESO's* average province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the next *dispatch day*.

### 12.2 Information, Sets, Indices and Parameters

12.2.1 Information, sets, indices and parameters used by the Reference Level Scheduling algorithm are described in section 3 and 4. In addition, the list of *resources* that failed the Conduct Test from section 11.6.1.1 and a revised set of *financial dispatch data parameters* from section 11.6.1.3, for those *resources* shall be used by the Reference Level Scheduling algorithm.

12.2.2 The Reference Level Scheduling algorithm shall use the *reference level value* that corresponds to any *financial dispatch data parameter* submitted for a *resource* that failed the Conduct Test.

### 12.3 Variables and Objective Function

12.3.1 The *day-ahead market calculation engine* shall solve for the variables listed in section 8.3.1.

12.3.2 The objective function for the Reference Level Scheduling algorithm shall be the same as the objective function in section 8.3.2, subject to section 12.4.



## 12.4 Constraints

- 12.4.1 The constraints in sections 8.4 through 8.7 apply in the Reference Level Scheduling algorithm, except that the sensitivities and limits considered for *IESO* internal transmission limits shall be those provided by the most recent *security* assessment function iteration of the Reference Level Scheduling algorithm.

## 12.5 Outputs

- 12.5.1 Outputs of the Reference Level Scheduling algorithm include *resource* schedules and commitments.

# 13 Reference Level Pricing

## 13.1 Purpose

- 13.1.1 The *day-ahead market calculation engine* shall perform the Reference Level Pricing algorithm whenever the Reference Level Scheduling algorithm has been performed.
- 13.1.2 The Reference Level Pricing algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, *reference level values* for *resources* subject to section 13.2.2, and *resource* schedules and commitments produced by the Reference Level Scheduling algorithm, to meet the *IESO's* average province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the next *dispatch day*.

## 13.2 Information, Sets, Indices and Parameters

- 13.2.1 Information, sets, indices and parameters used by the Reference Level Pricing algorithm are described in sections 3 and 4. In addition, the following *resource* schedule and commitments from the Reference Level Scheduling algorithm shall be used by the Reference Level Pricing algorithm:

- 13.2.1.1  $SDG_{h,b,k}^{RLS}$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide above  $MinQDG_b$  at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^E$ ;

- 13.2.1.2  $ODG_{h,b}^{RLS}$  designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  was scheduled at or above its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ ;
- 13.2.1.3  $S10SDG_{h,b,k}^{RLS}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10S}$ ;
- 13.2.1.4  $S10NDG_{h,b,k}^{RLS}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10N}$ ;
- 13.2.1.5  $S30RDG_{h,b,k}^{RLS}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{30R}$ ; and
- 13.2.1.6  $OHO_{h,b}^{RLS}$ , which designates whether the *dispatchable hydroelectric generation resource* at bus  $b \in B^{HE}$  has been scheduled at or above  $MinHO_{h,b}$  in hour  $h \in \{1, \dots, 24\}$ .

13.2.2 The Reference Level Pricing algorithm shall use a *resource's reference level value* for any *financial dispatch data parameters* submitted by *registered market participants* that failed the Conduct Test.

### 13.3 Variables and Objective Function

- 13.3.1 The *day-ahead market calculation engine* shall solve for the variables set out in section 9.3.1.
- 13.3.2 The objective function used in the Reference Level Pricing algorithm shall be the same as the objective function set out in section 9.3.2, subject to section 13.4.

### 13.4 Constraints

- 13.4.1 The constraints that apply in the Reference Level Pricing algorithm shall be the same as the constraints in sections 9.4 through 9.8, with the following exceptions:
  - 13.4.1.1 the marginal loss factors used in the *energy* balance constraint in section 9.7.1 shall be fixed to the marginal loss factors used in the

last optimization function iteration of the Reference Level Scheduling algorithm;

13.4.1.2 the sensitivities and limits in section 9.7.3 shall be replaced with the most recent *security* assessment function iteration of the Reference Level Pricing algorithm; and

13.4.1.3 for the constraints in section 9.8, the outputs from the As-Offered Scheduling algorithm shall be replaced with the outputs from the Reference Level Scheduling algorithm as follows:

13.4.1.3.1  $SDG_{h,b,k}^{AOS}$  shall be replaced by  $SDG_{h,b,k}^{RLS}$  for all  $h \in \{1, \dots, 24\}, b \in B^{ELR} \cup B^{HE}, k \in K_{h,b}^E$ ;

13.4.1.3.2  $ODG_{h,b}^{AOS}$  shall be replaced by  $ODG_{h,b}^{RLS}$  for all  $h \in \{1, \dots, 24\}, b \in B^{DG}$ ;

13.4.1.3.3  $S10SDG_{h,b,k}^{AOS}$  shall be replaced by  $S10SDG_{h,b,k}^{RLS}$  for all  $h \in \{1, \dots, 24\}, b \in B^{ELR} \cup B^{HE}, k \in K_{h,b}^{10S}$ ;

13.4.1.3.4  $S10NDG_{h,b,k}^{AOS}$  shall be replaced by  $S10NDG_{h,b,k}^{RLS}$  for all  $h \in \{1, \dots, 24\}, b \in B^{ELR} \cup B^{HE}, k \in K_{h,b}^{10N}$ ;

13.4.1.3.5  $S30RDG_{h,b,k}^{AOS}$  shall be replaced by  $S30RDG_{h,b,k}^{RLS}$  for all  $h \in \{1, \dots, 24\}, b \in B^{ELR} \cup B^{HE}, k \in K_{h,b}^{30R}$ ; and

13.4.1.3.6  $OHO_{h,b}^{AOS}$  shall be replaced by  $OHO_{h,b}^{RLS}$  for all  $h \in \{1, \dots, 24\}, b \in B^{HE}$ .

## 13.5 Outputs

13.5.1 Outputs of the Reference Level Pricing algorithm include the following:

13.5.1.1 shadow prices; and

13.5.1.2 *locational marginal prices* and their components.

# 14 Price Impact Test

## 14.1 Purpose

- 14.1.1 The *day-ahead market calculation engine* shall perform the Price Impact Test whenever at least one *financial dispatch data parameter* for a *resource* failed the Conduct Test.
- 14.1.2 The Price Impact Test shall:
  - 14.1.2.1 compare the *locational marginal prices for energy* or *operating reserve* produced by the As-Offered Pricing algorithm with those produced by the Reference Level Pricing algorithm; and
  - 14.1.2.2 consider the corresponding *offer* parameters to have failed the Price Impact Test if the difference in price in section 14.1.2.1 is greater than the applicable impact threshold in section 4.3.8.

## 14.2 Information, Sets, Indices and Parameters

- 14.2.1 Information, sets, indices and parameters for the Price Impact Test are described in sections 3 and 4. In addition, the following *locational marginal prices* from the As-Offered Pricing algorithm and the Reference Level Pricing algorithm shall be used by the Price Impact Test:
  - 14.2.1.1  $LMP_{h,b}^{AOP}$ , which designates the *locational marginal price for energy* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$  from the As-Offered Pricing algorithm;
  - 14.2.1.2  $L30RP_{h,b}^{AOP}$ , which designates the *locational marginal price for thirty-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$  from the As-Offered Pricing algorithm;
  - 14.2.1.3  $L10NP_{h,b}^{AOP}$ , which designates the *locational marginal price for non-synchronized ten-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$  from the As-Offered Pricing algorithm;
  - 14.2.1.4  $L10SP_{h,b}^{AOP}$ , which designates the *locational marginal price for synchronized ten-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$  from the As-Offered Pricing algorithm;
  - 14.2.1.5  $LMP_{h,b}^{RLP}$ , which designates the *locational marginal price for energy* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$  from the Reference Level Pricing algorithm;

- 14.2.1.6  $L30RP_{h,b}^{RLP}$ , which designates the *locational marginal price* for *thirty-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$  from the Reference Level Pricing algorithm;
- 14.2.1.7  $L10NP_{h,b}^{RLP}$ , which designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$  from the Reference Level Pricing algorithm; and
- 14.2.1.8  $L10SP_{h,b}^{RLP}$ , which designates the *locational marginal price* for synchronized *ten-minute operating reserve* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$  from the Reference Level Pricing algorithm.

### 14.3 Variables

14.3.1 The *day-ahead market calculation engine* shall apply the Price Impact Test as set out in sections 14.4 and 14.5 for the *resources* identified in accordance with section 10.3.1, to identify:

- 14.3.1.1 A set of *resources* that failed the Price Impact Test for each condition for all hours  $h \in \{1, \dots, 24\}$ , where:
  - 14.3.1.1.1  $BIT_h^{NCA}$  designates the *resources* in a *narrow constrained area* that failed the Price Impact Test for the *locational marginal price* for *energy*;
  - 14.3.1.1.2  $BIT_h^{DCA}$  designates the *resources* in a *dynamic constrained area* that failed the Price Impact Test for the *locational marginal price* for *energy*;
  - 14.3.1.1.3  $BIT_h^{BCA}$  designates the *resources* in a *broad constrained area* that failed the Price Impact Test for the *locational marginal price* for *energy*;
  - 14.3.1.1.4  $BIT_h^{GMP}$  designates the *resources* that failed the global market power (*energy*) Price Impact Test for the *locational marginal price* for *energy*;
  - 14.3.1.1.5  $BIT_h^{ORL}$  designates the *resources* that failed the local market power (*operating reserve*) Price Impact Test for at least one type of *locational marginal price* for *operating reserve*;
  - 14.3.1.1.6  $BIT_h^{ORG}$  designates the *resources* that failed the global market power (*operating reserve*) Price Impact Test for at

least one type of *locational marginal price* for *operating reserve*; and

14.3.1.1.7  $LMPIT_{h,b}$  designates the *locational marginal price* that failed the Price Impact Test for bus  $b \in BIT_h^{NCA} \cup BIT_h^{DCA} \cup BIT_h^{BCA} \cup BIT_h^{GMP} \cup BIT_h^{ORL} \cup BIT_h^{ORG}$  in hour  $h$ ; and

14.3.1.2 *Locational marginal prices* for *energy* and *operating reserve* for each *resource* at bus  $b \in B^{DG} \cup B^{DL}$  that failed the Price Impact Test, where:

14.3.1.2.1  $EnergyLMP$  designates that the *locational marginal price* for *energy* failed the Price Impact Test;

14.3.1.2.2  $OR10SLMP$  designates that the *locational marginal price* for synchronized *ten-minute operating reserve* failed the Price Impact Test;

14.3.1.2.3  $OR10NLMP$  designates that the *locational marginal price* for non-synchronized *ten-minute operating reserve* failed the Price Impact Test; and

14.3.1.2.4  $OR30RLMP$  designates that the *locational marginal price* for *thirty-minute operating reserve* failed the Price Impact Test.

## 14.4 Price Impact Test for Energy

14.4.1 The *day-ahead market calculation engine* shall perform the Price Impact Test for *resources* that were identified in the corresponding Conduct Test for *energy* in section 11.6.1.1, as follows:

14.4.1.1 For local market power for *energy*:

14.4.1.1.1 For each hour  $h \in \{1, \dots, 24\}$  and  $b \in BCT_h^{NCA}$ , if  $LMP_{h,b}^{AOP} > \min(LMP_{h,b}^{RLP} + (abs(LMP_{h,b}^{RLP}) * ITThresh1^{NCA}), LMP_{h,b}^{RLP} + ITThresh2^{NCA})$ , the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{NCA}$  and add  $EnergyLMP$  to  $LMPIT_{h,b}$ ;

14.4.1.1.2 For each hour  $h \in \{1, \dots, 24\}$  and  $b \in BCT_h^{DCA}$ , if  $LMP_{h,b}^{AOP} > \min(LMP_{h,b}^{RLP} + (abs(LMP_{h,b}^{RLP}) * ITThresh1^{DCA}), LMP_{h,b}^{RLP} + ITThresh2^{DCA})$ , the Price Impact Test was failed

by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{DCA}$  and add  $EnergyLMP$  to  $LMPIT_{h,b}$ ; and

14.4.1.1.3 For each hour  $h \in \{1, \dots, 24\}$  and  $b \in BCT_h^{BCA}$ , if  $LMP_{h,b}^{AOP} > \min(LMP_{h,b}^{RLP} + (abs(LMP_{h,b}^{RLP}) * ITThresh1^{BCA}), LMP_{h,b}^{RLP} + ITThresh2^{BCA})$ , the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{BCA}$  and add  $EnergyLMP$  to  $LMPIT_{h,b}$ .

14.4.1.2 For global market power for *energy*:

14.4.1.2.1 For each hour  $h \in \{1, \dots, 24\}$  and  $b \in BCT_h^{GMP}$ , if  $LMP_{h,b}^{AOP} > \min(LMP_{h,b}^{RLP} + (abs(LMP_{h,b}^{RLP}) * ITThresh1^{GMP}), LMP_{h,b}^{RLP} + ITThresh2^{GMP})$ , the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{GMP}$  and add  $EnergyLMP$  to  $LMPIT_{h,b}$ .

## 14.5 Price Impact Test for Operating Reserve

14.5.1 The *day-ahead market calculation engine* shall perform the Price Impact Test for *resources* that were identified in the corresponding Conduct Test for *operating reserve* in section 11.6.1.1, as follows:

14.5.1.1 For local market power for *operating reserve*, for each hour  $h \in \{1, \dots, 24\}$  and  $b \in BCT_h^{ORL}$ :

14.5.1.1.1 If  $L30RP_{h,b}^{AOP} > L30RP_{h,b}^{RLP}$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{ORL}$  and add  $OR30RLMP$  to  $LMPIT_{h,b}$ ;

14.5.1.1.2 If  $L10NP_{h,b}^{AOP} > L10NP_{h,b}^{RLP}$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{ORL}$  and add  $OR10NLMP$  to  $LMPIT_{h,b}$ ; and

14.5.1.1.3 If  $L10SP_{h,b}^{AOP} > L10SP_{h,b}^{RLP}$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{ORL}$  and add  $OR10SLMP$  to  $LMPIT_{h,b}$ .

14.5.1.2 For global market power for *operating reserve*, for each hour  $h \in \{1, \dots, 24\}$  and  $b \in BCT_h^{ORG}$ :

14.5.1.2.1 If

$L30RP_{h,b}^{AOP} > \min(L30RP_{h,b}^{RLP} + (abs(L30RP_{h,b}^{RLP}) * ITThresh1^{ORG}), L30RP_{h,b}^{RLP} + ITThresh2^{ORG})$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{ORG}$  and add  $OR30RLMP$  to  $LMPIT_{h,b}$ ;

14.5.1.2.2 If

$L10NP_{h,b}^{AOP} > \min(L10NP_{h,b}^{RLP} + (abs(L10NP_{h,b}^{RLP}) * ITThresh1^{ORG}), L10NP_{h,b}^{RLP} + ITThresh2^{ORG})$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BIT_h^{ORG}$  and add  $OR10NLMP$  to  $LMPIT_{h,b}$ ; and

14.5.1.2.3 If

$L10SP_{h,b}^{AOP} > \min(L10SP_{h,b}^{RLP} + (abs(L10SP_{h,b}^{RLP}) * ITThresh1^{ORG}), L10SP_{h,b}^{RLP} + ITThresh2^{ORG})$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource*  $BIT_h^{ORG}$  and add  $OR10SLMP$  to  $LMPIT_{h,b}$ .

## 14.6 Revised Financial Dispatch Data Parameter Determination

14.6.1.1 A *resource* that fails the Price Impact Test shall have its *financial dispatch data parameters* revised as follows:

14.6.1.1 If the *resource* has failed a Price Impact Test for *energy* and is in  $BIT_h^{NCA}$ ,  $BIT_h^{DCA}$ ,  $BIT_h^{BCA}$ , or  $BIT_h^{GMP}$ , the *dispatch data parameters* in  $PARAME_{h,b}$  shall be used to determine the *dispatch data parameters* that shall be replaced.

14.6.1.2 If the *resource* has failed a Price Impact Test for *operating reserve* and is in  $BIT_h^{ORL}$  or  $BIT_h^{ORG}$ , the *dispatch data parameters* in  $PARAMOR_{h,b}$  shall be used to determine the *dispatch data parameters* that shall be replaced.

14.6.1.3 If a *non-quick-start resource* has failed a Price Impact Test in any hour, the *commitment cost parameters* that failed the corresponding Conduct Test shall be replaced with the *resource's* applicable



*reference level value* for that hour. For any hours prior, any *commitment cost parameters* for that *resource* that failed the Conduct Test shall be replaced with the *resource's* applicable *reference level values* in those hours. This is expressed as:

14.6.1.3.1 For each hour  $h \in \{1, \dots, 24\}$  and all  $b \in B^{NQS}$  such that  $b \in BIT_h^{NCA} \cup BIT_h^{DCA} \cup BIT_h^{BCA} \cup BIT_h^{GMP}$ , for hours prior to and including the hour that failed the Price Impact Test,  $H \in \{1, \dots, h\}$ , if  $b \in BCT_H^{NCA} \cup BCT_H^{DCA} \cup BCT_H^{BCA} \cup BCT_H^{GMP}$  and  $PARAME_{H,b}$  contains any of the *commitment cost parameters* *SUOffer*, *SNLOffer*, or *EnergyToMLP<sub>k</sub>*, these parameters shall be replaced with *reference levels*.

14.6.1.4 Section 14.6.1.3 shall apply to the tests for local market power and global market power for *operating reserve*, except  $PARAMOR_{H,b}$  shall be checked in place of  $PARAME_{H,b}$ .

14.6.1.5 If a *resource* is in a *narrow constrained area* or a *dynamic constrained area* and has failed a Price Impact Test, each *resource* in the same *narrow constrained area* or *dynamic constrained area* that also failed the corresponding Conduct Test shall have its *offer* data replaced with its applicable *reference level value* for that hour. For each hour  $h \in \{1, \dots, 24\}$ :

14.6.1.5.1 if  $BIT_h^{NCA}$  includes one or more *resource* in a *narrow constrained area*,  $n$ , each *resource*  $b \in BCT_h^{NCA}$  for the *narrow constrained area*,  $n$ , shall have the parameters in  $PARAME_{h,b}$  replaced with its *reference level values*; and

14.6.1.5.2 if  $BIT_h^{DCA}$  includes one or more *resources* in a *dynamic constrained area*,  $d$ , each *resource*  $b \in BCT_h^{DCA}$  for *dynamic constrained area*,  $d$ , shall have the parameters in  $PARAME_{h,b}$  replaced with its *reference level values*.

14.6.1.6 If a *non-quick-start resource* in a *narrow constrained area* or a *dynamic constrained area* has failed a Price Impact Test, each *non-quick start resource* in the *narrow constrained area* or *dynamic constrained area* that also failed the corresponding Conduct Test shall have its *commitment cost parameters* replaced with its applicable *reference level value* for that hour. For any hours prior, if a *non-quick-start resource* in that *narrow constrained area* or *dynamic constrained area* has a *commitment cost parameter* that failed the Conduct Test, that *commitment cost parameter* shall be replaced with

the *resource's* applicable *reference level value* in those hours. This is expressed as:

14.6.1.6.1 For all hours up to the hour in which a *resource* failed the Price Impact Test for a *narrow constrained area*, for all  $b \in BCT_h^{NCA}$ , if  $PARAME_{h,b}$  contains any of the *commitment cost parameters*  $SUOffer$ ,  $SNLOffer$ , or  $EnergyToMLP_k$ , replace these parameters with *reference level values*.

14.6.1.6.2 For all hours up to the hour in which a *resource* failed the Price Impact Test for a *dynamic constrained area*, for all  $b \in BCT_h^{DCA}$ , if  $PARAME_{h,b}$  contains any of the *commitment cost parameters*  $SUOffer$ ,  $SNLOffer$ , or  $EnergyToMLP_k$ , replace these parameters with *reference level values*.

14.6.1.7 If a *resource* fails the local market power for *operating reserve* Price Impact Test, all *resources* in the same *operating reserve* region with a non-zero *operating reserve* minimum requirement that failed the corresponding Conduct Test for at least one parameter shall have the parameter that failed the Conduct Test replaced with the *resource's* applicable *reference level value* for that hour. This is expressed as:

14.6.1.7.1 For each hour  $h \in \{1, \dots, 24\}$ , if  $BIT_h^{ORL}$  includes one or more *resources* in *operating reserve* region,  $r$ , all *resources*,  $b \in BIT_h^{ORL}$  for *operating reserve* region,  $r$ , shall have the parameters in  $PARAMOR_{h,b}$  replaced with *reference level values*.

14.6.1.8 If a *non-quick start resource* fails the local market power for *operating reserve* Price Impact Test in any hour, the *commitment cost parameters* for all *non-quick start resources* in the same *operating reserve* region with a non-zero *operating reserve* minimum requirement that failed the corresponding Conduct Test shall be replaced with the *resource's* applicable *reference level value* for that hour. For any hours prior, any *commitment cost parameters* of *non-quick start resources* that failed the Conduct Test shall be replaced with the *resource's* applicable *reference level value* in those hours. This is expressed as:

14.6.1.8.1 For all hours up to the hour in which a *resource* failed the Price Impact Test for  $r$ , for all  $b \in BCT_h^{ORL}$ , if  $PARAME_{h,b}$  contains any of the *commitment cost parameters*  $SUOffer$ ,  $SNLOffer$ , or  $EnergyToMLP_k$ , replace these parameters with *reference level values*.

## 14.7 Outputs

- 14.7.1 The *day-ahead market calculation engine* shall prepare the following outputs for each hour  $h \in \{1, \dots, 24\}$ :
- 14.7.1.1 The set of *resources* that failed the Price Impact Test, by condition, in accordance to sections 14.4 and 14.5;
  - 14.7.1.2 The *locational marginal prices* for *energy* and *operating reserve* that failed the Price Impact Test for each *resource* at bus  $b$  in accordance to sections 14.4 and 14.5; and
  - 14.7.1.3 A revised set of *offer* data for *resources* that failed the Price Impact Test, replacing *offer* data that failed the Conduct Test with the applicable *reference level values*, in accordance with section 14.6.
- 14.7.2 The *day-ahead market calculation engine* shall not replace *financial dispatch data parameters* for a *resource* with that *resource's* applicable *reference level value* if the *dispatch data* is less than the *reference level value*.

## 15 Mitigated Scheduling

### 15.1 Purpose

- 15.1.1 The *day-ahead market calculation engine* shall perform the Mitigated Scheduling algorithm if at least one *resource* failed the Price Impact Test in section 14.
- 15.1.2 The Mitigated Scheduling algorithm shall perform a *security-constrained* unit commitment and economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, including *resource reference level values* subject to section 15.2.2, to meet the *IESO's* average province-wide non-*dispatchable demand* forecast and *IESO-specified operating reserve* requirements for each hour of the next *dispatch day*.

### 15.2 Information, Sets, Indices and Parameters

- 15.2.1 Information, sets, indices and parameters used by the Mitigated Scheduling algorithm are described in section 3 and 4. In addition, the Mitigated Scheduling algorithm shall use the list of *resources* that failed the Price Impact Test and a revised set of *financial dispatch data parameters* for those *resources*.

- 15.2.2 For *resources* identified in section 14.7.1, the Mitigated Scheduling algorithm shall use *reference level value* for any *financial dispatch data parameters* that failed the Conduct Test.

## **15.3 Variables, Objective Function and Constraints**

- 15.3.1 The *day-ahead market calculation engine* shall solve for the variables set out in section 8.3.1.
- 15.3.2 The objective function for the Mitigated Scheduling algorithm shall be the same as the objective function in section 8.3.2, subject to the constraints in sections 8.4 through 8.7. The sensitivities and limits used in section 8.7.3 shall be replaced with those provided by the most recent *security* assessment function iteration in the Mitigated Scheduling algorithm.

## **15.4 Outputs**

- 15.4.1 Outputs of the Mitigated Scheduling algorithm include *resource* schedules and commitments.

# **16 Mitigated Pricing**

## **16.1 Purpose**

- 16.1.1 The *day-ahead market calculation engine* shall perform the Mitigated Pricing algorithm if the *day-ahead market calculation engine* performs the Mitigated Scheduling algorithm.
- 16.1.2 The Mitigated Pricing algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, *resource reference level value* subject to section 16.2.2, and *resource* schedules and commitments produced by the Mitigated Scheduling algorithm, to meet the *IESO's* average province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the next *dispatch day*.

## **16.2 Information, Sets, Indices and Parameters**

- 16.2.1 Information, sets, indices and parameters used by the Mitigated Pricing algorithm are described in sections 3 and 4. In addition, the following *resource*

schedules and commitments from the Mitigated Scheduling algorithm shall be used by the Mitigated Pricing algorithm:

- 16.2.1.1  $SDG_{h,b,k}^{MS}$  designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide above  $MinQDG_b$  at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^E$ ;
- 16.2.1.2  $ODG_{h,b}^{MS}$  designates whether a *dispatchable generation resource* at bus  $b \in B^{DG}$  was scheduled at or above its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ ;
- 16.2.1.3  $S10SDG_{h,b,k}^{MS}$  designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10S}$ ;
- 16.2.1.4  $S10NDG_{h,b,k}^{MS}$  designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10N}$ ;
- 16.2.1.5  $S30RDG_{h,b,k}^{MS}$  designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{30R}$ ; and
- 16.2.1.6  $OHO_{h,b}^{MS}$  designates whether a *dispatchable hydroelectric generation resource* at bus  $b \in B^{HE}$  has been scheduled at or above  $MinHO_{h,b}$  in hour  $h \in \{1, \dots, 24\}$ .

- 16.2.2 For each *resource* identified in section 14.7.1, the Mitigated Pricing algorithm shall use such *resource's reference level value* for any *financial dispatch data parameters* that failed the Conduct Test.

## 16.3 Variables and Objective Function

- 16.3.1 The *day-ahead market calculation engine* shall solve for the variables listed in section 9.3.1.
- 16.3.2 The objective function for the Mitigated Pricing algorithm shall be the same as the objective function in section 9.3.2, subject to section 16.4.

## 16.4 Constraints

16.4.1 The constraints that apply in the Mitigated Pricing algorithm shall be the same as the constraints in sections 9.4 through 9.8, with the following exceptions:

16.4.1.1 The marginal loss factors used in the *energy* balance constraint in section 9.7.1 shall be fixed to the marginal loss factors used in the last iteration of the optimization function in the Mitigated Scheduling algorithm.

16.4.1.2 The sensitivities and limits used in section 9.7.3 shall be replaced with those provided by the most recent *security* assessment function iteration in the Mitigated Pricing algorithm.

16.4.1.3 For the constraints in section 9.8, the outputs from the As-Offered Scheduling algorithm shall be replaced with the outputs from the Mitigated Scheduling algorithm as follows:

16.4.1.3.1  $SDG_{h,b,k}^{AOS}$  shall be replaced by  $SDG_{h,b,k}^{MS}$  for all  $h \in \{1, \dots, 24\}$ ,  $b \in B^{ELR} \cup B^{HE}$ ,  $k \in K_{h,b}^E$ ;

16.4.1.3.2  $ODG_{h,b}^{AOS}$  shall be replaced by  $ODG_{h,b}^{MS}$  for all  $h \in \{1, \dots, 24\}$ ,  $b \in B^{DG}$ ;

16.4.1.3.3  $S10SDG_{h,b,k}^{AOS}$  shall be replaced by  $S10SDG_{h,b,k}^{MS}$  for all  $h \in \{1, \dots, 24\}$ ,  $b \in B^{ELR} \cup B^{HE}$ ,  $k \in K_{h,b}^{10S}$ ;

16.4.1.3.4  $S10NDG_{h,b,k}^{AOS}$  shall be replaced by  $S10NDG_{h,b,k}^{MS}$  for all  $h \in \{1, \dots, 24\}$ ,  $b \in B^{ELR} \cup B^{HE}$ ,  $k \in K_{h,b}^{10N}$ ;

16.4.1.3.5  $S30RDG_{h,b,k}^{AOS}$  shall be replaced by  $S30RDG_{h,b,k}^{MS}$  for all  $h \in \{1, \dots, 24\}$ ,  $b \in B^{ELR} \cup B^{HE}$ ,  $k \in K_{h,b}^{30R}$ ; and

16.4.1.3.6  $OHO_{h,b}^{AOS}$  shall be replaced by  $OHO_{h,b}^{MS}$  for all  $h \in \{1, \dots, 24\}$ ,  $b \in B^{HE}$ .

## 16.5 Outputs

16.5.1 Outputs of the Mitigated Pricing algorithm include the following:

16.5.1.1 Shadow prices; and

16.5.1.2 *Locational marginal prices* and their components.

## 17 Pass 2: Reliability Scheduling and Commitment

### 17.1 Purpose

- 17.1.1 Pass 2 shall use *market participant* and *IESO* inputs along with *resource* and system constraints to determine a set of *resource* schedules and commitments. Pass 2 shall consist of the Reliability Scheduling algorithm described in section 18.

## 18 Reliability Scheduling

### 18.1 Purpose

- 18.1.1 The Reliability Scheduling algorithm shall use *dispatch data* submitted by *registered market participants* and perform a *security-constrained* unit commitment and economic *dispatch* to meet the *IESO's* peak province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the next day to minimize the cost of additional commitments.

### 18.2 Information, Sets, Indices and Parameters

- 18.2.1 Information sets, indices and parameters used by the Reliability Scheduling algorithm are described in sections 3 and 4. The Reliability Scheduling algorithm shall also use the following:

- 18.2.1.1 *resource* schedules, commitments, and *locational marginal prices* from Pass 1, where:

18.2.1.1.1  $SXL_{h,d,j}^1$  designates the amount of *energy* that a *boundary entity resource* is scheduled to export at *intertie zone* bus  $d \in DX$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,d}^E$

18.2.1.1.2  $SDG_{h,b,k}^1$  designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide

above  $MinQDG_b$  at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^E$ ;

18.2.1.1.3  $ODG_{h,b}^1$  designates whether a *dispatchable generation resource* at bus  $b \in B^{DG}$  was scheduled at or above its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ ;

18.2.1.1.4  $S10SDG_{h,b,k}^1$  designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10S}$ ;

18.2.1.1.5  $S10NDG_{h,b,k}^1$  designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10N}$ ;

18.2.1.1.6  $S30RDG_{h,b,k}^1$  designates the amount of *thirty-minute operating reserve* that a qualified *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{30R}$ ;

18.2.1.1.7  $SIG_{h,d,k}^1$  designates the amount of *energy* that a *boundary entity resource* is scheduled to import at *intertie zone* bus  $d \in DI$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,d}^E$ ; and

18.2.1.1.8  $LMP_{h,b}^1$  designates the *locational marginal price* in hour  $h \in \{1, \dots, 24\}$  at bus  $b \in B^{ELR} \cup B^{HE}$ ; and

18.2.1.2 the buses identifying either single *energy limited resources* or multiple *dispatchable hydroelectric generation resources* with a registered *forebay*, and the subset of *resources* with a binding *maximum daily energy limit* constraint from Pass 1:

18.2.1.2.1  $B^{LIM} = B^{ELR} \cup \{B_s^{HE} \text{ for all } s \in SHE\}$  designates the set of buses identifying either *energy limited resources* or *dispatchable hydroelectric generation resources* sharing a *maximum daily energy limit*; and

18.2.1.2.2  $B^{BND} \subseteq B^{LIM}$  designates the subset of buses identifying either *energy limited resources*, or *dispatchable hydroelectric generation resources* sharing a *maximum*



*daily energy limit*, with a binding *maximum daily energy limit* constraint from Pass 1, where:

a *maximum daily energy limit* shall be considered binding if the criteria in sections 9.8.2 and 9.8.3.6 are met using  $ODG_{h,b}^1$ ,  $SDG_{h,b,k}^1$ ,  $S10SDG_{h,b,k}^1$ ,  $S10NDG_{h,b,k}^1$  and  $S30RDG_{h,b,k}^1$ .

18.2.2 The Reliability Scheduling algorithm shall use *reference level value* for any *financial dispatch data parameters* that failed the Conduct Test associated with *resources* identified in section 14.7.

18.2.3 *Dispatchable loads, non-dispatchable generation resources*, and the *energy* offered above *minimum loading point* for *dispatchable generation resources* shall be evaluated in the Reliability Scheduling algorithm as follows:

18.2.3.1  $PRucDL_{h,b,j}$  designates the *energy* price for incremental *energy* consumption in hour  $h \in \{1, \dots, 24\}$  at *dispatchable load* bus  $b \in B^{DL}$  in association with *bid* lamination  $j \in J_{h,b}^E$ , where:

$$PRucDL_{h,b,j} = \min(n, PDL_{h,b,j});$$

18.2.3.2  $PRuc10SDL_{h,b,j}$  designates the price of being scheduled to provide synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  at *dispatchable load* bus  $b \in B^{DL}$  in association with *offer* lamination  $j \in J_{h,b}^{10S}$ , where:

$$PRuc10SDL_{h,b,j} = \min(n, P10SDL_{h,b,j});$$

18.2.3.3  $PRuc10NDL_{h,b,j}$  designates the price of being scheduled to provide non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  at *dispatchable load* bus  $b \in B^{DL}$  in association with *offer* lamination  $j \in J_{h,b}^{10N}$ , where:

$$PRuc10NDL_{h,b,j} = \min(n, P10NDL_{h,b,j});$$

18.2.3.4  $PRuc30RDL_{h,b,j}$  designates the price of being scheduled to provide *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  at *dispatchable load* bus  $b \in B^{DL}$  in association with *offer* lamination  $j \in J_{h,b}^{30R}$ , where:

$$PRuc30RDL_{h,b,j} = \min(n, P30RDL_{h,b,j});$$

18.2.3.5  $PRucNDG_{h,b,k}$  designates the *energy* price for incremental generation in hour  $h \in \{1, \dots, 24\}$  at *non-dispatchable generation resource* bus  $b \in B^{NDG}$  in association with *offer* lamination  $k \in K_{h,b}^E$ , where:

$$PRucNDG_{h,b,k} = \min(n, PNDG_{h,b,k});$$

- 18.2.3.6  $PRucDG_{h,b,k}$  designates the *energy* price for incremental generation in hour  $h \in \{1, \dots, 24\}$  at *dispatchable generation resource* bus  $b \in B^{DG}$  in association with *offer* lamination  $k \in K_{h,b}^E$ , where:

$$PRucDG_{h,b,k} = \min(n, PDG_{h,b,k});$$

- 18.2.3.7  $PRuc10SDG_{h,b,k}$  designates the price of being scheduled to provide synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  at *dispatchable generation resource* bus  $b \in B^{DG}$  in association with *offer* lamination  $k \in K_{h,b}^{A0S}$ , where:

$$PRuc10SDG_{h,b,k} = \min(n, P10SDG_{h,b,k});$$

- 18.2.3.8  $PRuc10NDG_{h,b,k}$  designates the price of being scheduled to provide non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  at *dispatchable generation resource* bus  $b \in B^{DG}$  in association with *offer* lamination  $k \in K_{h,b}^{A0N}$ , where:

$$PRuc10NDG_{h,b,k} = \min(n, P10NDG_{h,b,k});$$

- 18.2.3.9  $PRuc30RDG_{h,b,k}$  designates the price of being scheduled to provide *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  at *dispatchable* generation bus  $b \in B^{DG}$  in association with *offer* lamination  $k \in K_{h,b}^{30R}$ , where:

$$PRuc30RDG_{h,b,k} = \min(n, P30RDG_{h,b,k});$$

where:

$$n = \$0.10/\text{MWh};$$

- 18.2.4 For the set of *resources* identified in the buses in section 18.2.1.2, incremental quantities of *energy* at or above *minimum loading point* shall be evaluated in the Reliability Scheduling algorithm as follows:

- 18.2.4.1  $Q1DG_{h,b,k}$  designates an incremental quantity of *energy* that a *resource* may be scheduled to provide in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$  and corresponding to the Pass 1 scheduled portion of the lamination, where:

$$Q1DG_{h,b,k} = SDG_{h,b,k}^1;$$

- 18.2.4.2  $P1DG_{h,b,k}$  designates the price for the incremental quantity of *energy* that a *resource* may be scheduled to provide in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$  and corresponding to the Pass 1 scheduled portion of the lamination, where:

$$P1DG_{h,b,k} = \min (PDG_{h,b,k}, -LMP_{h,b}^1);$$

- 18.2.4.3  $Q2DG_{h,b,k}$  designates an incremental quantity of *energy* that a *resource* may be scheduled to provide in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$  and corresponding to the Pass 1 unscheduled portion of the lamination, where:

$$Q2DG_{h,b,k} = QDG_{h,b,k} - SDG_{h,b,k}^1; \text{ and}$$

- 18.2.4.4  $P2DG_{h,b,k}$  designates the price for the incremental quantity of *energy* that a *resource* may be scheduled to provide in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$  and corresponding to the Pass 1 unscheduled portion of the lamination, where:

$$P2DG_{h,b,k} = \begin{cases} \max(n, PDG_{h,b,k} - LMP_{h,b}^1) & \text{if } b \in B^{BND} \\ \min(n, PDG_{h,b,k}) & \text{otherwise} \end{cases}.$$

## 18.3 Variable and Objective Function

- 18.3.1 The *day-ahead market calculation engine* shall solve for the variables listed in section 8.3.1.
- 18.3.2 The objective function for the Reliability Scheduling algorithm shall be the same as the objective function in section 8.3.2, with the following exceptions:
- 18.3.2.1 The *day-ahead market calculation engine* shall remove the variables for *price responsive loads* ( $SPRL_{h,b,j}$ ), *virtual transaction bids* ( $PVB_{h,v,j}$ ,  $QVB_{h,v,j}$ ), and *virtual transaction offers* ( $PVO_{h,v,k}$ ,  $QVO_{h,v,k}$ ) from the objective function;
- 18.3.2.2 The *day-ahead market calculation engine* shall add the following variables to the objective function:
- 18.3.2.2.1  $S1DG_{h,b,k}$  designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{LIM}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^E$  corresponding to the Pass 1 scheduled portion of the lamination; and
- 18.3.2.2.2  $S2DG_{h,b,k}$  designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{LIM}$  in hour  $h \in \{1, \dots, 24\}$  in association with

lamination  $k \in K_{h,b}^E$  corresponding to the Pass 1 unscheduled portion of the lamination;

18.3.2.3 The objective function coefficients for *dispatchable loads*, *non-dispatchable generation resources* and *dispatchable generation resources* shall be modified to reflect the price of incremental *energy* from such *resources* as specified in section 18.2.3; and

18.3.2.4 The objective function coefficients for single *energy limited resources* and multiple *dispatchable* hydroelectric *generation resources* with a registered *forebay* shall be modified to reflect the pricing of the Pass 1 scheduled and unscheduled portions as specified in section 18.2.4.

18.3.3 The objective function for the Reliability Scheduling algorithm shall minimize the cost of additional commitments by maximizing the following expression:

$$\sum_{h=1, \dots, 24} \left( ObjDL_h - ObjHDR_h + ObjXL_h - ObjNDG_h - ObjDG_h - ObjIG_h - TB_h - ViolCost_h \right)$$

where:

$$ObjDL_h = \sum_{b \in B^{DL}} \left( \sum_{j \in J_{h,b}^E} SDL_{h,b,j} \cdot PRucDL_{h,b,j} - \sum_{j \in J_{h,b}^{10S}} S10SDL_{h,b,j} \cdot PRuc10SDL_{h,b,j} - \sum_{j \in J_{h,b}^{10N}} S10NDL_{h,b,j} \cdot PRuc10NDL_{h,b,j} - \sum_{j \in J_{h,b}^{30R}} S30RDL_{h,b,j} \cdot PRuc30RDL_{h,b,j} \right)$$

$$ObjHDR_h = \sum_{b \in B^{HDR}} \left( \sum_{j \in J_{h,b}^E} SHDR_{h,b,j} \cdot PHDR_{h,b,j} \right)$$

$$ObjXL_h = \sum_{d \in DX} \left( \sum_{j \in J_{h,d}^E} SXL_{h,d,j} \cdot PXL_{h,d,j} - \sum_{j \in J_{h,d}^{10N}} S10NXL_{h,d,j} \cdot P10NXL_{h,d,j} - \sum_{j \in J_{h,d}^{30R}} S30RXL_{h,d,j} \cdot P30RXL_{h,d,j} \right)$$

$$ObjNDG_h = \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{h,b}^E} SNDG_{h,b,k} \cdot PRucNDG_{h,b,k} \right)$$

$$\begin{aligned}
& ObjDG_h \\
&= \sum_{b \in B^{DG}, b \notin B^{LIM}} \left( \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \cdot PRucDG_{h,b,k} \right) \\
&+ \sum_{b \in B^{LIM}} \left( \sum_{k \in K_{h,b}^E} (S1DG_{h,b,k} \cdot P1DG_{h,b,k} + S2DG_{h,b,k} \cdot P2DG_{h,b,k}) \right) \\
&+ \sum_{b \in B^{DG}} \left( \sum_{k \in K_{h,b}^{10S}} S10SDG_{h,b,k} \cdot PRuc10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} S10NDG_{h,b,k} \cdot PRuc10NDG_{h,b,k} + \sum_{k \in K_{h,b}^{30R}} S30RDG_{h,b,k} \cdot PRuc30RDG_{h,b,k} \right) \\
&+ \sum_{b \in B^{NQS}} (ODG_{h,b} \cdot MGODG_{h,b} + IDG_{h,b} \cdot SUDG_{h,b}) \\
& \\
& ObjIG_h = \sum_{d \in DI} \left( \sum_{k \in K_{h,d}^E} SIG_{h,d,k} \cdot PIG_{h,d,k} + \sum_{k \in K_{h,d}^{10N}} S10NIG_{h,d,k} \cdot P10NIG_{h,d,k} \right. \\
&\quad \left. + \sum_{k \in K_{h,d}^{30R}} S30RIG_{h,d,k} \cdot P30RIG_{h,d,k} \right)
\end{aligned}$$

18.3.3.1 The tie-breaking ( $TB_h$ ) and the violation cost ( $ViolCost_h$ ) terms used shall be the ones defined in sections 8.3.1 and 8.3.2.

## 18.4 Constraints

18.4.1 The Reliability Scheduling algorithm optimization shall apply the constraints described in sections 18.5 through 18.7 and 18.8.

## 18.5 Dispatch Data Constraints Applying to Individual Hours

18.5.1 Scheduling Variable Bounds and Commitment Status Variables

18.5.1.1 The constraints shall be the same as in section 8.5.1 with the following exceptions:

18.5.1.1.1 the constraints applying to *price responsive loads* in section 8.5.1.6 shall be removed; and

18.5.1.1.2 the constraints applying to *virtual transaction bids* and *offers* in section 8.5.1.6 shall be removed.

## 18.5.2 Resource Minimums and Maximums

18.5.2.1 The constraints in section 8.5.2 shall apply for *dispatchable loads*, *non-dispatchable generation resources* and inadvertent payback transactions.

18.5.2.2 The constraints in section 8.5.2 shall apply for *dispatchable generation resources*, except the alternative forecast ( $AFG_{h,b}$ ) is replaced with the *IESO's* centralized forecast ( $FG_{h,b}$ ). That is:

$$AdjMaxDG_{h,b} = \begin{cases} \min(MaxDG_{h,b}, FG_{h,b}) & \text{if } b \in B^{VG} \\ MaxDG_{h,b} & \text{otherwise} \end{cases}$$

and

$$AdjMinDG_{h,b} = \min(MinDG_{h,b}, AdjMaxDG_{h,b})$$

Then, for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

$$\begin{aligned} AdjMinDG_{h,b} &\leq MinQDG_b \cdot ODG_{h,b} + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} \\ &\leq AdjMaxDG_{h,b} \end{aligned}$$

## 18.5.3 Operating Reserve Requirements

18.5.3.1 The constraints in section 8.5.4 shall apply for *operating reserve* requirements.

## 18.5.4 Pseudo-Units

18.5.4.1 The constraints in section 8.5.5 shall apply for *pseudo-units*.

## 18.5.5 Dispatchable Hydroelectric Generation Resources

18.5.5.1 The constraints in section 8.5.6 shall apply for *dispatchable hydroelectric generation resources*.

## 18.5.6 Linked Wheeling Through Transactions

18.5.6.1 The constraints in section 8.5.7 shall apply for *linked wheeling through transactions*.

## **18.6 Dispatch Data Inter-Hour/Multi-Hour Constraints**

### **18.6.1 Energy Ramping**

18.6.1.1 The constraints in section 8.6.1 shall apply for *energy* ramping.

### **18.6.2 Operating Reserve Ramping**

18.6.2.1 The constraints in section 8.6.2 shall apply for *operating reserve* ramping.

### **18.6.3 Non-Quick-start Resources**

18.6.3.1 The constraints in section 8.6.3 shall apply for *non-quick start resources*.

### **18.6.4 Energy Limited Resources**

18.6.4.1 The constraints in section 8.6.4 shall apply for *energy limited resources*.

### **18.6.5 Dispatchable Hydroelectric Generation Resources**

18.6.5.1 The constraints in section 8.6.5 shall apply for *dispatchable hydroelectric generation resources*.

## **18.7 Constraints for Reliability Requirements**

### **18.7.1 Energy Balance**

18.7.1.1 The constraint in section 8.7.1 shall apply in the Reliability Scheduling algorithm, with the following exceptions:

18.7.1.1.1 *price responsive loads* shall be removed from the total amount of scheduled *energy* withdrawals,  $With_{h,b}$ , in section 8.7.1.1;

18.7.1.1.2 the net withdrawal for *virtual transaction zones*,  $VWith_{h,m}$ , in sections 8.7.1.2 and 8.7.1.6 shall be removed; and

18.7.1.1.3 the Reliability Scheduling algorithm shall use the *IESO's* peak province-wide non-*dispatchable demand* forecast ( $PFL_h$ ), in place of the *IESO's* average province-wide non-*dispatchable demand* forecast ( $AFL_h$ ).

18.7.1.2 The total amount of *energy* withdrawals scheduled at load bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ ,  $With_{h,b}$  shall be:

$$With_{h,b} = \begin{cases} \sum_{j \in J_{h,b}^E} SDL_{h,b,j} & \text{if } b \in B^{DL} \\ \sum_{j \in J_{h,b}^E} (QHDR_{h,b,j} - SHDR_{h,b,j}) & \text{if } b \in B^{HDR} \end{cases}$$

18.7.1.3 The total amount of *energy* withdrawals scheduled at *intertie zone* bus  $d \in DX$  in hour  $h \in \{1, \dots, 24\}$ ,  $With_{h,d}$  shall be:

$$With_{h,d} = \sum_{j \in J_{h,d}^E} SXL_{h,d,j}$$

18.7.1.4 The total amount of *energy* injections scheduled at internal bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ ,  $Inj_{h,b}$  shall be:

$$Inj_{h,b} = OfferInj_{h,b} + RampInj_{h,b}$$

where:

$$OfferInj_{h,b} = \begin{cases} \sum_{k \in K_{h,b}^E} SNDG_{h,b,k} & \text{if } b \in B^{NDG} \\ ODG_{h,b} \cdot MinQDG_b + \sum_{k \in K_{h,b}^E} SDG_{h,b,k} & \text{if } b \in B^{DG} \end{cases}$$

and

$$RampInj_{h,b} = \begin{cases} \sum_{w=1..min(RampHrs_b, 24-h)} RampE_{b,w} \cdot IDG_{h+w,b} & \text{if } b \in B^{NQS} \\ 0 & \text{otherwise} \end{cases}$$



18.7.1.5 The total amount of *energy* injections scheduled at *intertie zone* bus  $d \in DI$  in hour  $h \in \{1, \dots, 24\}$ ,  $Inj_{h,d}$ , shall be:

$$Inj_{h,d} = \sum_{k \in K_{h,d}^E} SIG_{h,d,k}.$$

18.7.1.6 *Energy* injections and withdrawals at each bus shall be multiplied by one plus the marginal loss factor from the *security* assessment function to reflect the losses or reduction in losses that result when injections or withdrawals occur at locations other than the *reference bus*. These loss-adjusted *energy* injections and withdrawals must then be equal to each other, after taking into account the adjustment for any discrepancy between total and marginal losses. Load or generation reduction associated with the *demand* constraint violation shall be subtracted from the total load or generation to allow the *day-ahead market calculation engine* to produce a solution. For hour  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned} PFL_h + & \sum_{b \in B^{DL \cup B^{HDR}}} (1 + MglLoss_{h,b}) \cdot With_{h,b} \\ & + \sum_{d \in DX} (1 + MglLoss_{h,d}) \cdot With_{h,d} \\ & - \sum_{i=1..N_{LdViol_h}} SLdViol_{h,i} \\ = & \sum_{b \in B^{NDG \cup B^{DG}}} (1 + MglLoss_{h,b}) \cdot Inj_{h,b} \\ & + \sum_{d \in DI} (1 + MglLoss_{h,d}) \cdot Inj_{h,d} \\ & - \sum_{i=1..N_{GenViol_h}} SGenViol_{h,i} + LossAdj_h. \end{aligned}$$

## 18.7.2 Operating Reserve Requirements

18.7.2.1 The constraints in section 8.7.2 shall apply for *operating reserve*.

## 18.7.3 IESO Internal Transmission Limits

18.7.3.1 The constraints in section 8.7.3 shall apply for *IESO* internal transmission limits. The sensitivities and limits applied shall be

provided by the most recent *security* assessment function iteration of the Reliability Scheduling algorithm, with the following exceptions:

18.7.3.2 The terms for *price responsive loads* in sections 8.7.3.3 and 8.7.3.4 shall be removed; and

18.7.3.3 The terms for *bids* and *offers* for *virtual transactions* in sections 8.7.3.3 and 8.7.3.4 shall be removed.

18.7.4 Intertie Limits

18.7.4.1 The constraints in section 8.7.4 shall apply for *intertie* limits.

18.7.5 Penalty Price Variable Bounds

18.7.5.1 The constraints in section 8.7.5 shall apply for penalty price variable bounds.

## 18.8 Constraints to Respect Pass 1 Decisions

18.8.1 The Reliability Scheduling algorithm shall not schedule *energy* import schedules for *boundary entity resources* below those import schedules determined in Pass 1. For all hours  $h \in \{1, \dots, 24\}$  and *intertie zone* buses  $d \in DI$  that are not part of a *linked wheeling through transaction*:

$$\sum_{k \in K_{h,d}^E} SIG_{h,d,k} \geq \sum_{k \in K_{h,d}^E} SIG_{h,d,k}^1$$

18.8.2 The Reliability Scheduling algorithm shall not schedule *energy* export schedules for *boundary entity resources* above those export schedules determined in Pass 1. For all hours  $h \in \{1, \dots, 24\}$  and *intertie zone* buses  $d \in DX$  that are not part of a *linked wheeling through transaction*:

$$\sum_{j \in J_{h,d}^E} SXL_{h,d,j} \leq \sum_{j \in J_{h,d}^E} SXL_{h,d,j}^1$$

18.8.3 The Reliability Scheduling algorithm shall not de-commit *dispatchable generation resources* committed in Pass 1. For all hours  $h \in \{1, \dots, 24\}$  and buses  $b \in B^{DG}$ :

$$ODG_{h,b} \geq ODG_{h,b}^1$$

- 18.8.4 For single *energy limited resources* and multiple *dispatchable* hydroelectric *generation resources* with a registered *forebay*, the Reliability Scheduling algorithm shall ensure the schedule for each *offer* lamination is equal to the schedules corresponding to the Pass 1 scheduled and unscheduled portions. For all buses  $b \in B^{LIM}$ , hours  $h \in \{1, \dots, 24\}$  and *offer* laminations  $k \in K_{h,b}^E$ :

$$SDG_{h,b,k} = S1DG_{h,b,k} + S2DG_{h,b,k}$$

- 18.8.5 The *generation resource* schedules for the Pass 1 scheduled and unscheduled portions of the lamination shall respect the incremental quantity of *energy* beyond the *minimum loading point* that may be scheduled. For all buses  $b \in B^{LIM}$ , hours  $h \in \{1, \dots, 24\}$  and *offer* laminations  $k \in K_{h,b}^E$ :

$$0 \leq S1DG_{h,b,k} \leq Q1DG_{h,b,k}$$

and

$$0 \leq S2DG_{h,b,k} \leq Q2DG_{h,b,k}$$

## 18.9 Outputs

- 18.9.1 Outputs of the Reliability Scheduling algorithm shall include *resource* schedules and commitments.

# 19 Pass 3: DAM Scheduling and Pricing

## 19.1 Purpose

- 19.1.1 Pass 3 shall use *market participant* and *IESO* inputs along with *resource* and system constraints to determine a set of *resource* schedules, commitments, and shadow prices, as well as a set of schedules and *locational marginal prices* that shall be used for *settlement*. Pass 3 consists of the DAM Scheduling algorithm described in section 20 and the DAM Pricing algorithm described in section 21.

## 20 DAM Scheduling

### 20.1 Purpose

- 20.1.1 The DAM Scheduling algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, *reference level values* for *resources* subject to section 20.2.2, and *resource* schedules and commitments from the Reliability Scheduling algorithm, to meet the *IESO's* average province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the next *dispatch day*.

### 20.2 Information, Sets, Indices and Parameters

- 20.2.1 Information, sets, indices and parameters for the DAM Scheduling algorithm are described in sections 3 and 4. In addition, the following *resource* schedules and commitments from Pass 2 shall be used by the DAM Scheduling algorithm:

20.2.1.1  $SXL_{h,d,j}^2$ , which designates the amount of *energy* that a *boundary entity resource* is scheduled to export at *intertie zone* bus  $d \in DX$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,d}^E$ ;

20.2.1.2  $ODG_{h,b}^2$ , which designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  was scheduled at or above its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ ; and

20.2.1.3  $SIG_{h,d,k}^2$ , which designates the amount of *energy* that a *boundary entity resource* is scheduled to import at *intertie zone* bus  $d \in DI$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,d}^E$ .

- 20.2.2 The DAM Scheduling algorithm shall use *reference level value* for any *financial dispatch data parameters* that failed the Conduct Test associated with *resources* identified in section 14.7.

### 20.3 Variables and Objective Function

- 20.3.1 The *day-ahead market calculation engine* shall solve for the variables set out in section 8.3.1.
- 20.3.2 The objective function for the DAM Scheduling algorithm shall be the same as the objective function in section 8.3.2, with the following exceptions:

- 20.3.2.1 the variables for unit commitment decisions ( $ODG_{h,b}$ ) shall be fixed within the optimization function; and
  - 20.3.2.2 the *start-up offer* ( $SUDG_{h,b}$ ) and the *offer* price to operate at *minimum loading point* ( $MGODG_{h,b}$ ) shall be removed from the objective function.
- 20.3.3 The optimization function in the DAM Scheduling algorithm shall be subject to the constraints described in section 20.4.

## 20.4 Constraints

- 20.4.1 The DAM Scheduling algorithm optimization function shall apply the constraints described in sections 20.5– 20.8.

## 20.5 Dispatch Data Constraints Applying to Individual Hours

- 20.5.1 The constraints in section 8.5 shall apply in the DAM Scheduling algorithm.

## 20.6 Dispatch Data Inter-Hour/Multi-Hour Constraints

- 20.6.1 The constraints in section 8.6 shall apply in the DAM Scheduling algorithm, with the exception that the constraints for *non-quick start resources* in section 8.6.3 shall be removed.

## 20.7 Constraints to Ensure Schedules Do Not Violate Reliability Requirements

- 20.7.1 The constraints are the same as in section 8.7. The sensitivities and limits used in section 8.7.3 are those provided by the most recent *security* assessment function iteration of the DAM Scheduling algorithm.

## 20.8 Constraints to Respect Pass 2 Decisions

- 20.8.1 The DAM Scheduling algorithm shall not decrease import schedules from the values produced in Pass 2 and may schedule additional imports of *energy* in Pass 3. For all hours  $h \in \{1, \dots, 24\}$  and *intertie zone* buses  $d \in DI$  that are not part of a *linked wheeling through transaction*:

$$\sum_{k \in K_{h,d}^E} SIG_{h,d,k} \geq \sum_{k \in K_{h,d}^E} SIG_{h,d,k}^2$$

- 20.8.2 The DAM Scheduling algorithm shall not increase export schedules in Pass 3 from the values produced in Pass 2. For all hours  $h \in \{1, \dots, 24\}$  and *intertie zone* buses  $d \in DX$  that are not part of a *linked wheeling through transaction*:

$$\sum_{j \in J_{h,d}^E} SXL_{h,d,j} \leq \sum_{j \in J_{h,d}^E} SXL_{h,d,j}^2$$

- 20.8.3 The DAM Scheduling algorithm shall not change commitments statuses in Pass 3 for *resources* as determined in Pass 2. For all hours  $h \in \{1, \dots, 24\}$  and buses  $b \in B^{DG}$ :

$$ODG_{h,b} = ODG_{h,b}^2$$

## 20.9 Outputs

- 20.9.1 Outputs for the DAM Scheduling algorithm shall include *resource* schedules and commitments.

# 21 DAM Pricing

## 21.1 Purpose

- 21.1.1 The DAM Pricing algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, *reference level values* for *resources* subject to section 21.2.2, and *resource* schedules and commitments produced by the DAM Scheduling algorithm, to meet the *IESO's* average province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the next *dispatch day*.

## 21.2 Information, Sets, Indices and Parameters

- 21.2.1 Information, sets, indices and parameters for the DAM Pricing algorithm are described in sections 3 and 4. In addition, DAM Pricing algorithm shall use the following *resource* schedules and commitments from the DAM Scheduling algorithm in section 20:

- 21.2.1.1  $SDG_{h,b,k}^3$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide above  $MinQDG_b$  at bus

$b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^E$ ;

- 21.2.1.2  $ODG_{h,b}^3$ , which designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  was scheduled at or above its *minimum loading point* in hour  $h \in \{1, \dots, 24\}$ . Note that  $ODG_{h,b}^3 = ODG_{h,b}^2$  for all hours  $h \in \{1, \dots, 24\}$  and buses  $b \in B^{DG}$ ;
- 21.2.1.3  $S10SDG_{h,b,k}^3$ , which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10S}$ ;
- 21.2.1.4  $S10NDG_{h,b,k}^3$ , which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{10N}$ ;
- 21.2.1.5  $S30RDG_{h,b,k}^3$ , which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,b}^{30R}$ ; and
- 21.2.1.6  $OHO_{h,b}^3$ , which designates whether the *dispatchable hydroelectric generation resource* at bus  $b \in B^{HE}$  has been scheduled at or above  $MinHO_{h,b}$  in hour  $h \in \{1, \dots, 24\}$ .

## 21.2.2 The *resource* schedules from Pass 2:

- 21.2.2.1  $SXL_{h,d,j}^2$ , which designates the amount of *energy* that a *boundary entity resource* is scheduled to export at bus  $d \in DX$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $j \in J_{h,d}^E$ ; and
- 21.2.2.2  $SIG_{h,d,k}^2$ , which designates the amount of *energy* that a *boundary entity resource* is scheduled to import at bus  $d \in DI$  in hour  $h \in \{1, \dots, 24\}$  in association with lamination  $k \in K_{h,d}^E$ .
- 21.2.2.3 The DAM Pricing algorithm shall use *reference level values* for any *financial dispatch data parameters* that failed the Conduct Test associated with *resources* identified in section 14.7.

## 21.3 Variables and Objective Function

- 21.3.1 The DAM Pricing algorithm shall solve for the variables listed in section 9.3.1.
- 21.3.2 The objective function for the DAM Pricing algorithm shall be the same as the objective function in section 9.3.2, subject to section 21.4.

## 21.4 Constraints

- 21.4.1 The constraints in sections 9.4 through 9.8 shall apply in the DAM Pricing algorithm, with the following exceptions:
- 21.4.1.1 The marginal loss factors used in the *energy* balance constraint in section 9.7.1 shall be fixed to the marginal loss factors used in the last optimization function iteration of the DAM Scheduling algorithm in section 20.
- 21.4.1.2 The sensitivities and limits used in section 9.7.3 shall be provided by the most recent *security* assessment function iteration of the DAM Pricing algorithm.
- 21.4.1.3 For the constraints in section 9.8, the outputs from the As-Offered Scheduling algorithm in section 8 shall be replaced with the outputs from the DAM Scheduling algorithm in section 20, as follows:
- 21.4.1.3.1  $SDG_{h,b,k}^{AOS}$  shall be replaced by  $SDG_{h,b,k}^3$  for all  $h \in \{1, \dots, 24\}, b \in B^{ELR} \cup B^{HE}, k \in K_{h,b}^E$ ;
- 21.4.1.3.2  $ODG_{h,b}^{AOS}$  shall be replaced by  $ODG_{h,b}^3$  for all  $h \in \{1, \dots, 24\}, b \in B^{DG}$ ;
- 21.4.1.3.3  $S10SDG_{h,b,k}^{AOS}$  shall be replaced by  $S10SDG_{h,b,k}^3$  for all  $h \in \{1, \dots, 24\}, b \in B^{ELR} \cup B^{HE}, k \in K_{h,b}^{10S}$ ;
- 21.4.1.3.4  $S10NDG_{h,b,k}^{AOS}$  shall be replaced by  $S10NDG_{h,b,k}^3$  for all  $h \in \{1, \dots, 24\}, b \in B^{ELR} \cup B^{HE}, k \in K_{h,b}^{10N}$ ;
- 21.4.1.3.5  $S30RDG_{h,b,k}^{AOS}$  shall be replaced by  $S30RDG_{h,b,k}^3$  for all  $h \in \{1, \dots, 24\}, b \in B^{ELR} \cup B^{HE}, k \in K_{h,b}^{30R}$ , and
- 21.4.1.3.6  $OHO_{h,b}^{AOS}$  shall be replaced by  $OHO_{h,b}^3$  for all  $h \in \{1, \dots, 24\}, b \in B^{HE}$ .



21.4.1.4 The constraints imposed for *boundary entity resource* schedules in section 20.8 shall apply to *boundary entity resource* schedules in the DAM Pricing algorithm, with a tolerance  $\Delta$  specified by the *IESO* and:

21.4.1.4.1 For all hours  $h \in \{1, \dots, 24\}$  and *boundary entity resource* import buses  $d \in DI$  that are not part of a *linked wheeling through transaction*:

$$\sum_{k \in K_{h,d}^E} SIG_{h,d,k} \geq \sum_{k \in K_{h,d}^E} SIG_{h,d,k}^2 - \Delta$$

21.4.1.4.2 For all hours  $h \in \{1, \dots, 24\}$  and *boundary entity resource* export buses  $d \in DX$  that are not part of a *linked wheeling through transaction*:

$$\sum_{j \in J_{h,d}^E} SXL_{h,d,j} \leq \sum_{j \in J_{h,d}^E} SXL_{h,d,j}^2 + \Delta$$

## 21.5 Outputs

21.5.1 Outputs of the DAM Pricing algorithm include shadow prices and *locational marginal prices* for *energy* and *operating reserve*.

# 22 Pseudo-Unit Modelling

## 22.1 Pseudo-Unit Model Parameters

22.1.1 The *day-ahead market calculation engine* shall use the following registration and daily *dispatch data* to determine the underlying relationship between a *pseudo-unit* and the associated physical *resources* for a *combined cycle plant* with  $K$  combustion turbine *resources* and one steam turbine *resource*:

22.1.1.1  $CMCR_k$  designates the registered *maximum continuous rating* of combustion turbine  $k \in \{1, \dots, K\}$  in MW;

22.1.1.2  $CMLP_k$  designates the *minimum loading point* of combustion turbine *resource*  $k \in \{1, \dots, K\}$  in MW;

22.1.1.3  $SMCR$  designates the registered *maximum continuous rating* of the steam turbine *resource* in MW;

- 22.1.1.4 *SMLP* designates the *minimum loading point* of the steam turbine *resource* in MW for a 1x1 configuration;
- 22.1.1.5 *SDF* designates the amount of duct firing capacity available on the steam turbine *resource* in MW;
- 22.1.1.6  $STPortion_k$  designates the percentage of the steam turbine *resource* capacity attributed to *pseudo-unit*  $k \in \{1, \dots, K\}$ ; and
- 22.1.1.7  $CSCM_k \in \{0,1\}$  designates whether *pseudo-unit*  $k \in \{1, \dots, K\}$  is flagged to operate in single cycle mode for the day.
- 22.1.2 The *day-ahead market calculation engine* shall calculate the following model parameters for each *pseudo-unit*  $k \in \{1, \dots, K\}$ :
- 22.1.2.1  $MMCR_k$  designates the *maximum continuous rating* of *pseudo-unit*  $k$  and is calculated as follows:
- $$CMCR_k + SMCR \cdot STPortion_k \cdot (1 - CSCM_k)$$
- 22.1.2.2  $MMLP_k$  designates the *minimum loading point* of *pseudo-unit*  $k$  and is calculated as follows:
- $$CMLP_k + SMLP \cdot (1 - CSCM_k)$$
- 22.1.2.3  $MDF_k$  designates the duct firing capacity of *pseudo-unit*  $k$  and is calculated as follows:
- $$SDF \cdot STPortion_k \cdot (1 - CSCM_k)$$
- 22.1.2.4  $MDR_k$  designates the *dispatchable* capacity of *pseudo-unit*  $k$  and is calculated as follows:
- $$MMCR_k - MMLP_k - MDF_k$$
- 22.1.3 The *day-ahead market calculation engine* shall define three operating regions of *pseudo-unit*  $k \in \{1, \dots, K\}$ , as follows:
- 22.1.3.1 The *minimum loading point* region shall be the capacity between 0 and  $MMLP_k$ ;
- 22.1.3.2 The *dispatchable* region shall be the capacity between  $MMLP_k$  and  $MMLP_k + MDR_k$ ; and

22.1.3.3 The duct firing region shall be the capacity between  $MMLP_k + MDR_k$  and  $MMCR_k$ .

22.1.4 The *day-ahead market calculation engine* shall calculate the associated combustion turbine *resource* and steam turbine *resource* shares for the three operating regions of *pseudo-unit*  $k \in \{1,..K\}$ , as follows:

22.1.4.1 For the *minimum loading point* region:

22.1.4.1.1 Steam turbine *resource* share:

$$STShareMLP_k = \frac{SMLP(1-CSCM_k)}{MMLP_k};$$

and

22.1.4.1.2 Combustion turbine *resource* share:

$$CTShareMLP_k = \frac{CMLP_k}{MMLP_k};$$

22.1.4.2 For the *dispatchable* region:

22.1.4.2.1 Steam turbine *resource* share:

$$STShareDR_k = \frac{(1-CSCM_k)(SMCR \cdot STPortion_k - SMLP - SDF_k \cdot STPortion_k)}{MDR_k};$$

and

22.1.4.2.2 Combustion turbine *resource* share:

$$CTShareDR_k = \frac{CMCR_k - CMLP_k}{MDR_k}; \text{ and}$$

22.1.4.3 For the duct firing region:

22.1.4.3.1 Steam turbine *resource* share shall be equal to 1; and

22.1.4.3.2 Combustion turbine *resource* share shall be equal to 0.

## 22.2 Application of Physical Resource Deratings to the Pseudo-Unit Model

22.2.1 The *day-ahead market calculation engine* shall apply deratings submitted by *market participants* to the applicable *dispatchable* capacity and duct firing capacity parameters for a *pseudo-unit*, where:

22.2.1.1  $CTCap_{h,k}$  designates the capacity of combustion turbine *resource*  $k \in \{1, \dots, K\}$  in hour  $h$  as determined by submitted deratings;

22.2.1.2  $STCap_h$  designates the capacity of the steam turbine *resource* in hour  $h$  as determined by submitted deratings; and

22.2.1.3  $TotalQ_{h,k}$  designates the total *offered* quantity of *energy* for *pseudo-unit*  $k \in \{1, \dots, K\}$  in hour  $h$ .

22.2.2 The *day-ahead market calculation engine* shall solve for the following operating region parameters for hour  $h \in \{1, \dots, 24\}$  for each *pseudo-unit*  $k \in \{1, \dots, K\}$ :

22.2.2.1  $MLP_{h,k}$  designates the *minimum loading point* of *pseudo-unit*  $k$  in hour  $h$ ;

22.2.2.2  $DR_{h,k}$  designates the *dispatchable* region capacity of *pseudo-unit*  $k$  in hour  $h$ ; and

22.2.2.3  $DF_{h,k}$  designates the duct firing region capacity of *pseudo-unit*  $k$  in hour  $h$ .

22.2.3 Pre-processing of De-rates

22.2.3.1 The *day-ahead market calculation engine* shall perform the following pre-processing steps to determine the available operating regions for a *pseudo-unit* based on the combustion turbine *resource* and steam turbine *resource* share and the application of the *pseudo-unit* deratings. For *pseudo-unit*  $k \in \{1, \dots, K\}$  for hour  $h \in \{1, \dots, 24\}$ :

22.2.3.1.1 Step 1: Calculate the amount of *offered energy* attributed to each combustion turbine *resource* ( $CTAmt_{h,k}$ ) and steam turbine *resource* portion ( $STAmt_{h,k}$ ):

If  $TotalQ_{h,k} < MMLP_k$  then:

$CTAmt_{h,k} = 0$ ; and

$STAmt_{h,k} = 0$ .

Otherwise:

$$CTAmt_{MLP} = MMLP_k \cdot CTShare_{MLP_k}; \text{ and}$$

$$STAmt_{MLP} = MMLP_k \cdot STShare_{MLP_k}.$$

If  $TotalQ_{h,k} > MMLP_k + MDR_k$ , then:

$$CTAmt_{DR} = MDR_k \cdot CTShare_{DR_k};$$

$$STAmt_{DR} = MDR_k \cdot STShare_{DR_k}; \text{ and}$$

$$STAmt_{DF} = (1 - CSCM_k) \cdot (TotalQ_{h,k} - MMLP_k - MDR_k).$$

Otherwise:

$$CTAmt_{DR} = (TotalQ_{h,k} - MMLP_k) \cdot CTShare_{DR_k};$$

$$STAmt_{DR} = (TotalQ_{h,k} - MMLP_k) \cdot STShare_{DR_k};$$

$$STAmt_{DF} = 0;$$

$$CTAmt_{h,k} = CTAmt_{MLP} + CTAmt_{DR}; \text{ and}$$

$$STAmt_{h,k} = STAmt_{MLP} + STAmt_{DR} + STAmt_{DF}.$$

22.2.3.1.2 Step 2: Allocate the steam turbine *resource* capacity to each *pseudo-unit*:

$$PRSTCap_{h,k} = \left( \frac{STAmt_{h,k}}{\sum_{w \in \{1, \dots, K\}} STAmt_{h,w}} \right) \cdot STCap_h$$

22.2.3.1.3 Step 3: Determine if the *pseudo-unit* is available:

If  $CTAmt_{h,k} < CMLP_k$ , then the *pseudo-unit* is unavailable.

If  $STAmt_{h,k} < SMLP(1 - CSCM_k)$ , then the *pseudo-unit* is unavailable.

If  $CTCap_{h,k} < CMLP_k$ , then the *pseudo-unit* is unavailable.

If  $PRSTCap_{h,k} < SMLP(1 - CSCM_k)$ , then the *pseudo-unit* is unavailable.

22.2.3.1.4 Step 4: Initialize the operating region parameters for hour  $h \in \{1, \dots, 24\}$  to the model parameter values:

$$\text{Set } MLP_{h,k} = MMLP_k.$$

$$\text{Set } DR_{h,k} = MDR_k.$$

$$\text{Set } DF_{h,k} = MDF_k.$$

22.2.3.1.5 Step 5: Apply the derating on the combustion turbine *resource* to the *dispatchable* region:

Calculate  $P$  so that  $CMLP_k + P \cdot CTShareDR_k \cdot MDR_k = CTCap_{h,k}$ ;  
and

Set  $DR_{h,k} = \min(DR_{h,k}, P \cdot MDR_k)$ .

22.2.3.1.6 Step 6: Apply the derating on the steam turbine *resource* to the duct firing and *dispatchable* regions for *pseudo-units* not operating in *single cycle mode*:

Calculate  $R$  so that  $SMLP + R \cdot STShareDR_k \cdot MDR_k = PRSTCap_{h,k}$ .

If  $R \leq 1$ , set  $DF_{h,k} = 0$ , and  $DR_{h,k} = \min(DR_{h,k}, R \cdot MDR_k)$ .

If  $R > 1$ , set  $DF_{h,k} = \min(DF_{h,k}, PRSTCap_{h,k} - SMLP - STShareDR_k \cdot MDR_k)$ .

#### 22.2.4 Available Energy Laminations

22.2.4.1 The *day-ahead market calculation engine* shall determine the *offer* quantity laminations that may be scheduled for *energy* and *operating reserve* in each operating region for hour  $h \in \{1, \dots, 24\}$  for each *pseudo-unit*  $k \in \{1, \dots, K\}$ , subject to section 22.2.4.2, where:

22.2.4.1.1  $QMLP_{h,k}$  designates the total quantity that may be scheduled in the *minimum loading point* region;

22.2.4.1.2  $QDR_{h,k}$  designates the total quantity that may be scheduled in the *dispatchable* region; and

22.2.4.1.3  $QDF_{h,k}$  designates the total quantity that may be scheduled in the duct firing region.

22.2.4.2 The available *offered* quantity laminations shall be subject to the following conditions:

$$0 \leq QMLP_{h,k} \leq MLP_{h,k};$$

$$0 \leq QDR_{h,k} \leq DR_{h,k};$$

$$0 \leq QDF_{h,k} \leq DF_{h,k};$$

if  $QMLP_{h,k} < MLP_{h,k}$ , then the *pseudo-unit* is unavailable and  $QDR_{h,k} = QDF_{h,k} = 0$ ; and

if  $QDR_{h,k} < DR_{h,k}$ , then  $QDF_{h,k} = 0$ .

## 22.3 Convert Physical Resource Constraints to Pseudo-Unit Constraints

22.3.1 The *day-ahead market calculation engine* shall convert physical *resource* constraints to *pseudo-unit* constraints, where:

22.3.1.1  $PSUMin_{h,k}^q$  designates the minimum limitation on *pseudo-unit*  $k$  determined by translating constraint  $q$ . When constraint  $q$  does not provide a minimum limitation on *pseudo-unit*  $k$ , then  $PSUMin_{h,k}^q$  shall be set equal to 0;

22.3.1.2  $PSUMax_{h,k}^q$  designates the maximum limitation on *pseudo-unit*  $k$  determined by translating constraint  $q$ . When constraint  $q$  does not provide a maximum limitation on *pseudo-unit*  $k$ , then  $PSUMax_{h,k}^q$  shall be set equal to  $MLP_{h,k} + DR_{h,k} + DF_{h,k}$ ; and

22.3.1.3  $CTCmt_{h,k} \in \{0,1\}$  designates whether combustion turbine *resource*  $k \in \{1, \dots, K\}$  is considered committed in hour  $h \in \{1, \dots, 24\}$ .

22.3.2 The *day-ahead market calculation engine* shall calculate the minimum and maximum limitations, subject to section 22.3.3.1, as follows:

22.3.2.1 Minimum limitation:  $MinDG_{h,k} = \max_{q \in \{1, \dots, Q\}} PSUMin_{h,k}^q$ ; and

22.3.2.2 Maximum limitation:  $MaxDG_{h,k} = \min_{q \in \{1, \dots, Q\}} PSUMax_{h,k}^q$ .

where  $Q$  designates the number of constraints impacting a *combined cycle plant* that have been provided to the *day-ahead market calculation engine*.

### 22.3.3 Pseudo-unit Minimum and Maximum Constraints

22.3.3.1 *Pseudo-unit* minimum and maximum constraints shall be calculated as follows:

22.3.3.1.1  $PSUMin_{h,k} = PMin$ , where  $PMin$  shall be a minimum constraint provided on *pseudo-unit*  $k \in \{1, \dots, K\}$  for hour  $h \in \{1, \dots, 24\}$ ; and

22.3.3.1.2  $PSUMax_{h,k} = PMax$ , where  $PMax$  shall be a maximum constraint provided on *pseudo-unit*  $k \in \{1, \dots, K\}$  for hour  $h \in \{1, \dots, 24\}$ .

### 22.3.4 Combustion Turbine Resource Minimum and Maximum Constraints

22.3.4.1 If a *pseudo-unit* is not flagged to operate in *single cycle mode*, then the combustion turbine *resource* minimum constraint shall be converted to a *pseudo-unit* constraint as follows:

If  $CTMin < MLP_{h,k} \cdot CTShareMLP_k$ , then set

$$STMinMLP = CTMin \cdot \left( \frac{STShareMLP_k}{CTShareMLP_k} \right); \text{ and}$$

$$STMinDR = 0$$

Otherwise, if  $CTMin \geq MLP_{h,k} \cdot CTShareMLP_k$ , then set

$$STMinMLP = MLP_{h,k} \cdot STShareMLP_k; \text{ and}$$

$$STMinDR = (CTMin - MLP_{h,k} \cdot CTShareMLP_k) \cdot \left( \frac{STShareDR_k}{CTShareDR_k} \right)$$

$$PSUMin_{h,k} = CTMin + STMinMLP + STMinDR$$

22.3.4.2 If a *pseudo-unit* is flagged to operate in *single cycle mode*, then the combustion turbine *resource* minimum constraint shall be converted to a *pseudo-unit* constraint as follows:

$$PSUMin_{h,k} = CTMin$$



- 22.3.4.3 If a *pseudo-unit* is not flagged to operate in *single cycle mode*, then the combustion turbine *resource* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

If  $CTMax < MLP_{h,k} \cdot CTShareMLP_k$ , then  $PSUMax_{h,k} = 0$

Otherwise, calculate the effect of the constraint on the steam turbine within the *minimum loading point* and *dispatchable* regions:

$$STMaxMLP = MLP_{h,k} \cdot STShareMLP_k$$

$$STMaxDR = (CTMax - MLP_{h,k} \cdot CTShareMLP_k) \cdot \left( \frac{STShareDR_k}{CTShareDR_k} \right)$$

$$PSUMax_{h,k} = CTMax + STMaxMLP + STMaxDR$$

- 22.3.4.4 If a *pseudo-unit* is flagged to operate in *single cycle mode*, then the combustion turbine *resource* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

$$PSUMax_{h,k} = CTMax$$

## 22.3.5 Steam Turbine Resource Minimum and Maximum Constraints

- 22.3.5.1 The *day-ahead market calculation engine* shall convert a steam turbine *resource* minimum constraint to a *pseudo-unit* constraint as follows:

22.3.5.1.1 Step 1: Identify  $A \subseteq \{1, \dots, K\}$ , which shall indicate the set of *pseudo-units* to which the constraint may be allocated where *pseudo-unit*  $k \in \{1, \dots, K\}$  is placed in set  $A$  if and only if  $CSCM_k = 0$  and  $CTCmtd_{h,k} = 1$ . If the set  $A$  is empty, then no further steps are required, otherwise proceed to Step 2.

22.3.5.1.2 Step 2: Determine the steam turbine *resource* portion of the capacity of *pseudo-unit*  $k \in A$ :

$$STCap_k = QMLP_{h,k} \cdot STShareMLP_k + QDR_{h,k} \cdot STShareDR_k + QDF_{h,k}$$

22.3.5.1.3 Step 3: Allocate the  $STMin$  constraint to each *pseudo-unit*  $k \in A$ , where  $STMin$  constraint shall be allocated equally to each *pseudo-unit*  $k \in A$  and  $STPMin_k$  is limited by  $STCap_k$ .

22.3.5.1.4 Step 4: The steam turbine *resource* portion minimum constraint shall be converted to a *pseudo-unit* constraint, where for each *pseudo-unit*  $k \in A$ :

If  $STPMin_k < MLP_{h,k} \cdot STShareMLP_k$ , then set

$$CTMinMLP_k = STPMin_k \cdot \left( \frac{CTShareMLP_k}{STShareMLP_k} \right); \text{ and}$$

$$CTMinDR_k = 0$$

Otherwise, if  $STPMin_k \geq MLP_{h,k} \cdot STShareMLP_k$ , then set

$$CTMinMLP_k = MLP_{h,k} \cdot CTShareMLP_k; \text{ and}$$

$$CTMinDR_k = (STPMin_k - MLP_{h,k} \cdot STShareMLP_k) \cdot \left( \frac{CTShareDR_k}{STShareDR_k} \right)$$

<sup>a</sup> Therefore:

$$PSUMin_{h,k} = STPMin_k + CTMinMLP_k + CTMinDR_k$$

22.3.5.2 If *pseudo-units* with sufficient steam turbine *resource* capacity are not committed, then the *day-ahead market calculation engine* shall not convert the entire quantity of the steam turbine *resource* minimum constraint to *pseudo-unit* constraints.

- 22.3.5.3 The steam turbine *resource* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

$$PRSTMax_{h,k} = \left( \frac{STAmt_{h,k}}{\sum_{w \in \{1, \dots, K\}} STAmt_{h,w}} \right) \cdot STMax$$

If the prorated steam turbine maximum constraint limits the steam turbine portion to below its *minimum loading point*, then

$$PSUMax_{h,k} = 0$$

Otherwise, calculate  $R$  so that  $SMLP + R \cdot STShareDR_k \cdot MDR_k = PRSTMax_{h,k}$

If  $R \leq 1$ , set  $PSUMax_{h,k} = MLP_{h,k} + \min(DR_{h,k}, R \cdot MDR_k)$

If  $R > 1$ , set  $PSUMax_{h,k} = MLP_{h,k} + DR_{h,k} + PRSTMax_{h,k} - SMLP - STShareDR_k \cdot MDR_k$

- 22.3.5.4 If the steam turbine *resource* minimum and maximum constraints are equal but do not convert to equal *pseudo-unit* minimum and maximum constraints, then the steam turbine *resource* minimum constraint conversion in section 22.3.5.1 shall be used to determine equal *pseudo-unit* minimum and maximum constraints.

## 22.4 Conversion of Pseudo-Unit Schedules to Physical Resource Schedules

- 22.4.1 For a *combined cycle plant* with  $K$  combustion turbine *resources* and one steam turbine *resource*, the *day-ahead market calculation engine* shall compute the following *energy* and *operating reserve* schedules for hours  $h \in \{1, \dots, 24\}$ :

- 22.4.1.1  $CTE_{h,k}$  designates the *energy* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
- 22.4.1.2  $STPE_{h,k}$  designates the *energy* schedule for the steam turbine *resource* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
- 22.4.1.3  $STE_h$  designates the *energy* schedule for the steam turbine *resource*;
- 22.4.1.4  $CT10S_{h,k}$  designates the synchronized *ten-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;

- 22.4.1.5  $STP10S_{h,k}$  designates the synchronized *ten-minute operating reserve* schedule for the steam turbine *resource* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
  - 22.4.1.6  $ST10S_h$  designates the synchronized *ten-minute operating reserve* schedule for the steam turbine *resource*;
  - 22.4.1.7  $CT10N_{h,k}$  designates the non-synchronized *ten-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
  - 22.4.1.8  $STP10N_{h,k}$  designates the non-synchronized *ten-minute operating reserve* schedule for the steam turbine *resource* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
  - 22.4.1.9  $ST10N_h$  designates the non-synchronized *ten-minute operating reserve* schedule for the steam turbine *resource*;
  - 22.4.1.10  $CT30R_{h,k}$  designates the *thirty-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
  - 22.4.1.11  $STP30R_{h,k}$  designates the *thirty-minute operating reserve* schedule for the steam turbine *resource* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ; and
  - 22.4.1.12  $ST30R_h$  designates the *thirty-minute operating reserve* schedule for the steam turbine *resource*.
- 22.4.2 The *day-ahead market calculation engine* shall determine the following *energy* and *operating reserve* schedules for *pseudo-unit*  $k \in \{1, \dots, K\}$  in hour  $h \in \{1, \dots, 24\}$ :
- 22.4.2.1  $SE_{h,k}$  designates the total amount of *energy* scheduled and  $SE_{h,k} = SEMLP_{h,k} + SEDR_{h,k} + SEDF_{h,k}$  where:
    - 22.4.2.1.1  $SEMLP_{h,k}$  designates the portion of the schedule corresponding to the *minimum loading point* region, where  $0 \leq SEMLP_{h,k} \leq QMLP_{h,k}$ ;
    - 22.4.2.1.2  $SEDR_{h,k}$  designates the portion of the schedule corresponding to the *dispatchable* region, where  $0 \leq SEDR_{h,k} \leq QDR_{h,k}$  and  $SEDR_{h,k} > 0$  only if  $SEMLP_{h,k} = QMLP_{h,k}$ ; and

22.4.2.1.3  $SEDF_{h,k}$  designates the portion of the schedule corresponding to the duct firing region, where  $0 \leq SEDF_{h,k} \leq QDF_{h,k}$  and  $SEDF_{h,k} > 0$  only if  $SEDR_{h,k} = QDR_{h,k}$ ;

22.4.2.2  $S10S_{h,k}$  designates the total amount of synchronized *ten-minute operating reserve* scheduled;

22.4.2.3  $S10N_{h,k}$  designates the total amount of non-synchronized *ten-minute operating reserve* scheduled. If the *pseudo-unit* cannot provide *operating reserve* from its duct firing region then  $0 \leq SE_{h,k} + S10S_{h,k} + S10N_{h,k} \leq QMLP_{h,k} + QDR_{h,k}$ ; and

22.4.2.4  $S30R_{h,k}$  designates the total amount of *thirty-minute operating reserve* scheduled, where  $0 \leq SE_{h,k} + S10S_{h,k} + S10N_{h,k} + S30R_{h,k} \leq QMLP_{h,k} + QDR_{h,k} + QDF_{h,k}$ .

22.4.3 The *day-ahead market calculation engine* shall convert *pseudo-unit* schedules to physical *generation resource* schedules for *energy* and *operating reserve*, as follows:

22.4.3.1 If  $SE_{h,k} \geq MLP_{h,k}$ , then:

$$CTE_{h,k} = SEMLP_{h,k} \cdot CTShareMLP_k + SEDR_{h,k} \cdot CTShareDR_k;$$

$$STPE_{h,k} = SEMLP_{h,k} \cdot STShareMLP_k + SEDR_{h,k} \cdot STShareDR_k + SEDF_{h,k};$$

$$RoomDR_{h,k} = QDR_{h,k} - SEDR_{h,k};$$

$$10SDR_{h,k} = \min(RoomDR_{h,k}, S10S_{h,k});$$

$$10NDR_{h,k} = \min(RoomDR_{h,k} - 10SDR_{h,k}, S10N_{h,k});$$

$$30RDR_{h,k} = \min(RoomDR_{h,k} - 10SDR_{h,k} - 10NDR_{h,k}, S30R_{h,k});$$

$$CT10S_{h,k} = 10SDR_{h,k} \cdot CTShareDR_k;$$

$$STP10S_{h,k} = 10SDR_{h,k} \cdot STShareDR_k + (S10S_{h,k} - 10SDR_{h,k});$$

$$CT10N_{h,k} = 10NDR_{h,k} \cdot CTShareDR_k;$$

$$STP10N_{h,k} = 10NDR_{h,k} \cdot STShareDR_k + (S10N_{h,k} - 10NDR_{h,k});$$

$$CT30R_{h,k} = 30RDR_{h,k} \cdot CTShareDR_k; \text{ and}$$

$$STP30R_{h,k} = 30RDR_{h,k} \cdot STShareDR_k + (S30R_{h,k} - 30RDR_{h,k}).$$

- 22.4.3.2 If  $SE_{h,k} < MLP_{h,k}$  and is ramping to *minimum loading point*, then the conversion shall be determined by the *ramp up energy to minimum loading point*.
- 22.4.3.3 The steam turbine *resources* portion schedules from section 22.4.3.1 shall be summed to obtain the steam turbine *resource* schedule as follows:

$$STE_h = \sum_{k=1,\dots,K} STPE_{h,k};$$

$$ST10S_h = \sum_{k=1,\dots,K} STP10S_{h,k};$$

$$ST10N_h = \sum_{k=1,\dots,K} STP10N_{h,k}; \text{ and}$$

$$ST30R_h = \sum_{k=1,\dots,K} STP30R_{h,k}.$$

## 23 Pricing Formulas

### 23.1 Purpose

- 23.1.1 The *day-ahead market calculation engine* shall calculate *locational marginal prices* using shadow prices, constraint sensitivities and marginal loss factors.

### 23.2 Sets, Indices and Parameters

- 23.2.1 The sets, indices and parameters used to calculate *locational marginal prices* are described in section 4. In addition, the following shadow prices from Passes 1 and 3 shall be used:
- 23.2.1.1  $SPEmT_{h,c,f}^p$  designates the Pass  $p$  shadow price for the post-contingency transmission constraint for *facility*  $f \in F$  in contingency  $c \in C$  in hour  $h$ ;
- 23.2.1.2  $SPEExtT_{h,z}^p$  designates the Pass  $p$  shadow price for the import or export limit constraint  $z \in Z_{Sch}$  in hour  $h$ ;
- 23.2.1.3  $SPL_h^p$  designates the Pass  $p$  shadow price for the *energy* balance constraint in hour  $h$ ;
- 23.2.1.4  $SPNIUExtBwdT_h^p$  designates the Pass  $p$  shadow price for the net interchange scheduling limit constraint limiting increases in net imports between hour  $(h - 1)$  and hour  $h$ ;

- 23.2.1.5  $SPNIDExtBwdT_h^p$  designates the Pass  $p$  shadow price for the net interchange scheduling limit constraint limiting decreases in net imports between hour  $(h - 1)$  and hour  $h$ ;
- 23.2.1.6  $SPNIUExtFwdT_h^p$  designates the Pass  $p$  shadow price for the net interchange scheduling limit constraint limiting increases in net imports between hour  $h$  and hour  $(h + 1)$ ;
- 23.2.1.7  $SPNIDExtFwdT_h^p$  designates the Pass  $p$  shadow price for the net interchange scheduling limit constraint limiting decreases in net imports between hour  $h$  and hour  $(h + 1)$ ;
- 23.2.1.8  $SPNormT_{h,f}^p$  designates the Pass  $p$  shadow price for the pre-contingency transmission constraint for *facility*  $f \in F$  in hour  $h$ ;
- 23.2.1.9  $SP10S_h^p$  designates the Pass  $p$  shadow price for the total synchronized *ten-minute operating reserve* requirement constraint in hour  $h$ ;
- 23.2.1.10  $SP10R_h^p$  designates the Pass  $p$  shadow price for the total *ten-minute operating reserve* requirement constraint in hour  $h$ ;
- 23.2.1.11  $SP30R_h^p$  designates the Pass  $p$  shadow price for the total *thirty-minute operating reserve* requirement constraint in hour  $h$ ;
- 23.2.1.12  $SPREGMin10R_{h,r}^p$  designates the Pass  $p$  shadow price for the minimum *ten-minute operating reserve* constraint for region  $r \in ORREG$  in hour  $h$ ;
- 23.2.1.13  $SPREGMin30R_{h,r}^p$  designates the Pass  $p$  shadow price for the minimum *thirty-minute operating reserve* constraint for region  $r \in ORREG$  in hour  $h$ ;
- 23.2.1.14  $SPREGMax10R_{h,r}^p$  designates the Pass  $p$  shadow price for the maximum *ten-minute operating reserve* constraint for region  $r \in ORREG$  in hour  $h$ ; and
- 23.2.1.15  $SPREGMax30R_{h,r}^p$  designates the Pass  $p$  shadow price for the maximum *thirty-minute operating reserve* constraint for region  $r \in ORREG$  in hour  $h$ .

## 23.3 Locational Marginal Prices for Energy

### 23.3.1 Energy Locational Marginal Prices for Delivery Points

23.3.1.1 The *day-ahead market calculation engine* shall calculate a *locational marginal price* and components for *energy* for each Pass  $p \in \{1,3\}$  and hour  $h \in \{1, \dots, 24\}$  for every bus  $b \in L$  where a non-*dispatchable* or *dispatchable generation resource*, a *dispatchable load*, a *price responsive load*, an *hourly demand response resource*, or a non-*dispatchable load* is sited and:

23.3.1.1.1  $LMP_{h,b}^p$  designates the Pass  $p$  hour  $h$  *locational marginal price for energy*;

23.3.1.1.2  $PRef_h^p$  designates the Pass  $p$  hour  $h$  energy locational marginal price for energy at the reference bus;

23.3.1.1.3  $PLoss_{h,b}^p$  designates the Pass  $p$  hour  $h$  loss component; and

23.3.1.1.4  $PCong_{h,b}^p$  designates the Pass  $p$  hour  $h$  congestion component.

23.3.1.2 The *day-ahead market calculation engine* shall calculate an initial *locational marginal price for energy*, a *locational marginal price for energy* at the *reference bus*, a loss component and a congestion component for Pass  $p \in \{1,3\}$  at bus  $b \in L$  in hour  $h \in \{1, \dots, 24\}$ , as follows:

$$InitLMP_{h,b}^p = InitPRef_h^p + InitPLoss_{h,b}^p + InitPCong_{h,b}^p$$

where

$$InitPRef_h^p = SPL_h^p;$$

$$InitPLoss_{h,b}^p = MglLoss_{h,b}^p \cdot SPL_h^p;$$

and

$$InitPCong_{h,b}^p = \sum_{f \in F_h} PreConSF_{h,f,b} \cdot SPNormT_{h,f}^p + \sum_{c \in C} \sum_{f \in F_{h,c}} SF_{h,c,f,b} \cdot SPEmT_{h,c,f}^p$$



- 23.3.1.3 If the initial *locational marginal price for energy* at the *reference bus* ( $InitPRef_h^p$ ) is not within the *settlement bounds* ( $EngyPrcFlr, EngyPrcCeil$ ), then the *day-ahead market calculation engine* shall modify the *locational marginal price for energy* at the *reference bus* as follows:

If  $InitPRef_h^p > EngyPrcCeil$ ,  $PRef_h^p = EngyPrcCeil$

If  $InitPRef_h^p < EngyPrcFlr$ ,  $PRef_h^p = EngyPrcFlr$

Otherwise,  $PRef_h^p = InitPRef_h^p$

- 23.3.1.4 If the initial *locational marginal price for energy* ( $InitLMP_{h,b}^p$ ) is not within the *settlement bounds* ( $EngyPrcFlr, EngyPrcCeil$ ), then the *day-ahead market calculation engine* shall modify the *locational marginal price for energy* as follows:

If  $InitLMP_{h,b}^p > EngyPrcCeil$ ,  $LMP_{h,b}^p = EngyPrcCeil$

If  $InitLMP_{h,b}^p < EngyPrcFlr$ ,  $LMP_{h,b}^p = EngyPrcFlr$

Otherwise,  $LMP_{h,b}^p = InitLMP_{h,b}^p$

- 23.3.1.5 The *day-ahead market calculation engine* shall modify the *loss component* as follows:

If  $PRef_h^p \neq InitPRef_h^p$ , then  $PLoss_{h,b}^p = MglLoss_{h,b}^p \cdot PRef_h^p$

Otherwise,  $PLoss_{h,b}^p = InitPLoss_{h,b}^p$

- 23.3.1.6 The *day-ahead market calculation engine* shall modify the *congestion component* as follows:

If  $LMP_{h,b}^p - PRef_h^p - PLoss_{h,b}^p$  and

$InitPCong_{h,b}^p$  have the same mathematical sign, then  $PCong_{h,b}^p =$

$LMP_{h,b}^p - PRef_h^p - PLoss_{h,b}^p$

Otherwise,  $PCong_{h,b}^p = 0$  and  $PLoss_{h,b}^p = LMP_{h,b}^p - PRef_h^p$

## 23.3.2 Energy Locational Marginal Prices for Intertie Metering Points

- 23.3.2.1 The *day-ahead market calculation engine* shall calculate a *locational marginal price* and components for *energy* for each  $Pass\ p \in \{1,3\}$  and hour  $h \in \{1, \dots, 24\}$  for *intertie zone bus*  $d \in D$ , where:

- 23.3.2.1.1  $ExtLMP_{h,d}^p$  designates the  $Pass\ p$  hour  $h$  *locational marginal price for energy*,

- 23.3.2.1.2  $IntLMP_{h,d}^p$  designates the Pass  $p$  hour  $h$  *intertie border price for energy*;
  - 23.3.2.1.3  $ICP_{h,d}^p$  designates the Pass  $p$  hour  $h$  *intertie congestion price*;
  - 23.3.2.1.4  $PRef_h^p$  designates the Pass  $p$  hour  $h$  *locational marginal price for energy* at the reference bus;
  - 23.3.2.1.5  $PLoss_{h,d}^p$  designates the Pass  $p$  hour  $h$  loss component;
  - 23.3.2.1.6  $PIntCong_{h,d}^p$  designates the Pass  $p$  hour  $h$  internal congestion component for *energy*;
  - 23.3.2.1.7  $PExtCong_{h,d}^p$  designates the Pass  $p$  hour  $h$  external congestion component for the *intertie congestion price*; and
  - 23.3.2.1.8  $PNISL_{h,d}^p$  designates the Pass  $p$  hour  $h$  net interchange scheduling limit congestion component for the *intertie congestion price*.
- 23.3.2.2 The *day-ahead market calculation engine* shall calculate an initial *locational marginal price for energy*, a *locational marginal price for energy* for the *reference bus*, a loss component and a congestion component for *energy* for Pass  $p$  at *intertie zone bus*  $d \in D_a$  in *intertie*

zone  $a \in A$  in hour  $h \in \{1, \dots, 24\}$ , subject to section 23.3.2.8 and 23.3.2.9, as follows:

$$InitExtLMP_{h,d}^p = InitIntLMP_{h,d}^p + InitICP_{h,d}^p$$

where

$$InitPRef_h^p = SPL_h^p ;$$

$$InitPloss_{h,d}^p = MglLoss_{h,d}^p \cdot SPL_h^p ;$$

$$\begin{aligned} InitPIntCong_{h,d}^p &= \sum_{f \in F_h} PreConSF_{h,f,d} \cdot SPNormT_{h,f}^p \\ &+ \sum_{c \in C} \sum_{f \in F_{h,c}} SF_{h,c,f,d} \cdot SPEmT_{h,c,f}^p ; \end{aligned}$$

$$\begin{aligned} InitIntLMP_{h,d}^p &= InitPRef_h^p + InitPloss_{h,d}^p \\ &+ InitPIntCong_{h,d}^p ; \end{aligned}$$

$$InitICP_{h,d}^p = InitPExtCong_{h,d}^p + InitPNISL_{h,d}^p ;$$

$$InitPExtCong_{h,d}^p = \sum_{z \in Z_{sch}} EnCoeff_{a,z} \cdot SPExtT_{h,z}^p ;$$

and

$$\begin{aligned} InitPNISL_{h,d}^p &= SPNIUExtBwdT_h^p - SPNIUExtFwdT_h^p \\ &- SPNIDExtBwdT_h^p + SPNIDExtFwdT_h^p \end{aligned}$$

23.3.2.3 If the initial *locational marginal price* for *energy* ( $InitExtLMP_{h,d}^p$ ) is not within the *settlement* bounds ( $EngyPrcFlr, EngyPrcCeil$ ), then the *day-ahead market calculation engine* shall modify the *intertie border price* for *energy*, and its components, as follows:

23.3.2.3.1 The initial *locational marginal price* for the *reference bus* ( $InitPRef_h^p$ ) shall be modified per section 23.3.1.3;

23.3.2.3.2 The initial *intertie border price* ( $InitIntLMP_{h,d}^p$ ) shall be modified per section 23.3.1.4, where  $InitLMP_{h,b}^p = InitIntLMP_{h,d}^p$ ;

23.3.2.3.3 The initial loss component ( $InitPloss_{h,b}^p$ ) shall be modified per section 23.3.1.5; and

23.3.2.3.4 The initial congestion component ( $InitPCong_{h,b}^p$ ) shall be modified per section 23.3.1.6.

23.3.2.4 If the initial *locational marginal price* for *energy* ( $InitExtLMP_{h,d}^p$ ) is not within the *settlement bounds* ( $EngyPrcFlr, EngyPrcCeil$ ), then the *day-ahead market calculation engine* shall modify the *locational marginal price* for *energy*, as follows:

If  $InitExtLMP_{h,d}^p > EngyPrcCeil$ , set  $ExtLMP_{h,d}^p = EngyPrcCeil$

If  $InitExtLMP_{h,d}^p < EngyPrcFlr$ , set  $ExtLMP_{h,d}^p = EngyPrcFlr$

Otherwise, set  $ExtLMP_{h,d}^p = InitExtLMP_{h,d}^p$

23.3.2.5 If the modified *locational marginal price* for *energy* ( $ExtLMP_{h,d}^p$ ) is equal to the *intertie border price* for *energy* ( $IntLMP_{h,d}^p$ ), then the *day-ahead market calculation engine* shall modify the external congestion component for the *intertie congestion price* and net interchange scheduling limit congestion components for the *intertie congestion price*, as follows:

If  $ExtLMP_{h,d}^p = IntLMP_{h,d}^p$  set  $PExtCong_{h,d}^p = 0$  and  $PNISL_{h,d}^p = 0$

23.3.2.6 If the modified *locational marginal price* for *energy* ( $ExtLMP_{h,d}^p$ ) is not equal to the *intertie border price* for *energy* ( $IntLMP_{h,d}^p$ ), then the *day-ahead market calculation engine* shall modify the external congestion component for the *intertie congestion price* and net interchange scheduling limit congestion components for the *intertie congestion price*, as follows:

If  $ExtLMP_{h,d}^p \neq IntLMP_{h,d}^p$ , set

$$PNISL_{h,d}^p = (ExtLMP_{h,d}^p - IntLMP_{h,d}^p) \cdot \left( \frac{InitPNISL_{h,d}^p}{InitPNISL_{h,d}^p + InitPExtCong_{h,d}^p} \right)$$

If  $PNISL_{h,d}^p > NISLPen$ ,  $PNISL_{h,d}^p = NISLPen$

If  $PNISL_{h,d}^p < (-1) \cdot NISLPen$ ,  $PNISL_{h,d}^p = (-1) \cdot NISLPen$

Then  $PExtCong_{h,d}^p = ExtLMP_{h,d}^p - IntLMP_{h,d}^p - PNISL_{h,d}^p$

23.3.2.7 The *day-ahead market calculation engine* shall calculate the *intertie congestion price* as follows:

$$ICP_{h,d}^p = PExtCong_{h,d}^p + PNISL_{h,d}^p$$

23.3.2.8 The *locational marginal price for energy* calculated by the *day-ahead market calculation engine* shall be the same for all *boundary entity resource* buses at the same *intertie zone*. *Intertie* transactions associated with the same *boundary entity resource* bus, but specified as occurring at different *intertie zones*, subject to phase shifter operation, shall be modelled as flowing across independent paths. Pricing of these transactions shall utilize shadow prices associated with the internal transmission constraints, *intertie* limits and transmission losses applicable to the path associated to the relevant *intertie zone*.

23.3.2.9 When an *intertie zone* is out-of-service, the *intertie* limits for that *intertie zone* will be set to zero and all import and export *boundary entity resources* for that *intertie zone* will receive a zero schedule and the *locational marginal price for energy* shall be set to the *intertie border price for energy*.

### 23.3.3 Zonal Prices for Energy

23.3.3.1 The *day-ahead market calculation engine* shall calculate the zonal price for *energy* and its components for each Pass  $p \in \{1,3\}$  and hour  $h \in \{1, \dots, 24\}$  for each *virtual transaction zone*  $m \in M$ , as follows:

$$VZonalP_{h,m}^p = PRef_h^p + VZonalP_{h,m}^{Loss,p} + VZonalP_{h,m}^{Cong,p}$$

where

$$VZonalP_{h,m}^{Loss,p} = \sum_{b \in L_m^{VIRT}} WF_{h,m,b}^{VIRT} \cdot P_{h,b}^{Loss,p}$$

and

$$VZonalP_{h,m}^{Cong,p} = \sum_{b \in L_m^{VIRT}} WF_{h,m,b}^{VIRT} \cdot P_{h,b}^{Cong,p}$$

23.3.3.2 The *day-ahead market calculation engine* shall calculate the zonal price for *energy* and its components for each Pass  $p \in \{1,3\}$  and hour  $h \in \{1, \dots, 24\}$  for *non-dispatchable load zone*,  $y \in Y$  as follows:

$$ZonalP_{h,y}^p = PRef_h^p + ZonalP_{h,y}^{Loss,p} + ZonalP_{h,y}^{Cong,p}$$

where

$$ZonalP_{h,y}^{Loss,p} = \sum_{b \in L_y^{NDL}} WF_{h,y,b}^{NDL} \cdot P_{h,b}^{Loss,p}$$

and

$$ZonalP_{h,y}^{Cong,p} = \sum_{b \in L_y^{NDL}} WF_{h,y,b}^{NDL} \cdot P_{h,b}^{Cong,p}$$

23.3.3.3 The *day-ahead market Ontario zonal price* is calculated per section 23.3.3.2 where the *non-dispatchable load zone* is comprised of all *non-dispatchable loads* within Ontario.

#### 23.3.4 Pseudo-Unit Pricing

23.3.4.1 The *day-ahead market calculation engine* shall calculate a *locational marginal price* and components for *energy* for each Pass  $p \in \{1,3\}$  and hour  $h \in \{1, \dots, 24\}$  for every *pseudo-unit*  $k \in \{1, \dots, K\}$  where:

23.3.4.1.1  $CTMglLoss_{h,k}^p$  designates the marginal loss factor for the combustion turbine *resource* identified by *pseudo-unit*  $k$  for hour  $h$  in Pass  $p$ ;

23.3.4.1.2  $STMglLoss_{h,k}^p$  designates the marginal loss factor for the steam turbine *resource* identified by *pseudo-unit*  $k$  for hour  $h$  in Pass  $p$ ;

23.3.4.1.3  $CTPreConSF_{h,f,k}$  designates the pre-contingency sensitivity factor for the combustion turbine *resource* identified by *pseudo-unit*  $k$  on *facility*  $f$  during hour  $h$  under pre-contingency conditions;

23.3.4.1.4  $STPreConSF_{h,f,k}$  designates the pre-contingency sensitivity factor for the steam turbine *resource* identified by *pseudo-unit*  $k$  on *facility*  $f$  during hour  $h$  under pre-contingency conditions;

23.3.4.1.5  $CTSF_{h,c,f,k}$  designates the post-contingency sensitivity factor for the combustion turbine *resource* identified by *pseudo-unit*  $k$  on *facility*  $f$  during hour  $h$  under post-contingency conditions for contingency  $c$ ; and

23.3.4.1.6  $STSF_{h,c,f,k}$  designates the post-contingency sensitivity factor for the steam turbine *resource* identified by *pseudo-unit*  $k$  on *facility*  $f$  during hour  $h$  under post-contingency conditions for contingency  $c$ .

23.3.4.2 The *day-ahead market calculation engine* shall calculate an initial *locational marginal price* for *energy*, a *locational marginal price* for *energy* at the *reference bus*, a loss component and a congestion component for Pass  $p \in \{1,3\}$  for every *pseudo-unit*  $k \in \{1, \dots, K\}$  in hour  $h \in \{1, \dots, 24\}$ , as follows:

$$InitLMP_{h,k}^p = InitPRef_h^p + InitPLoss_{h,k}^p + InitPCong_{h,k}^p$$

where

$$InitPRef_h^p = SPL_h^p;$$

$$InitPLoss_{h,k}^p = MglLoss_{h,k}^p \cdot SPL_h^p;$$

and

$$InitPCong_{h,k}^p = \sum_{f \in F_h} PreConSF_{h,f,k} \cdot SPNormT_{h,f}^p + \sum_{c \in C} \sum_{f \in F_{h,c}} SF_{h,c,f,k} \cdot SPEmT_{h,c,f}^p$$

23.3.4.3 If *pseudo-unit*  $k \in \{1, \dots, K\}$  is scheduled within its Minimum Loading Point range or not scheduled at all, its marginal loss and sensitivity factors shall be:

$$MglLoss_{h,k}^p = CTShareMLP_k \cdot CTMglLoss_{h,k}^p + STShareMLP_k \cdot STMglLoss_{h,k}^p$$

$$PreConSF_{h,f,k} = CTShareMLP_k \cdot CTPreConSF_{h,f,k} + STShareMLP_k \cdot STPreConSF_{h,f,k}$$

$$SF_{h,c,f,k} = CTShareMLP_k \cdot CTSF_{h,c,f,k} + STShareMLP_k \cdot STSF_{h,c,f,k}$$

23.3.4.4 If *pseudo-unit*  $k \in \{1, \dots, K\}$  is scheduled within its *dispatchable* region, its marginal loss and sensitivity factors shall be:

$$MglLoss_{h,k}^p = CTShareDR_k \cdot CTMglLoss_{h,k}^p + STShareDR_k \cdot STMglLoss_{h,k}^p$$

$$PreConSF_{h,f,k} = CTShareDR_k \cdot CTPreConSF_{h,f,k} + STShareDR_k \cdot STPreConSF_{h,f,k}$$

$$SF_{h,c,f,k} = CTShareDR_k \cdot CTSF_{h,c,f,k} + STShareDR_k \cdot STSF_{h,c,f,k}$$

23.3.4.5 If *pseudo-unit*  $k \in \{1, \dots, K\}$  is scheduled within its duct firing region, its marginal loss and sensitivity factors shall be:

$$MglLoss_{h,k}^p = STMglLoss_{h,k}^p$$

$$PreConSF_{h,f,k} = STPreConSF_{h,f,k}$$

$$SF_{h,c,f,k} = STSF_{h,c,f,k}$$

## 23.4 Locational Marginal Prices for Operating Reserve

23.4.1 Operating Reserve Locational Marginal Prices for Delivery Points

23.4.1.1 The *day-ahead market calculation engine* shall calculate a *locational marginal price* and components for *operating reserve* for each Pass  $p \in \{1,3\}$  and hour  $h \in \{1, \dots, 24\}$  for a *delivery point* associated with the *dispatchable generation resource* and *dispatchable load* at bus  $b \in B$ , where:

23.4.1.1.1  $L30RP_{h,b}^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for *thirty-minute operating reserve*;

23.4.1.1.2  $P30RRef_h^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for *thirty-minute operating reserve* at the *reference bus*;

23.4.1.1.3  $P30RCong_{h,b}^p$  designates the Pass  $p$  hour  $h$  congestion component for *thirty-minute operating reserve*;

23.4.1.1.4  $L10NP_{h,b}^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for non-synchronized *ten-minute operating reserve*;



23.4.1.1.5  $P10NRef_h^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for non-synchronized *ten-minute operating reserve* at the *reference bus*;

23.4.1.1.6  $P10NCong_{h,b}^p$  designates the Pass  $p$  hour  $h$  congestion component for non-synchronized *ten-minute operating reserve*;

23.4.1.1.7  $L10SP_{h,b}^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for synchronized *ten-minute operating reserve*;

23.4.1.1.8  $P10SRef_h^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for synchronized *ten-minute operating reserve* at the *reference bus*;

23.4.1.1.9  $P10SCong_{h,b}^p$  designates the Pass  $p$  hour  $h$  congestion component for synchronized *ten-minute operating reserve*; and

23.4.1.1.10  $ORREG_b \subseteq ORREG$  designates the subset of  $ORREG$  consisting of regions that include bus  $b$ .

23.4.1.2 The *day-ahead market calculation engine* shall calculate an initial *locational marginal price*, a *locational marginal price* at the *reference bus*, and congestion components for Pass  $p$  for a *delivery point* associated with the *dispatchable generation resource* and *dispatchable load* at bus  $b \in B$  in hour  $h \in \{1, \dots, 24\}$ , for each class of *operating reserve*, as follows:

$$InitL30RP_{h,b}^p = InitP30RRef_h^p + InitP30RCong_{h,b}^p$$

where

$$InitP30RRef_h^p = SP30R_h^p$$

and

$$\begin{aligned} InitP30RCong_{h,b}^p &= \sum_{r \in ORREG_b} SPREGMin30R_{h,r}^p \\ &+ \sum_{r \in ORREG_b} SPREGMax30R_{h,r}^p \end{aligned}$$

$$InitL10NP_{h,b}^p = InitP10NRef_h^p + InitP10NCong_{h,b}^p$$

where

$$InitP10NRef_h^p = SP10R_h^p + SP30R_h^p$$

and

$$\begin{aligned} InitP10NCong_{h,b}^p &= \sum_{r \in ORREG_b} (SPREGMin10R_{h,r}^p \\ &\quad + SPREGMin30R_{h,r}^p) \\ &\quad + \sum_{r \in ORREG_b} (SPREGMax10R_{h,r}^p \\ &\quad + SPREGMax30R_{h,r}^p) \end{aligned}$$

$$InitL10SP_{h,b}^p = InitP10SRef_h^p + InitP10SCong_{h,b}^p$$

where

$$InitP10SRef_h^p = SP10S_h^p + SP10R_h^p + SP30R_h^p$$

and

$$\begin{aligned} InitP10SCong_{h,b}^p &= \sum_{r \in ORREG_b} (SPREGMin10R_{h,r}^p \\ &\quad + SPREGMin30R_{h,r}^p) \\ &\quad + \sum_{r \in ORREG_b} (SPREGMax10R_{h,r}^p \\ &\quad + SPREGMax30R_{h,r}^p) \end{aligned}$$

23.4.1.3 If the initial *locational marginal price* at the *reference bus* ( $InitP30RRef_h^p$ ,  $InitP10NRef_h^p$ , or  $InitP10SRef_h^p$ ) is not within the *settlement bounds* ( $ORPrCFlr$ ,  $ORPrCCeil$ ), then the *day-ahead market calculation engine* shall modify the initial *locational marginal prices* at the *reference bus* for each class of *operating reserve* as follows:

If  $InitP30RRef_h^p > ORPrCCeil$ ,  $P30RRef_h^p = ORPrCCeil$ ;

If  $InitP30RRef_h^p < ORPrCFlr$ ,  $P30RRef_h^p = ORPrCFlr$ ; Otherwise,  $P30RRef_h^p = InitP30RRef_h^p$ .

If  $InitP10NRef_h^p > ORPrCCeil$ ,  $P10NRef_h^p = ORPrCCeil$ ;

If  $InitP10NRef_h^p < ORPrcFlr$ ,  $P10NRef_h^p = ORPrcFlr$ ;  
 Otherwise,  $P10NRef_h^p = InitP10NRef_h^p$ .

If  $InitP10SRef_h^p > ORPrcCeil$ ,  $P10SRef_h^p = ORPrcCeil$ ;

If  $InitP10SRef_h^p < ORPrcFlr$ ,  $P10SRef_h^p = ORPrcFlr$ ;  
 Otherwise,  $P10SRef_h^p = InitP10SRef_h^p$

23.4.1.4 If the initial *locational marginal price* ( $InitL30RP_{h,b}^p$ ,  $InitL10NP_{h,b}^p$ , or  $InitL10SP_{h,b}^p$ ) is not within the *settlement* bounds ( $ORPrcFlr$ ,  $ORPrcCeil$ ), then the *day-ahead market calculation engine* shall modify the initial *locational marginal price* for each class of *operating reserve* as follows:

If  $InitL30RP_{h,b}^p > ORPrcCeil$ ,  $L30RP_{h,b}^p = ORPrcCeil$ ;

If  $InitL30RP_{h,b}^p < ORPrcFlr$ ,  $L30RP_{h,b}^p = ORPrcFlr$ ;  
 Otherwise,  $L30RP_{h,b}^p = InitL30RP_{h,b}^p$ .

If  $InitL10NP_{h,b}^p > ORPrcCeil$ ,  $L10NP_{h,b}^p = ORPrcCeil$ ;

If  $InitL10NP_{h,b}^p < ORPrcFlr$ ,  $L10NP_{h,b}^p = ORPrcFlr$ ;  
 Otherwise,  $L10NP_{h,b}^p = InitL10NP_{h,b}^p$ .

If  $InitL10SP_{h,b}^p > ORPrcCeil$ ,  $L10SP_{h,b}^p = ORPrcCeil$ ;

If  $InitL10SP_{h,b}^p < ORPrcFlr$ ,  $L10SP_{h,b}^p = ORPrcFlr$ ;  
 Otherwise,  $L10SP_{h,b}^p = InitL10SP_{h,b}^p$

23.4.1.5 If the initial *locational marginal price* ( $InitL30RP_{h,b}^p$ ,  $InitL10NP_{h,b}^p$ , or  $InitL10SP_{h,b}^p$ ) is not within the *settlement* bounds ( $ORPrcFlr$ ,  $ORPrcCeil$ ), then the *day-ahead market calculation engine* shall modify the congestion component for each class of *operating reserve*, as follows:

Set  $P30RCong_{h,b}^p = L30RP_{h,b}^p - P30RRef_h^p$ ;

Set  $P10NCong_{h,b}^p = L10NP_{h,b}^p - P10NRef_h^p$ ; and

Set  $P10SCong_{h,b}^p = L10SP_{h,b}^p - P10SRef_h^p$ .

## 23.4.2 Operating Reserve Locational Marginal Prices for Intertie Metering Points

- 23.4.2.1 The *day-ahead market calculation engine* shall calculate a *locational marginal price* and components for *operating reserve* for each Pass  $p \in \{1,3\}$  and hour  $h \in \{1, \dots, 24\}$  for *intertie zone* bus  $d \in D$ , where:
- 23.4.2.1.1  $ExtL30RP_{h,d}^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for *thirty-minute operating reserve*;
  - 23.4.2.1.2  $P30RRef_h^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for *thirty-minute operating reserve* at the *reference bus*;
  - 23.4.2.1.3  $P30RIntCong_{h,d}^p$  designates the Pass  $p$  hour  $h$  internal congestion component for *thirty-minute operating reserve*;
  - 23.4.2.1.4  $P30RExtCong_{h,d}^p$  designates the Pass  $p$  hour  $h$  *intertie* congestion component for *thirty-minute operating reserve*;
  - 23.4.2.1.5  $ExtL10NP_{h,d}^p$  designates the Pass  $p$  hour  $h$  non-synchronized *ten-minute operating reserve price*;
  - 23.4.2.1.6  $P10NRef_h^p$  designates the Pass  $p$  hour  $h$  *locational marginal price* for non-synchronized *ten-minute operating reserve* at the *reference bus*;
  - 23.4.2.1.7  $P10NIntCong_{h,d}^p$  designates the Pass  $p$  hour  $h$  internal congestion component for non-synchronized *ten-minute operating reserve*;
  - 23.4.2.1.8  $P10NExtCong_{h,d}^p$  designates the Pass  $p$  hour  $h$  *intertie* congestion component for non-synchronized *ten-minute operating reserve*; and
  - 23.4.2.1.9  $ORREG_d \subseteq ORREG$  designates the subset of  $ORREG$  consisting of regions that include bus  $d$ .
- 23.4.2.2 The *day-ahead market calculation engine* shall calculate an initial *locational marginal price*, a *locational marginal price* at the *reference bus*, an internal congestion component and an *intertie* congestion component for Pass  $p$  at *intertie zone* bus  $d \in D_a$  in *intertie zone*  $a \in A$

in hour  $h \in \{1, \dots, 24\}$ , for each class of *operating reserve*, subject to sections 23.4.2.5 and 23.4.2.6, as follows:

$$\begin{aligned} InitExtL30RP_{h,d}^p &= InitP30RRef_h^p + InitP30RIntCong_{h,d}^p \\ &\quad + InitP30RExtCong_{h,d}^p \end{aligned}$$

where

$$InitP30RRef_h^p = SP30R_h^p;$$

$$\begin{aligned} InitP30RIntCong_{h,d}^p &= \sum_{r \in ORREG_d} SPREGMin30R_{h,r}^p \\ &\quad + \sum_{r \in ORREG_d} SPREGMax30R_{h,r}^p ; \end{aligned}$$

and

$$\begin{aligned} InitP30RExtCong_{h,d}^p &= \sum_{z \in Z_{Sch}} 0.5 \cdot (EnCoeff_{a,z} + 1) \cdot SPExtT_{h,z}^p \end{aligned}$$

$$\begin{aligned}
InitExtL10NP_{h,d}^p &= InitP10NRef_h^p + InitP10NIntCong_{h,d}^p \\
&+ InitP10NExtCong_{h,d}^p
\end{aligned}$$

where

$$InitP10NRef_h^p = SP10R_h^p + SP30R_h^p;$$

$$\begin{aligned}
InitP10NIntCong_{h,d}^p &= \sum_{r \in ORREG_d} (SPREGMin10R_{h,r}^p \\
&+ SPREGMin30R_{h,r}^p) \\
&+ \sum_{r \in ORREG_d} (SPREGMax10R_{h,r}^p \\
&+ SPREGMax30R_{h,r}^p)
\end{aligned}$$

and

$$\begin{aligned}
InitP10NExtCong_{h,d}^p &= \sum_{z \in Z_{Sch}} 0.5 \cdot (EnCoeff_{a,z} + 1) \cdot SPExtT_{h,z}^p
\end{aligned}$$

23.4.2.3 If the initial *locational marginal price* ( $InitExtL30RP_{h,b}^p$ ) is not within the *settlement bounds* ( $ORPrCflr, ORPrCceil$ ), then the *day-ahead market calculation engine* shall modify the initial *locational marginal price*, the *locational marginal price* at the *reference bus*, and the external congestion component for *thirty-minute operating reserve* as follows:

$$IntL30R = InitP30RRef_h^p + InitP30RIntCong_{h,d}^p$$

If  $InitP30RRef_h^p > ORPrCceil$ ,  $P30RRef_h^p = ORPrCceil$ ;

If  $InitP30RRef_h^p < ORPrCflr$ ,  $P30RRef_h^p = ORPrCflr$ ;

Otherwise,  $P30RRef_h^p = InitP30RRef_h^p$ ;

Set  $P30RIntCong_{h,d}^p = ExtL30RP_{h,d}^p - P30RRef_h^p$

If  $InitExtL30RP_{h,b}^p > ORPrCceil$ ,  $ExtL30RP_{h,b}^p = ORPrCceil$ ;

If  $InitExtL30RP_{h,b}^p < ORPrCflr$ ,  $ExtL30RP_{h,b}^p = ORPrCflr$ ;

Otherwise,  $ExtL30RP_{h,b}^p = InitExtL30RP_{h,b}^p$ ; and

Set  $P30RExtCong_{h,d}^p = ExtL30RP_{h,b}^p - P30RRef_h^p - P30RIntCong_{h,d}^p$

- 23.4.2.4 If the initial *locational marginal price* ( $InitExtL10NP_{h,b}^p$ ) is not within the *settlement bounds* ( $ORPrCFlr, ORPrCCeil$ ), then the *day-ahead market calculation engine* shall modify the initial *locational marginal price*, the *locational marginal price* at the reference bus, and the external congestion component for *ten-minute operating reserve* as follows:

$$IntL10N = InitP10NRef_h^p + InitP10NIntCong_{h,d}^p$$

If  $InitP10NRef_h^p > ORPrCCeil$ ,  $P10NRef_h^p = ORPrCCeil$ ;

If  $InitP10NRef_h^p < ORPrCFlr$ ,  $P10NRef_h^p = ORPrCFlr$ ;

Otherwise,  $P10NRef_h^p = InitP10NRef_h^p$ ;

Set  $P10NCong_{h,b}^p = L10NP_{h,b}^p - P10NRef_h^p$

If  $InitExtL10NP_{h,b}^p > ORPrCCeil$ ,  $ExtL10NP_{h,b}^p = ORPrCCeil$ ;

If  $InitExtL10NP_{h,b}^p < ORPrCFlr$ ,  $ExtL10NP_{h,b}^p = ORPrCFlr$ ;

Otherwise,  $ExtL10NP_{h,b}^p = InitExtL10NP_{h,b}^p$ ; and

Set  $P10NExtCong_{h,d}^p = ExtL10NP_{h,b}^p - P10NRef_h^p - P10NIntCong_{h,d}^p$

- 23.4.2.5 The *locational marginal price* calculated by the *day-ahead market calculation engine* shall be the same for all *boundary entity resource* buses at the same *intertie zone*. Reserve imports associated with the same *boundary entity resource* bus, but specified as occurring at a different *intertie zone*, subject to phase shifter operation, shall be modelled as flowing across independent paths. Pricing of these reserve imports shall utilize shadow prices associated with *intertie* limits and regional minimum and maximum *operating reserve* requirements applicable to the path associated to the relevant *intertie zone*.
- 23.4.2.6 When an *intertie zone* is out-of-service, the *intertie* limits for that *intertie zone* will be set to zero and all *boundary entity resources* for that *intertie zone* will receive a zero schedule for *energy and operating reserve* and the *intertie operating reserve* prices shall be set equal to the *locational marginal price* for the *reference bus* for that class of *operating reserve* plus the applicable shadow prices associated with regional minimum and maximum *operating reserve* requirements.

## 23.5 Pricing for Islanded Nodes

23.5.1 For *non-quick start resources* that are not connected to the *main island*, the *day-ahead market calculation engine* may use the following reconnection logic where enabled by the *IESO* in the order set out below to calculate the *locational marginal prices for energy*:

23.5.1.1 Determine the connection paths over open switches that connect the *non-quick start resource* to the *main island*;

23.5.1.2 Determine the priority rating for each connection path identified based on a weighted sum of the base voltage over all open switches used by the reconnection path and the MW ratings of the newly connected branches; and

23.5.1.3 Select the reconnection path with the highest priority rating, breaking ties arbitrarily.

23.5.2 For all (i) *resources* other than those specified in section 23.5.1 not connected to the *main island*; (ii) *non-quick start resources* where a price was not able to be determined in accordance with section 23.5.1; the *day-ahead market calculation engine* shall use the following logic in the order set out below to calculate *locational marginal prices*, using a node-level and *facility*-level substitution list determined by the *IESO*:

23.5.2.1 Use the *locational marginal price for energy* at a node in the node-level substitution list where defined and enabled by the *IESO*, provided such node is connected to the *main island*;

23.5.2.2 If no such nodes are identified, use the average *locational marginal price for energy* of all nodes at the same voltage level within the same *facility* that are connected to the *main island*;

23.5.2.3 If no such nodes are identified, use the average *locational marginal price for energy* of all nodes within the same *facility* that are connected to the *main island*;

23.5.2.4 If no such nodes are identified, use the average *locational marginal price for energy* of all nodes from another *facility* that is connected to the *main island*, as determined by the *facility*-level substitution list where defined and enabled by the *IESO*; and

23.5.2.5 If a price is unable to be determined in accordance with sections 23.5.2.1 through 23.5.2.4, use the *locational marginal price for energy* for the *reference bus*.



**Note: The existing Appendix 7.5A- The DACP Calculation Engine Process has been deleted in its entirety and replaced with the new Appendix 7.5A- The Pre-Dispatch Calculation Engine Process**

## Appendix 7.5A – The Pre-Dispatch Calculation Engine Process

### 1.1 Purpose

- 1.1.1 This appendix describes the process used by the *pre-dispatch calculation engine* to determine commitments, schedules, and prices for the pre-dispatch look-ahead period.

## 2 Pre-Dispatch Calculation Engine

### 2.1 Pre-Dispatch Look-Ahead Period

- 2.1.1 The pre-dispatch look-ahead period is the time horizon considered in the multi-hour optimization. The pre-dispatch look-ahead period changes depending on when the *pre-dispatch calculation engine* runs:
  - 2.1.1.1 for the *pre-dispatch calculation engine* runs from 00:00 EST to 19:00 EST in the current *dispatch day*, the pre-dispatch look-ahead period consists of the remaining hours of the current *dispatch day*, and
  - 2.1.1.2 for the *pre-dispatch calculation engine* runs from 20:00 EST to 23:00 EST in the current *dispatch day*, the pre-dispatch look-ahead period consists of the remaining hours of the current *dispatch day* in addition to all hours in the next *dispatch day*.

### 2.2 Pre-Dispatch Calculation Engine Pass

- 2.2.1 The *pre-dispatch calculation engine* shall execute one pass, Pass 1, the Pre-Dispatch Scheduling Process Pass, in accordance with section 7, to produce *pre-dispatch schedules*, commitments and *locational marginal prices*.

### 3 Information Used by the Pre-Dispatch Calculation Engine

3.1.1 The *pre-dispatch calculation engine* shall use the information in section 3A.1 of Chapter 7.

### 4 Sets, Indices and Parameters Used in the Pre-Dispatch Calculation Engine

#### 4.1 Fundamental Sets and Indices

- 4.1.1  $A$  designates the set of all *intertie zones*;
- 4.1.2  $B$  designates the set of buses identifying all *dispatchable* and non-*dispatchable resources* within Ontario;
- 4.1.3  $B^{DG} \subseteq B$  designates the set of buses identifying *dispatchable generation resources*;
- 4.1.4  $B^{DL} \subseteq B$  designates the set of buses identifying *dispatchable loads*;
- 4.1.5  $B^{ELR} \subseteq B^{DG}$  designates the subset of buses identifying *energy limited resources*;
- 4.1.6  $B^{HDR} \subseteq B$  designates the set of buses identifying *hourly demand response resources*;
- 4.1.7  $B^{HE} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable hydroelectric generation resources*;
- 4.1.8  $\wp(B^{HE})$  designates the set of all subsets of the set  $B^{HE}$ ;
- 4.1.9  $B_{up}^{HE} \subseteq \wp(B^{HE})$  designates the set of buses identifying all upstream *dispatchable hydroelectric generation resources* with a registered *forebay* that are linked via *time lag* and *MWh ratio dispatch data* with downstream *dispatchable hydroelectric generation resources* with a registered *forebay*;
- 4.1.10  $B_{dn}^{HE} \subseteq \wp(B^{HE})$  designates the set of buses identifying all downstream *dispatchable hydroelectric generation resources* with a registered

*forebay* that are linked via *time lag* and *MWh ratio dispatch data* with upstream *dispatchable hydroelectric generation resources* with a registered *forebay*;

- 4.1.11  $B_s^{HE} \subseteq B^{HE}$  designates the subset of buses identifying *dispatchable hydroelectric generation resources* in set  $s \in SHE$ ;
- 4.1.12  $B^{NDG} \subseteq B$  designates the set of buses identifying *non-dispatchable generation resources*;
- 4.1.13  $B^{NO10DF} \subseteq B^{PSU}$  designates the subset of buses identifying *pseudo-units* that cannot provide *ten-minute operating reserve* from the duct firing region;
- 4.1.14  $B^{NQS} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable non-quick start resources*;
- 4.1.15  $B^{PSU} \subseteq B^{NQS}$  designates the subset of buses identifying *pseudo-units*;
- 4.1.16  $B_r^{REG} \subseteq B$  designates the set of internal buses in *operating reserve region*  $r \in ORREG$ ;
- 4.1.17  $B_p^{ST} \subseteq B^{PSU}$  designates the subset of buses identifying *pseudo-units* with a share of steam turbine *resource*  $p \in PST$ ;
- 4.1.18  $B^{VG} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable variable generation resources*;
- 4.1.19  $C$  designates the set of contingencies that shall be considered in the *security assessment function*;
- 4.1.20  $D$  designates the set of buses outside Ontario corresponding to imports and exports at *intertie zones*;
- 4.1.21  $DAYS$  designates the set of days in the look-ahead period. If the look-ahead period spans one day, then  $DAYS = \{tod\}$ . If the look-ahead period spans two days, then  $DAYS = \{tod, tom\}$ ;
- 4.1.22  $D_r^{REG} \subseteq D$  designates the set of *intertie zone* buses identifying *boundary entity resources* in *operating reserve region*  $r \in ORREG$ ;
- 4.1.23  $DX \subseteq D$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids*;

- 4.1.24  $DI \subseteq D$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers*;
- 4.1.25  $D_a \subseteq D$  designates the set of all buses identifying *boundary entity resources* in *intertie zone*  $a \in A$ ;
- 4.1.26  $DI_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers* in *intertie zone*  $a \in A$ ;
- 4.1.27  $DI_t^{CAPEX} \subseteq DI$  designates the *intertie zone* source buses identifying import *offers* flagged as capacity imports in time-step  $t \in \{4, \dots, n_{LAP}\}$ ;
- 4.1.28  $DI_t^{EM} \subseteq DI$  designates the *intertie zone* buses corresponding to *emergency energy* import transactions for time-step  $t \in TS$ ;
- 4.1.29  $DI_t^{EMNS} \subseteq DI_t^{EM}$  designates the *intertie zone* buses corresponding to *emergency energy* import transactions that do not support *emergency energy* export transactions in time-step  $t \in TS$ ;
- 4.1.30  $DI_t^{INP} \subseteq DI$  designates the *intertie zone* buses corresponding to inadvertent *energy* payback import transactions for time-step  $t \in TS$ ;
- 4.1.31  $DX_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids* in *intertie zone*  $a \in A$ ;
- 4.1.32  $DX_t^{CAPEX} \subseteq DX$  designates the *intertie zone* sink buses identifying export *bids* flagged as *capacity exports* in time-step  $t$ ;
- 4.1.33  $DX_t^{INP} \subseteq DX$  designates the *intertie zone* buses corresponding to inadvertent *energy* payback export transactions for time-step  $t \in TS$ ;
- 4.1.34  $DX_t^{EM} \subseteq DX$  designates the *intertie zone* buses corresponding to *emergency energy* export transactions for time-step  $t \in TS$ ;
- 4.1.35  $F$  designates the set of *facilities* and groups of *facilities* for which transmission constraints may be identified;
- 4.1.36  $F_t \subseteq F$  designates the set of *facilities* whose pre-contingency limit was violated in time step  $t$  as determined by a preceding *security* assessment function iteration;

- 4.1.37  $F_{tc} \subseteq F$  designates the set of *facilities* whose post-contingency limit for contingency  $c$  is violated in time step  $t$  as determined by a preceding *security* assessment function iteration;
- 4.1.38  $J_{t,b}^E$  designates the set of *bid* laminations for energy at bus  $b \in B \cup DX$  for time-step  $t \in TS$ ;
- 4.1.39  $J_{t,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.40  $J_{t,b}^{10S}$  designates the set of *reference level value* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.41  $J_{t,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B \cup DX$  for time-step  $t \in TS$ ;
- 4.1.42  $J_{t,b}^{10N}$  designates the set of *reference level value* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.43  $J_{t,b}^{30R}$  designates the set of *offer* laminations for *thirty-minute operating reserve offer* at bus  $b \in B \cup DX$  for time-step  $t \in TS$ ;
- 4.1.44  $J_{t,b}^{30R}$  designates the set of *reference level value* laminations for *thirty-minute operating reserve* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.45  $K_{t,b}^{DF} \subseteq K_{t,b}^E$  designates the set of *offer* laminations for *energy* corresponding to the duct firing region of a *pseudo-unit* at bus  $b \in B^{PSU}$  for time-step  $t \in TS$ ;
- 4.1.46  $K_{t,b}^{DR} \subseteq K_{t,b}^E$  designates the set of *offer* laminations for *energy* corresponding to the *dispatchable* region of a *pseudo-unit* at bus  $b \in B^{PSU}$  for time-step  $t \in TS$ ;
- 4.1.47  $K_{t,b}^E$  designates the set of *offer* laminations for *energy* at bus  $b \in B \cup DI$  for time-step  $t \in TS$ ;
- 4.1.48  $K_{t,b}^E$  designates the set of *reference level value* laminations for *energy* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.49  $K_{t,b}^{LTMPL}$  designates the set of *offer* laminations for *energy* quantities up to the *minimum loading point* for a *non-quick start resource* at bus  $b \in B^{NQS}$  for time-step  $t \in TS$ ;

- 4.1.50  $K_{t,b}^{LTMLP}$  designates the set of *reference level value* laminations for *energy* quantities up to the *minimum loading point reference level* for a *non-quick start resource* at bus  $b \in B^{NQS}$  for time-step  $t \in TS$ ;
- 4.1.51  $K_{t,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.52  $K_{t,b}^{10S}$  designates the set of *reference level value* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.53  $K_{t,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B \cup DI$  for time-step  $t \in TS$ ;
- 4.1.54  $K_{t,b}^{10N}$  designates the set of *reference level value* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.55  $K_{t,b}^{30R}$  designates the set of *offer* laminations for *thirty-minute operating reserve* at bus  $b \in B \cup DI$  for time-step  $t \in TS$ ;
- 4.1.56  $K_{t,b}^{30R}$  designates the set of *reference level value* laminations for *thirty-minute operating reserve* at bus  $b \in B$  for time-step  $t \in TS$ ;
- 4.1.57  $L$  designates the set of buses where the *locational marginal prices* represent prices for *delivery points* associated with *non-dispatchable generation resources* and *dispatchable generation resources*, *dispatchable loads*, *hourly demand response resources*, *price responsive loads* and *non-dispatchable loads*;
- 4.1.58  $L_y^{NDL} \subseteq L$ , designates the buses contributing to the zonal price for *non-dispatchable load zone*  $y \in Y$ ;
- 4.1.59  $L_m^{VIRT} \subseteq L$ , designates the buses contributing to the *virtual zonal price* for *virtual transaction zone*  $m \in M$ ;
- 4.1.60  $M$  designates the set of *virtual transaction zones*;
- 4.1.61  $NCA$  designates the set of *narrow constrained areas*;
- 4.1.62  $DCA$  designates the set of *dynamic constrained areas*;
- 4.1.63  $BCA$  designates the set of *broad constrained areas*;

- 4.1.64  $PST$  designates the set of steam turbine *resources offered* as part of a *pseudo-unit*;
- 4.1.65  $SHE$  designates the set indexing the sets of *dispatchable* hydroelectric *generation resources* with a *maximum daily energy limit* or a *minimum daily energy limit* or both for a registered *forebay*;
- 4.1.66  $THERM = \{COLD, WARM, HOT\}$  designates the set of *thermal states* for *non-quick start resources*;
- 4.1.67  $TS = \{2, \dots, n_{LAP}\}$  designates the set of all time-steps in the look-ahead period that are included in the *pre-dispatch calculation engine* optimization, where  $n_{LAP}$  designates the number of time-steps in the look-ahead period;
- 4.1.68  $TS_{tod} \subseteq TS$  designates the time-steps in the look-ahead period that are part of the current *dispatch day*;
- 4.1.69  $TS_{tom} \subseteq TS$  designates the time-steps in the look-ahead period that are part of the next *dispatch day*;
- 4.1.70  $TSC_b \subseteq TS$  designates the set of time-steps representing the first hour of a *day-ahead operational commitment* for the *resource* at bus  $b \in B$ ;
- 4.1.71  $t_{tom} \in TS_{tom}$  designates the first time-step of the next *dispatch day*;
- 4.1.72  $Y$  designates the *non-dispatchable load* zones in Ontario; and
- 4.1.73  $Z_{Sch}$  designates the set of all *inertie* limit constraints.

## 4.2 Market Participant Data Parameters

- 4.2.1 With respect to a *non-dispatchable generation resource* identified by bus  $b \in B^{NDG}$ :
  - 4.2.1.1  $QNDG_{t,b,k}$  designates the maximum incremental quantity of *energy* that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,b}^E$ ; and
  - 4.2.1.2  $PNDG_{t,b,k}$  designates the price for the maximum incremental quantity of *energy* in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,b}^E$ .

- 4.2.2 With respect to a *dispatchable generation resource* identified by bus  $b \in B^{DG}$ :
- 4.2.2.1  $MinQDG_{q,b}$  designates the *minimum loading point* for day  $q \in DAYS$ ;
  - 4.2.2.2  $QDG_{t,b,k}$  designates the maximum incremental quantity of *energy* above the *minimum loading point* that may be scheduled in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^E$ ;
  - 4.2.2.3  $PDG_{t,b,k}$  designates the price for the maximum incremental quantity of *energy* in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^E$ ;
  - 4.2.2.4  $Q10SDG_{t,b,k}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^{10S}$ ;
  - 4.2.2.5  $P10SDG_{t,b,k}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^{10S}$ ;
  - 4.2.2.6  $Q10NDG_{t,b,k}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^{10N}$ ;
  - 4.2.2.7  $P10NDG_{t,b,k}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^{10N}$ ;
  - 4.2.2.8  $Q30RDG_{t,b,k}$  designates the maximum incremental quantity of *thirty-minute operating reserve* in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^{30R}$ ;
  - 4.2.2.9  $P30RDG_{t,b,k}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^{30R}$ ;
  - 4.2.2.10  $ORRDG_b$  designates the maximum *operating reserve* ramp rate in MW per minute;
  - 4.2.2.11  $NumRRDG_{t,b}$  designates the number of ramp rates provided in time-step  $t \in TS$ ;
  - 4.2.2.12  $RmpRngMaxDG_{t,b,w}$  for  $w \in \{1, \dots, NumRRDG_{t,b}\}$  designates the  $w^{th}$  ramp rate break point in time-step  $t \in TS$ ;



- 4.2.2.13  $URRDG_{t,b,w}$  for  $w \in \{1,...,NumRRDG_{t,b}\}$  designates the ramp rate in MW per minute at which the *resource* can increase the amount of *energy* it supplies in time-step  $t \in TS$  while operating in the range between  $RmpRngMaxDG_{t,b,w-1}$  and  $RmpRngMaxDG_{t,b,w}$  where  $RmpRngMaxDG_{t,b,0}$  shall be equal to zero;
- 4.2.2.14  $DRRDG_{t,b,w}$  for  $w \in \{1,...,NumRRDG_{t,b}\}$  designates the ramp rate in MW per minute at which the *resource* can decrease the amount of *energy* it supplies in time-step  $t \in TS$  while operating in the range between  $RmpRngMaxDG_{t,b,w-1}$  and  $RmpRngMaxDG_{t,b,w}$  where  $RmpRngMaxDG_{t,b,0}$  shall be equal to zero;
- 4.2.2.15  $RLP30R_{t,b}$  designates the *reserve loading point* for *thirty-minute operating reserve* in time-step  $t \in TS$ ; and
- 4.2.2.16  $RLP10S_{t,b}$  designates the *reserve loading point* for *synchronized ten-minute operating reserve* in time-step  $t \in TS$ .
- 4.2.3 With respect to a *dispatchable non-quick start resource* identified by bus  $b \in B^{NQS}$  :
- 4.2.3.1  $LT_{q,b}^m$  designates the *lead time* in *dispatch day*  $q \in DAYS$  for *thermal state*  $m \in THERM$ ;
- 4.2.3.2  $MGODG_{t,b}$  designates the minimum generation cost to operate at *minimum loading point* in time-step  $t \in TS$ . This parameter is calculated as follows:
- $$MGODG_{t,b} = SNL_{t,b} + \sum_{k \in K_{t,b}^{LTMLP}} PLTMLP_{t,b,k} \cdot QLTMLP_{t,b,k}.$$
- 4.2.3.3  $MGBRTDG_{q,b}$  designates the *minimum generation block run-time* within *dispatch day*  $q \in DAYS$ ;
- 4.2.3.4  $MaxStartsDG_{q,b}$  designates the *maximum number of starts per day* within *dispatch day*  $q \in DAYS$ ;
- 4.2.3.5  $MGBDTDG_{q,b}^{HOT}$  designates the *minimum generation block down-time* for a hot *thermal state* within *dispatch day*  $q \in DAYS$ ;
- 4.2.3.6  $MGBDTDG_{q,b}^{WARM}$  designates the *minimum generation block down-time* for a warm *thermal state* in *dispatch day*  $q \in DAYS$ ;

- 4.2.3.7  $MGBD TDG_{q,b}^{COLD}$  designates the *minimum generation block down-time* for a cold *thermal state* in *dispatch day*  $q \in DAYS$ ;
- 4.2.3.8  $PLTMLP_{t,b,k}$  designates the price for the maximum incremental quantity of *energy* up to the *minimum loading point* that may be scheduled in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^{LTMLP}$ ;
- 4.2.3.9  $QLTMLP_{t,b,k}$  designates the maximum incremental quantity of *energy* up to the *minimum loading point* that may be scheduled in time-step  $t \in TS$  in association with *offer lamination*  $k \in K_{t,b}^{LTMLP}$ ;
- 4.2.3.10  $RampE_{q,b,w}^m$  designates the *ramp up energy to minimum loading point* in *dispatch day*  $q \in DAYS$  for  $w \in \{1, \dots, RampHrs_{q,b}^m\}$  and *thermal state*  $m \in THERM$ ;
- 4.2.3.11  $RampHrs_{q,b}^m$  designates the *ramp hours to minimum loading point* in *dispatch day*  $q \in DAYS$  for *thermal state*  $m \in THERM$ ;
- 4.2.3.12  $SNL_{t,b}$  designates the *speed no-load offer* in time-step  $t \in TS$ ;
- 4.2.3.13  $SUDG_{t,b}^m$  designates the *start-up offer* in time-step  $t \in TS$  for *thermal state*  $m \in THERM$ ;
- 4.2.3.14  $SUDG_{t,b}^{DAM}$  designates the *start-up offer* used to evaluate the *day-ahead operational commitment* starting in time-step  $t \in TSC_b$ ;
- 4.2.3.15  $SUAdjDG_{t,b}^m$  designates the *start-up offer* that the optimization function will evaluate in time-step  $t \in TS$  under *thermal state*  $m$ .
- 4.2.4 With respect to an *energy limited resource* identified by bus  $b \in B^{ELR}$ :
- 4.2.4.1  $MaxDEL_{q,b}$  designates the *maximum daily energy limit* for a single *resource* with or without a registered *forebay* within *dispatch day*  $q \in DAYS$ .
- 4.2.5 With respect to a *dispatchable hydroelectric generation resource* identified by bus  $b \in B^{HE}$ :
- 4.2.5.1  $MinHMR_{t,b}$  designates the *hourly must-run value* in time-step  $t \in TS$ ;
- 4.2.5.2  $MinHO_{t,b}$  designates the *minimum hourly output* in time-step  $t \in TS$ ;

- 4.2.5.3  $MinDEL_{q,b}$  designates the *minimum daily energy limit* for a single *resource* with or without a registered *forebay* within *dispatch day*  $q \in DAYS$ ;
- 4.2.5.4  $MaxStartsHE_{q,b}$  designates the *maximum number of starts per day* within *dispatch day*  $q \in DAYS$ ;
- 4.2.5.5  $StartMW_{b,i}$  for  $i \in \{1, \dots, NStartMW_b\}$  designates the *start indication value* for measuring *maximum number of starts per day*; a start is counted between time-step  $t$  and  $(t + 1)$  if the schedule increases from below  $StartMW_{b,i}$  to at or above  $StartMW_{b,i}$  and
- 4.2.5.6  $(ForL_{q,b,i}, ForU_{q,b,i})$  for  $i \in \{1, \dots, NFor_{q,b}\}$  designates the lower and upper limits of the *forbidden regions* and indicate that the *resource* cannot be scheduled between  $ForL_{q,b,i}$  and  $ForU_{q,b,i}$  for all  $i \in \{1, \dots, NFor_{q,b}\}$  within *dispatch day*  $q \in DAYS$ .
- 4.2.6 With respect to multiple *dispatchable hydroelectric generation resources* with a registered *forebay*:
- 4.2.6.1  $MaxSDEL_{q,s}$  designates the *maximum daily energy limit* shared by all *dispatchable hydroelectric generation resources* in set  $s \in SHE$  for *dispatch day*  $q \in DAYS$ ; and
- 4.2.6.2  $MinSDEL_{q,s}$  designates the *minimum daily energy limit* shared by all *dispatchable hydroelectric generation resources* in set  $s \in SHE$  within *dispatch day*  $q \in DAYS$ .
- 4.2.7 With respect to a *dispatchable hydroelectric generation resource* for which a *MWh ratio* was respected:
- 4.2.7.1  $LNK_q \subseteq B_{up}^{HE} \times B_{dn}^{HE}$  designates the set of linked *dispatchable hydroelectric generation resources* for *dispatch day*  $q \in DAYS$ , where  $LNK_q$  designates a set with elements of the form  $(b_1, b_2)$  where  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ ;
- 4.2.7.2  $Lag_{q,b_1,b_2} \in \{0, \dots, 23\}$  designates the *time lag* in hours between upstream *dispatchable hydroelectric generation resources*  $b_1 \in B_{up}^{HE}$  and downstream *dispatchable hydroelectric generation resources*  $b_2 \in B_{dn}^{HE}$  for  $(b_1, b_2) \in LNK_q$  for *dispatch day*  $q \in DAYS$ ; and
- 4.2.7.3  $MWhRatio_{q,b_1,b_2}$  designates the *MWh ratio* between upstream *dispatchable hydroelectric generation resources*  $b_1 \in B_{up}^{HE}$  and

downstream *dispatchable* hydroelectric *generation resources*  $b_2 \in B_{dn}^{HE}$   
for  $(b_1, b_2) \in LNK_q$  for dispatch day  $q \in DAYS$ .

4.2.8 With respect to a *pseudo-unit* identified by bus  $b \in B^{PSU}$ :

- 4.2.8.1  $STShareMLP_b$  designates the steam turbine *resource's* share of the *minimum loading point* region;
- 4.2.8.2  $STShareDR_b$  designates the steam turbine *resource's* share of the *dispatchable* region;
- 4.2.8.3  $RampCT_{q,b,w}^m$  designates the quantity of *energy* injected  $w$  hours before the *pseudo-unit* reaches its *minimum loading point* in *dispatch day*  $q \in DAYS$  and *thermal state*  $m \in THERM$  that is attributed to the combustion turbine *resource* for  $w \in \{1, \dots, RampHrs_{q,b}^m\}$ ; and
- 4.2.8.4  $RampST_{q,b,w}^m$  designates the quantity of *energy* injected  $w$  hours before the *pseudo-unit* reaches its *minimum loading point* in *dispatch day*  $q \in DAYS$  for *thermal state*  $m \in THERM$  that is attributed to the steam turbine *resource* for  $w \in \{1, \dots, RampHrs_{q,b}^m\}$ .

4.2.9 With respect to a *dispatchable load* identified by bus  $b \in B^{DL}$ :

- 4.2.9.1  $QDL_{t,b,j}$  designates the maximum incremental quantity of *energy* that may be scheduled in time-step  $t \in TS$  in association with *bid* lamination  $j \in J_{t,b}^E$ ;
- 4.2.9.2  $PDL_{t,b,j}$  designates the price for the maximum incremental quantity of *energy* in time-step  $t \in TS$  in association with *bid* lamination  $j \in J_{t,b}^E$ ;
- 4.2.9.3  $Q10SDL_{t,b,j}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,b}^{10S}$ ;
- 4.2.9.4  $P10SDL_{t,b,j}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,b}^{10S}$ ;
- 4.2.9.5  $Q10NDL_{t,b,j}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,b}^{10N}$ ;

- 4.2.9.6  $P10NDL_{t,b,j}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,b}^{10N}$ ;
- 4.2.9.7  $Q30RDL_{t,b,j}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,b}^{30R}$ ;
- 4.2.9.8  $P30RDL_{t,b,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,b}^{30R}$ ;
- 4.2.9.9  $ORRDL_b$  designates the *operating reserve* ramp rate in MW per minute for reductions in load consumption;
- 4.2.9.10  $NumRRDL_{t,b}$  designates the number of ramp rates provided in time-step  $t \in TS$ ;
- 4.2.9.11  $RmpRngMaxDL_{t,b,w}$  for  $w \in \{1, \dots, NumRRDL_{t,b}\}$  designates the  $w^{th}$  ramp rate break point in time-step  $t \in TS$ ;
- 4.2.9.12  $URRDL_{t,b,w}$  for  $w \in \{1, \dots, NumRRDL_{t,b}\}$  designates the ramp rate in MW per minute at which the *dispatchable load* can increase its amount of *energy* consumption in time-step  $t \in TS$  while operating in the range between  $RmpRngMaxDL_{t,b,w-1}$  and  $RmpRngMaxDL_{t,b,w}$ , where  $RmpRngMaxDL_{t,b,0}$  shall be equal to zero;
- 4.2.9.13  $DRRDL_{t,b,w}$  for  $w \in \{1, \dots, NumRRDL_{t,b}\}$  designates the ramp rate in MW per minute at which the *dispatchable load* can decrease its amount of *energy* consumption in time-step  $t \in TS$  while operating in the range between  $RmpRngMaxDL_{t,b,w-1}$  and  $RmpRngMaxDL_{t,b,w}$ , where  $RmpRngMaxDL_{t,b,0}$  shall be equal to zero; and
- 4.2.9.14  $QDLFIRM_{t,b}$  designates the quantity of *energy* that is *bid* at the *maximum market clearing price* in time-step  $t \in TS$ .
- 4.2.10 With respect to an *hourly demand response resource* identified by bus  $b \in B^{HDR}$ :
- 4.2.10.1  $QHDR_{t,b,j}$  designates an maximum incremental quantity of reduction in *energy* consumption that may be scheduled in time-step  $t \in TS$  in association with *bid* lamination  $j \in J_{t,b}^E$ ;

- 4.2.10.2  $PHDR_{t,b,j}$  designates the price for the maximum incremental quantity of reduction in *energy* consumption for time-step  $t \in TS$  in association with *bid* lamination  $j \in J_{t,b}^E$ ;
  - 4.2.10.3  $URRHDR_b$  designates the maximum rate in MW per minute at which the *hourly demand response resource* can decrease its amount of *energy* consumption; and
  - 4.2.10.4  $DRRHDR_b$  designates the maximum rate in MW per minute at which the *hourly demand response resource* can increase its amount of *energy* consumption.
- 4.2.11 With respect to a *boundary entity resource* import from *intertie zone* bus  $d \in DI$ , where the *locational marginal price* represents the price for the *intertie metering point*:
- 4.2.11.1  $QIG_{t,d,k}$  designates the maximum incremental quantity of *energy* that may be scheduled to import in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^E$ ;
  - 4.2.11.2  $PIG_{t,d,k}$  designates the price for the maximum incremental quantity of *energy* may be scheduled to import in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^E$ ;
  - 4.2.11.3  $Q10NIG_{t,d,k}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^{10N}$ ;
  - 4.2.11.4  $P10NIG_{t,d,k}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^{10N}$ ;
  - 4.2.11.5  $Q30RIG_{t,d,k}$  designates the maximum incremental quantity of *thirty-minute operating reserve* quantity that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^{30R}$ ; and
  - 4.2.11.6  $P30RIG_{t,d,k}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^{30R}$ .

- 4.2.12 With respect to a *boundary entity resource* export to *intertie zone* sink bus  $d \in DX$ , where the *locational marginal price* represents the price for the *intertie metering point*:
- 4.2.12.1  $QXL_{t,d,j}$  designates the maximum incremental quantity of *energy* that may be scheduled to export in time-step  $t \in TS$  in association with *bid* lamination  $j \in J_{t,d}^E$ ;
  - 4.2.12.2  $PXL_{t,d,j}$  designates the price for the maximum incremental quantity of *energy* that may be scheduled to export in time-step  $t \in TS$  in association with *bid* lamination  $j \in J_{t,d}^E$ ;
  - 4.2.12.3  $Q10NXL_{t,d,j}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled to provide in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,d}^{10N}$ ;
  - 4.2.12.4  $P10NXL_{t,d,j}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,d}^{10N}$ ;
  - 4.2.12.5  $Q30RXL_{t,d,j}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled to provide in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,d}^{30R}$ ; and
  - 4.2.12.6  $P30RXL_{t,d,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,d}^{30R}$ .
- 4.2.13 With respect to a *linked wheeling through transaction*:
- 4.2.13.1  $L_t \subseteq DX \times DI$  designates the set of linked *boundary entity resource* import and export buses corresponding to *linked wheeling through transactions*, where  $L_t$  is a set with elements of the form  $(dx, di)$  where  $dx \in DX$  and  $di \in DI$ .

## 4.3 IESO Data Parameters

- 4.3.1 Variable Generation Forecast
- 4.3.1.1  $FG_{t,b}$  designates the *IESO's* centralized *variable generation* forecast for a *variable generation resource* identified by bus  $b \in B^{VG}$  in time-step  $t \in TS$ .

#### 4.3.2 Variable Generation Tie-Breaking

- 4.3.2.1  $NumVG_t$  designates the number of *variable generation resources* in the daily *dispatch* order for time-step  $t \in TS$ ; and
- 4.3.2.2  $TBM_{tb} \in \{1, \dots, NumVG_t\}$  designates the tie-breaking modifier for the *variable generation resource* at bus  $b \in B^{VG}$  for time-step  $t \in TS$ .

#### 4.3.3 Intertie Curtailments

- 4.3.3.1  $ICMaxXL_{t,d}$  designates the maximum limit on the quantity of *energy* scheduled for export to *intertie zone* sink bus  $d \in DX$  and time-step  $t \in TS$  as the result of an *intertie* curtailment;
- 4.3.3.2  $ICMinXL_{t,d}$  designates the minimum limit on the quantity of *energy* scheduled for export to *intertie zone* sink bus  $d \in DX$  and time-step  $t \in TS$  as the result of an *intertie* curtailment;
- 4.3.3.3  $ICMaxIG_{t,d}$  designates the maximum limit on the quantity of *energy* scheduled for import from *intertie zone* source bus  $d \in DI$  and time-step  $t \in TS$  as the result of an *intertie* curtailment;
- 4.3.3.4  $ICMax10NIG_{t,d}$  designates the maximum limit on the quantity of non-synchronized *ten-minute operating reserve* scheduled for import from *intertie zone* source bus  $d \in DI$  and time-step  $t \in TS$  as the result of an *intertie* curtailment;
- 4.3.3.5  $ICMax30RIG_{t,d}$  designates the maximum limit on the quantity of *thirty-minute operating reserve* scheduled for import from *intertie zone* source bus  $d \in DI$  and time-step  $t \in TS$  as the result of an *intertie* curtailment;
- 4.3.3.6  $ICMinIG_{t,d}$  designates the minimum limit on the quantity of *energy* scheduled for import from *intertie zone* source bus  $d \in DI$  and time-step  $t \in TS$  as the result of an *intertie* curtailment;
- 4.3.3.7  $ICMin10NIG_{t,d}$  designates the minimum limit on the quantity of non-synchronized *ten-minute operating reserve* scheduled for import from *intertie zone* source bus  $d \in DI$  and time-step  $t \in TS$  as the result of an *intertie* curtailment; and
- 4.3.3.8  $ICMin30RIG_{t,d}$  designates the minimum limit on the quantity of *thirty-minute operating reserve* scheduled for import from *intertie zone* source bus  $d \in DI$  and time-step  $t \in TS$  as the result of an *intertie* curtailment.



#### 4.3.4 Operating Reserve Requirements

- 4.3.4.1  $TOT10S_t$  designates the synchronized *ten-minute operating reserve* requirement;
- 4.3.4.2  $TOT10R_t$  designates the total *ten-minute operating reserve* requirement;
- 4.3.4.3  $TOT30R_t$  designates the *thirty-minute operating reserve* requirement;
- 4.3.4.4  $ORREG$  designates the set of regions for which regional *operating reserve* limits have been defined;
- 4.3.4.5  $REGMin10R_{t,r}$  designates the minimum requirement for total *ten-minute operating reserve* in region  $r \in ORREG$  in time-step  $t \in TS$ ;
- 4.3.4.6  $REGMin30R_{t,r}$  designates the minimum requirement for *thirty-minute operating reserve* in region  $r \in ORREG$  in time-step  $t \in TS$ ;
- 4.3.4.7  $REGMax10R_{t,r}$  designates the maximum amount of total *ten-minute operating reserve* that may be scheduled in region  $r \in ORREG$  in time-step  $t \in TS$ ; and
- 4.3.4.8  $REGMax30R_{t,r}$  designates the maximum amount of *thirty-minute operating reserve* that may be scheduled in region  $r \in ORREG$  in time-step  $t \in TS$ .

#### 4.3.5 Intertie Limits

- 4.3.5.1  $EnCoeff_{a,z}$  designates the coefficient for calculating the contribution of scheduled *energy* flows and *operating reserve* inflows for *intertie* zone  $a \in A$ , which is part of *intertie* limit constraint  $z \in Z_{Sch}$ . A coefficient of + 1 shall describe flows into Ontario while a coefficient of –1 shall describe flows out of Ontario;
- 4.3.5.2  $MaxExtSch_{t,z}$  designates the maximum flow limit for *intertie* flow constraint  $z \in Z_{Sch}$  in time-step  $t \in TS$ ;
- 4.3.5.3  $ExtDSC_t$  designates the net interchange scheduling limit for when the net flows over all *interties* from time-step  $(t - 1)$  to time-step  $t$  decrease; and
- 4.3.5.4  $ExtUSC_t$  designates the net interchange scheduling limit for when the net flows over all *interties* from time-step  $(t - 1)$  to time-step  $t$  increase.

#### 4.3.6 Resource Minimum and Maximum Constraints

4.3.6.1 Where applicable the minimum or maximum output of a *dispatchable generation resource* or a *non-dispatchable generation resource*, minimum or maximum consumption of a *dispatchable load*, and minimum and maximum reduction of an *hourly demand response resource* may be limited due to *reliability constraints*, applicable *contracted ancillary services*, *day-ahead operational commitments*, previous *pre-dispatch operational commitments*, *outages*, *derates*, activation/non-activation of *hourly demand response resources* and other constraints, such that:

- 4.3.6.1.1  $MinDL_{t,b}$  designates the most restrictive minimum consumption limit for the *dispatchable load* at bus  $b \in B^{DL}$ ;
- 4.3.6.1.2  $MaxDL_{t,b}$  designates the most restrictive maximum consumption limit for the *dispatchable load* at bus  $b \in B^{DL}$ ;
- 4.3.6.1.3  $MinNDG_{t,b}$  designates the most restrictive minimum output limit for the *non-dispatchable generation resource* at bus  $b \in B^{NDG}$ ;
- 4.3.6.1.4  $MaxNDG_{t,b}$  designates the most restrictive maximum output limit for the *non-dispatchable generation resource* at bus  $b \in B^{NDG}$ ;
- 4.3.6.1.5  $MinDG_{t,b}$  designates the most restrictive minimum output limit for the *dispatchable generation resource* at bus  $b \in B^{DG}$ ;
- 4.3.6.1.6  $MaxDG_{t,b}$  designates the most restrictive maximum output limit for the *dispatchable generation resource* at bus  $b \in B^{DG}$ ;
- 4.3.6.1.7  $MaxMLP_{t,b}$  designates the maximum output limit in time-step  $t$  for the *minimum loading point* region of a *pseudo-unit* at bus  $b \in B^{PSU}$ ;
- 4.3.6.1.8  $MaxDR_{t,b}$  designates the maximum output limit in time-step  $t$  for the *dispatchable* region of a *pseudo-unit* at bus  $b \in B^{PSU}$ ;

- 4.3.6.1.9  $MaxDF_{t,b}$  designates the maximum output limit in time-step  $t$  for the duct firing region of a *pseudo-unit* at bus  $b \in B^{PSU}$ ;
- 4.3.6.1.10  $MinHDR_{t,b}$  designates the minimum load reduction level that may be scheduled for the *hourly demand response resource* at bus  $b \in B^{HDR}$ ; and
- 4.3.6.1.11  $MaxHDR_{t,b}$  designates the maximum load reduction level that may be scheduled for the *hourly demand response resource* at bus  $b \in B^{HDR}$ .

#### 4.3.7 Constraint violation penalties for time step $t \in TS$ :

- 4.3.7.1  $(PLdViolSch_{st,i}, QLdViolSch_{t,i})$  for  $i \in \{1, \dots, N_{LdViol_t}\}$  designates the price-quantity segments of the penalty curve for under generation used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.2  $(PLdViolPrc_{t,i}, QLdViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{LdViol_t}\}$  designates the price-quantity segments of the penalty curve for under generation used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.3  $(PGenViolSch_{t,i}, QGenViolSch_{t,i})$  for  $i \in \{1, \dots, N_{GenViol_t}\}$  designates the price-quantity segments of the penalty curve for over generation used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.4  $(PGenViolPrc_{t,i}, QGenViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{GenViol_t}\}$  designates the price-quantity segments of the penalty curve for over generation used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.5  $(P10SViolSch_{t,i}, Q10SViolSch_{t,i})$  for  $i \in \{1, \dots, N_{10SViol_t}\}$  designates the price-quantity segments of the penalty curve for the synchronized *ten-minute operating reserve* requirement used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.6  $(P10SViolPrc_{t,i}, Q10SViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{10SViol_t}\}$  designates the price-quantity segments of the penalty curve for the synchronized *ten-minute operating reserve* requirement used by the Pre-Dispatch

Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;

- 4.3.7.7 ( $P10RViolSch_{t,i}, Q10RViolSch_{t,i}$ ) for  $i \in \{1, \dots, N_{10RViol_t}\}$  designates the price-quantity segments of the penalty curve for the total *ten-minute operating reserve* requirement used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.8 ( $P10RViolPrc_{t,i}, Q10RViolPrc_{t,i}$ ) for  $i \in \{1, \dots, N_{10RViol_t}\}$  designates the price-quantity segments of the penalty curve for the total *ten-minute operating reserve* requirement used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.9 ( $P30RViolSch_{t,i}, Q30RViolSch_{t,i}$ ) for  $i \in \{1, \dots, N_{30RViol_t}\}$  designates the price-quantity segments of the penalty curve for the total *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.10 ( $P30RViolPrc_{t,i}, Q30RViolPrc_{t,i}$ ) for  $i \in \{1, \dots, N_{30RViol_t}\}$  designates the price-quantity segments of the penalty curve for the total *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.11 ( $PREG10RViolSch_{t,i}, QREG10RViolSch_{t,i}$ ) for  $i \in \{1, \dots, N_{REG10RViol_t}\}$  designates the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* minimum requirements used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.12 ( $PREG10RViolPrc_{t,i}, QREG10RViolPrc_{t,i}$ ) for  $i \in \{1, \dots, N_{REG10RViol_t}\}$  designates the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* minimum requirements used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.13 ( $PREG30RViolSch_{t,i}, QREG30RViolSch_{t,i}$ ) for  $i \in \{1, \dots, N_{REG30RViol_t}\}$  designates the price-quantity segments of the penalty curve for area *thirty-minute operating reserve* minimum requirements used by the

Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;

- 4.3.7.14  $(PREG30RViolPrc_{t,i}, QREG30RViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{REG30RViol_t}\}$   
designates the price-quantity segments of the penalty curve for area *thirty-minute operating reserve* minimum requirements used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.15  $(PXREG10RViolSch_{t,i}, QXREG10RViolSch_{t,i})$  for  $i \in \{1, \dots, N_{XREG10RViol_t}\}$   
designates the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* maximum restrictions used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.16  $(PXREG10RViolPrc_{t,i}, QXREG10RViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{XREG10RViol_t}\}$   
designates the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* maximum restrictions used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.17  $(PXREG30RViolSch_{t,i}, QXREG30RViolSch_{t,i})$  for  $i \in \{1, \dots, N_{XREG30RViol_t}\}$   
designates the price-quantity segments of the penalty curve for area total *thirty-minute operating reserve* maximum restrictions used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.18  $(PXREG30RViolPrc_{t,i}, QXREG30RViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{XREG30RViol_t}\}$   
designates the price-quantity segments of the penalty curve for area total *thirty-minute operating reserve* maximum restrictions used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.19  $(PPreITLViolSch_{f,t,i}, QPreITLViolSch_{f,t,i})$  for  $i \in \{1, \dots, N_{PreITLViol_{f,t}}\}$   
designates the price-quantity segments of the penalty curve for exceeding the pre-contingency limit of the transmission constraint for *facility*  $f \in F$  used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.20  $(PPreITLViolPrc_{f,t,i}, QPreITLViolPrc_{f,t,i})$  for  $i \in \{1, \dots, N_{PreITLViol_{f,t}}\}$   
designates the price-quantity segments of the penalty curve for exceeding the pre-contingency limit of the transmission constraint for *facility*  $f \in F$  used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;

- 4.3.7.21 ( $PITLViolSch_{c,f,t,i}$ ,  $QITLViolSch_{c,f,t,i}$ ) for  $i \in \{1, \dots, N_{ITLViol_{c,f,t}}\}$  designates the price-quantity segments of the penalty curve for exceeding the contingency  $c \in C$  post-contingency limit of the transmission constraint for facility  $f \in F$  used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.22 ( $PITLViolPrc_{c,f,t,i}$ ,  $QITLViolPrc_{c,f,t,i}$ ) for  $i \in \{1, \dots, N_{ITLViol_{c,f,t}}\}$  designates the price-quantity segments of the penalty curve for exceeding the contingency  $c \in C$  post-contingency limit of the transmission constraint for facility  $f \in F$  used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.23 ( $PPreXTLViolSch_{z,t,i}$ ,  $QPreXTLViolSch_{z,t,i}$ ) for  $i \in \{1, \dots, N_{PreXTLViol_{z,t}}\}$  designates the price-quantity segments of the penalty curve for exceeding the flow limit specified by  $z \in Z_{Sch}$  used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.24 ( $PPreXTLViolPrc_{z,t,i}$ ,  $QPreXTLViolPrc_{z,t,i}$ ) for  $i \in \{1, \dots, N_{PreXTLViol_{z,t}}\}$  designates the price-quantity segments of the penalty curve for exceeding the flow limit specified by  $z \in Z_{Sch}$  used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.25 ( $PNIUViolSch_{t,i}$ ,  $QNIUViolSch_{t,i}$ ) for  $i \in \{1, \dots, N_{NIUViol_t}\}$  designates the price-quantity segments of the penalty curve for exceeding the time-step  $t$  net interchange increase constraint between time-steps  $(t-1)$  and  $t$  used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.26 ( $PNIUViolPrc_{t,i}$ ,  $QNIUViolPrc_{t,i}$ ) for  $i \in \{1, \dots, N_{NIUViol_t}\}$  designates the price-quantity segments of the penalty curve for exceeding the time-step  $t$  net interchange increase constraint between time-steps  $(t-1)$  and  $t$  used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.27 ( $PNIDViolSch_{t,i}$ ,  $QPNIDViolSch_{t,i}$ ) for  $i \in \{1, \dots, N_{NIDViol_t}\}$  designates the price-quantity segments of the penalty curve for exceeding the time-step  $t$  net interchange decrease constraint between time-steps  $(t-1)$  and  $t$  used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.28 ( $PNIDViolPrc_{t,i}$ ,  $QPNIDViolPrc_{t,i}$ ) for  $i \in \{1, \dots, N_{NIDViol_t}\}$  designates the price-quantity segments of the penalty curve for exceeding the time-

step  $t$  net interchange decrease constraint between time-steps  $(t-1)$  and  $t$  used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;

- 4.3.7.29  $(PMaxDelViolSch_{t,i}, QMaxDelViolSch_{t,i})$  for  $i \in \{1, \dots, N_{MaxDelViol_t}\}$  designates the price-quantity segments of the penalty curve for exceeding a *resource's maximum daily energy limit* used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.30  $(PMaxDelViolPrc_{t,i}, QMaxDelViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{MaxDelViol_t}\}$  designates the price-quantity segments of the penalty curve for exceeding a *resource's maximum daily energy limit* used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.31  $(PMinDelViolSch_{t,i}, QMinDelViolSch_{t,i})$  for  $i \in \{1, \dots, N_{MinDelViol_t}\}$  designates the price-quantity segments of the penalty curve for under-scheduling a *resource's minimum daily energy limit* used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.32  $(PMinDelViolPrc_{t,i}, QMinDelViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{MinDelViol_t}\}$  designates the price-quantity segments of the penalty curve for under-scheduling a *resource's minimum daily energy limit* used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.33  $(PSMaxDelViolSch_{t,i}, QSMaxDelViolSch_{t,i})$  for  $i \in \{1, \dots, N_{SMaxDelViol_t}\}$  designate the price-quantity segments of the penalty curve for exceeding a shared *maximum daily energy limit* used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.34  $(PSMaxDelViolPrc_{t,i}, QSMaxDelViolPrc_{t,i})$  for  $i \in \{1, \dots, N_{SMaxDelViol_t}\}$  designate the price-quantity segments of the penalty curve for exceeding a shared *maximum daily energy limit* used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.35  $(PSMinDelViolSch_{t,i}, QSMinDelViolSch_{t,i})$  for  $i \in \{1, \dots, N_{SMinDelViol_t}\}$  designate the price-quantity segments of the penalty curve for under-scheduling a shared *minimum daily energy limit* used by the Pre-

Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;

- 4.3.7.36 ( $PSMinDelViolPrc_{t,i}, QSMInDelViolPrc_{t,i}$ ) for  $i \in \{1, \dots, N_{SMInDelViol_t}\}$  designate the price-quantity segments of the penalty curve for under-scheduling a shared *minimum daily energy limit* used by the Pre-Dispatch Pricing algorithm in section 9 and Reference Level Pricing algorithm in section 13;
- 4.3.7.37 ( $POGenLnkViolSch_{t,i}, QOGenLnkViolSch_{t,i}$ ) for  $i \in \{1, \dots, N_{OGenLnkViol_t}\}$  designate the price-quantity segments of the penalty curve for over generation on a downstream *resource* used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12;
- 4.3.7.38 ( $PUGenLnkViolSch_{t,i}, QUGenLnkViolSch_{t,i}$ ) for  $i \in \{1, \dots, N_{UGenLnkViol_t}\}$  designate the price-quantity segments of the penalty curve for under generation on a downstream *resource* used by the Pre-Dispatch Scheduling algorithm in section 8 and the Reference Level Scheduling algorithm in section 12; and
- 4.3.7.39  $NISLPen$  designates the net interchange scheduling limit constraint violation penalty price for *locational marginal pricing*.

#### 4.3.8 Price Bounds

- 4.3.8.1  $EngyPrcCeil$  designates and is equal to the *maximum market clearing price* for *energy*;
- 4.3.8.2  $EngyPrcFlr$  designates and is equal to the *settlement floor price* for *energy*;
- 4.3.8.3  $ORPrcCeil$  designates and is equal to the *maximum operating reserve price* for all classes of *operating reserve*; and
- 4.3.8.4  $ORPrcFlr$  designates the minimum price for all classes of *operating reserve* and is equal to \$0.

#### 4.3.9 Ex-Ante Market Power Mitigation

- 4.3.9.1  $BCACondThresh$  designates the threshold for the congestion component of a *resource's locational marginal price* for *energy*, above which the *resource* will meet the broad constrained area condition, and is equal to \$25/MWh;



- 4.3.9.2 *IBPThresh* designates the *intertie border price* threshold for *energy* and is equal to \$100/MWh;
- 4.3.9.3 *ORGCondThresh* designates the global market power condition threshold for a *resource's locational marginal price* for *operating reserve* and is equal to \$15/MW;
- 4.3.9.4  $PDGRef_{t,b,k'}$  designates the *reference level value* for *energy* lamination  $k' \in K_{t,b}^E$  for the *resource* at bus  $b \in B^{DG}$  in time-step  $t \in TS$ ;
- 4.3.9.5  $P10SDGRef_{t,b,k'}$  designates the *reference level value* for synchronized *ten-minute operating reserve* lamination  $k' \in K_{t,b}^{10S}$  for the *resource* at bus  $b \in B^{DG}$  in time-step  $t \in TS$ ;
- 4.3.9.6  $P10NDGRef_{t,b,k'}$  designates the *reference level value* for non-synchronized *ten-minute operating reserve* lamination  $k' \in K_{t,b}^{10N}$  for the *resource* at bus  $b \in B^{DG}$  in time-step  $t \in TS$ ;
- 4.3.9.7  $P30RDGRef_{t,b,k'}$  designates the *reference level value* for *thirty-minute operating reserve* lamination  $k' \in K_{t,b}^{30R}$  for the *resource* at bus  $b \in B^{DG}$  in time-step  $t \in TS$ ;
- 4.3.9.8  $P10SDLRef_{t,b,j'}$  designates the *reference level value* for synchronized *ten-minute operating reserve* lamination  $j' \in J_{t,b}^{10S}$  for the *resource* at bus  $b \in B^{DL}$  in time-step  $t \in TS$ ;
- 4.3.9.9  $P10NDLRef_{t,b,j'}$  designates the *reference level value* for non-synchronized *ten-minute operating reserve* lamination  $j' \in J_{t,b}^{10N}$  for the *resource* at bus  $b \in B^{DL}$  in time-step  $t \in TS$ ;
- 4.3.9.10  $P30RDLRef_{t,b,j'}$  designates the *reference level value* for *thirty-minute operating reserve* lamination  $j' \in J_{t,b}^{30R}$  for the *resource* at bus  $b \in B^{DG}$  in time-step  $t \in z$
- 4.3.9.11  $SUDGRef_{t,b}$  designates the *reference level value* for the *start-up offer* for the *resource* at bus  $b \in B^{NQS}$  in time-step  $t \in TS$ ;
- 4.3.9.12  $SNLRef_{t,b}$  designates the *reference level value* for the *speed no-load offer* for the *resource* at bus  $b \in B^{NQS}$  in time-step  $t \in TS$ ;
- 4.3.9.12  $PLTMLPRef_{t,b,k'}$  designates the *reference level value* for the *energy* up to the *minimum loading point reference level* lamination  $k' \in$

$K_{h,b}^{LTMLP}$  of the *offer* for the *resource* at bus  $b \in B^{DG}$  in time-step  $t \in TS_i$

- 4.3.9.14  $CTEnThresh1^{NCA}$  designates the conduct threshold for a *resource* in a *narrow constrained area* as a percent increase above the *reference level value* of the *energy offer* for the *resource* and is equal to 50%;
- 4.3.9.15  $CTEnThresh2^{NCA}$  designates the conduct threshold for a *resource* in a *narrow constrained area* as a \$/MWh increase above the *reference level value* of the *energy offer* for the *resource* and is equal to \$25/MWh;
- 4.3.9.16  $CTSUThresh^{NCA}$  designates the conduct threshold for a *resource* in a *narrow constrained area* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 25%;
- 4.3.9.17  $CTSNLThresh^{NCA}$  designates the conduct threshold for a *resource* in a *narrow constrained area* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 25%;
- 4.3.9.18  $CTEnThresh1^{DCA}$  designates the conduct threshold for a *resource* in a *dynamic constrained area* as a percent increase above the *reference level value* of the *energy offer* for the *resource* and is equal to 50%;
- 4.3.9.19  $CTEnThresh2^{DCA}$  designates the conduct threshold for a *resource* in a *dynamic constrained area* as a \$/MWh increase above the *reference level value* of the *energy offer* for the *resource* and is equal to \$25/MWh;
- 4.3.9.20  $CTSUThresh^{DCA}$  designates the conduct threshold for a *resource* in a *dynamic constrained area* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 25%;
- 4.3.9.21  $CTSNLThresh^{DCA}$  designates the conduct threshold for a *resource* in a *dynamic constrained area* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 25%;
- 4.3.9.22  $CTEnThresh1^{BCA}$  designates the conduct threshold for a *resource* in a *broad constrained area* as a percent increase above the *reference level value* of the *energy offer* for the *resource* and is equal to 300%;
- 4.3.9.23  $CTEnThresh2^{BCA}$  designates the conduct threshold for a *resource* in a *broad constrained area* as a \$/MWh increase above the *reference*

*level value* of the *energy offer* for the *resource* and is equal to \$100/MWh;

- 4.3.9.24 *CTSUThresh<sup>BCA</sup>* designates the conduct threshold for a *resource* in a broad constrained area as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 100%;
- 4.3.9.25 *CTSNLThresh<sup>BCA</sup>* designates the conduct threshold for a *resource* in a broad constrained area as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 100%;
- 4.3.9.26 *CTEnThresh1<sup>GMP</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *energy offer* for the *resource* and is equal to 300%;
- 4.3.9.27 *CTEnThresh2<sup>GMP</sup>* designates the global market power conduct threshold for a *resource* as a \$/MWh increase above the *reference level value* of the *energy offer* for the *resource* and is equal to \$100 MW/h;
- 4.3.9.28 *CTSUThresh<sup>GMP</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 100%;
- 4.3.9.29 *CTSNLThresh<sup>GMP</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 100%;
- 4.3.9.30 *CTORThresh1<sup>ORL</sup>* designates the local market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *operating reserve offer* for the *resource* and is equal to 10%;
- 4.3.9.31 *CTORThresh2<sup>ORL</sup>* designates the local market power conduct threshold for a *resource* as a \$/MW increase above the *reference level value* of the *operating reserve offer* for the *resource* and is equal to \$25/MW;
- 4.3.9.32 *CTEnThresh1<sup>ORL</sup>* designates the local market power conduct threshold for *energy to minimum loading point* for a *resource* as a percent increase above the *reference level value* of the *offer for energy* up to the *minimum loading point* for the *resource* and is equal to 10%;

- 4.3.9.33 *CTEnThresh2<sup>ORL</sup>* designates the local market power conduct threshold for *energy* to *minimum loading point* conduct threshold for a *resource* as a \$/MW increase above the *reference level value* of the *energy* for *energy* up to the *minimum loading point* for the *resource* and is equal to \$25/MW;
- 4.3.9.34 *CTSUThresh<sup>ORL</sup>* designates the local market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 10%;
- 4.3.9.35 *CTSNLThresh<sup>ORL</sup>* designates the local market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 10%;
- 4.3.9.36 *CTORThresh1<sup>ORG</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *operating reserve offer* for the *resource* and is equal to 50%;
- 4.3.9.37 *CTORThresh2<sup>ORG</sup>* designates the global market power conduct threshold for a *resource* as a \$/MW increase above the *reference level value* of the *operating reserve offer* for the *resource* and is equal to \$25/MW;
- 4.3.9.38 *CTEnThresh1<sup>ORG</sup>* designates the global market power conduct threshold for *energy* to *minimum loading point* for a *resource* as a percent increase above the *reference level value* of the *offer* for *energy* up to the *minimum loading point* for the *resource* and is equal to 50%;
- 4.3.9.39 *CTEnThresh2<sup>ORG</sup>* designates the global market power conduct threshold for *energy* to *minimum loading point* for a *resource* as a \$/MW increase above the *reference level value* of the *offer* for *energy* up to the *minimum loading point* for the *resource* and is equal to \$25/MW;
- 4.3.9.40 *CTSUThresh<sup>ORG</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *start-up offer* for the *resource* and is equal to 25%;
- 4.3.9.41 *CTSNLThresh<sup>ORG</sup>* designates the global market power conduct threshold for a *resource* as a percent increase above the *reference level value* of the *speed no-load offer* for the *resource* and is equal to 25%;

- 4.3.9.42 *CTEnMinOffer* designates the minimum price for the *offer* lamination for *energy* to be included in the Conduct Test. *Offer* laminations for *energy* below this value are excluded from the Conduct Test and is equal to \$25/MWh;
- 4.3.9.43 *CTORMinOffer* designates the minimum price for the *offer* lamination for *operating reserve* to be included in the Conduct Test. *Offer* laminations for *operating reserve* below this value are excluded from the Conduct Test and is equal to \$5/MW;
- 4.3.9.44 *ITThresh1<sup>NCA</sup>* designates the price impact threshold for a *resource* in a *narrow constrained area* as a percent increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to 50%;
- 4.3.9.45 *ITThresh2<sup>NCA</sup>* designates the price impact threshold for a *resource* in a *narrow constrained area* as a \$/MWh increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to \$25/MWh;
- 4.3.9.46 *ITThresh1<sup>DCA</sup>* designates the price impact threshold for a *resource* in a *dynamic constrained area* as a percent increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to 50%;
- 4.3.9.47 *ITThresh2<sup>DCA</sup>* designates the price impact threshold for a *resource* in a *dynamic constrained area* as a \$/MWh increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to \$25/MWh;
- 4.3.9.48 *ITThresh1<sup>BCA</sup>* designates the price impact threshold for a *resource* in a *broad constrained area* as a percent increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to 100%;
- 4.3.9.49 *ITThresh2<sup>BCA</sup>* designates the price impact threshold for a *resource* in a *broad constrained area* as a \$/MWh increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to \$50/MWh;

- 4.3.9.50  $ITThresh1^{GMP}$  designates the global market power price impact threshold for a *resource* as a percent increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to 100%;
- 4.3.9.51  $ITThresh2^{GMP}$  designates the global market power price impact threshold for a *resource* as a \$/MWh increase in the *energy locational marginal price* output from section 9 above the *energy locational marginal price* output from section 13 and is equal to \$50/MWh;
- 4.3.9.52  $ITThresh1^{ORG}$  designates the global market power price impact threshold for a *resource* as a percent increase in the *operating reserve locational marginal price* output from section 9 above the *operating reserve locational marginal price* output from section 13 and is equal to 50%; and
- 4.3.9.53  $ITThresh2^{ORG}$  designates the global market power price impact threshold for a *resource* as a \$/MW increase in the *operating reserve locational marginal price* output from section 9 above the *operating reserve locational marginal price* output from section 13 and is equal to \$25/MW.

#### 4.3.10 Weighting Factors for Zonal Prices

- 4.3.10.1  $WF_{t,m,b}^{VIRT}$  designates the weighting factor for bus  $b \in L_m^{VIRT}$  used to calculate the price for *virtual transaction zone*  $m \in M$  for time-step  $t \in TS$  and is equal to the weighting factor used in the *day-ahead market* for the applicable hour;
- 4.3.10.2  $WF_{h,y,b}^{NDL}$  designates the weighting factor for bus  $b \in L_y^{NDL}$  used to calculate the price for *non-dispatchable load zone*  $y \in Y$  for time-step  $t \in TS$ . The weighting factors shall be obtained by renormalizing the load distribution factors so that for a given time-step the sum of weighting factors for a *non-dispatchable load zone* is equal to one.

#### 4.3.11 Day-Ahead Market Scheduled Intertie Transactions

- 4.3.11.1  $SIGT_{t,d}^{DAM}$  designates the *day-ahead market* scheduled quantity of import *energy* for *intertie zone* source bus  $d \in DI$  in time-step  $t \in \{4, \dots, n_{LAP}\}$ ;
- 4.3.11.2  $S10NIGT_{t,d}^{DAM}$  designates the *day-ahead market* scheduled quantity of non-synchronized *ten-minute operating reserve* for *intertie zone* source bus  $d \in DI$  in time-step  $t \in \{4, \dots, n_{LAP}\}$ ;

- 4.3.11.3  $S30RIGT_{t,d}^{DAM}$  designates the *day-ahead market* scheduled quantity of *thirty-minute operating reserve* for *intertie zone* source bus  $d \in DI$  in time-step  $t \in \{4, \dots, n_{LAP}\}$ ;
- 4.3.11.4  $SXLT_{t,d}^{DAM}$  designates the *day-ahead market* scheduled quantity of export *energy* for *intertie zone* sink bus  $d \in DX$  in time-step  $t \in \{4, \dots, n_{LAP}\}$ ;
- 4.3.11.5  $S10NXLT_{t,d}^{DAM}$  designates the *day-ahead market* scheduled quantity of non-synchronized *ten-minute operating reserve* for *intertie zone* sink bus  $d \in DX$  in time-step  $t \in \{4, \dots, n_{LAP}\}$ ; and
- 4.3.11.6  $S30RXLT_{t,d}^{DAM}$  designates the *day-ahead market* scheduled quantity of *thirty-minute operating reserve* for *intertie zone* sink bus  $d \in DX$  in time-step  $t \in \{4, \dots, n_{LAP}\}$ .

#### 4.3.12 Import Offers Without a Day-Ahead Market Schedule

- 4.3.12.1  $SIGT_{t,d}^{EXTRA}$  designates the extra quantity of *energy* for import from *intertie zone* source bus  $d \in DI$  in time-step  $t \in \{4, \dots, n_{LAP}\}$  that may be considered for the purpose of *reliability*;
- 4.3.12.2  $S10NIGT_{t,d}^{EXTRA}$  designates the extra quantity of non-synchronized *ten-minute operating reserve* for import from *intertie zone* source bus  $d \in DI$  in time-step  $t \in \{4, \dots, n_{LAP}\}$  that may be considered for the purpose of *reliability*; and
- 4.3.12.3  $S30RIGT_{t,d}^{EXTRA}$  designates the extra quantity of *thirty-minute operating reserve* for import from *intertie zone* source bus  $d \in DI$  in time-step  $t \in \{4, \dots, n_{LAP}\}$  that may be considered for the purpose of *reliability*.

## 4.4 Other Data Parameters

### 4.4.1 Non-Dispatchable Demand Forecast

- 4.4.1.1  $FL_t$  designates the total province-wide non-*dispatchable demand* forecast for time-step  $t \in TS$  calculated by the *security* assessment function.

### 4.4.2 Internal Transmission Constraints

- 4.4.2.1  $PreConSF_{t,f,b}$  designates the pre-contingency sensitivity factor for bus  $b \in B \cup D$  indicating the fraction of *energy* injected at bus  $b$  which flows on *facility*  $f$  during time-step  $t$  under pre-contingency conditions;

- 4.4.2.2  $AdjNormMaxFlow_{t,f}$  designates the limit corresponding to the maximum flow allowed on *facility f* in time-step  $t$  under pre-contingency conditions;
  - 4.4.2.3  $SF_{t,c,f,b}$  designates the post-contingency sensitivity factor for bus  $b \in B \cup D$  indicating the fraction of *energy* injected at bus  $b$  which flows on *facility f* during time-step  $t$  under post-contingency conditions for contingency  $c$ ; and
  - 4.4.2.4  $AdjEmMaxFlow_{t,c,f}$  designates the limit corresponding to the maximum flow allowed on *facility f* in time-step  $t$  under post-contingency conditions for contingency  $c$ .
- 4.4.3 Transmission Losses
- 4.4.3.1  $MglLoss_{t,b}$  designates the marginal loss factor and represents the marginal impact on transmission losses resulting from transmitting *energy* from the *reference bus* to serve an increment of additional load at *resource bus*  $b \in B \cup D$  in time-step  $t \in TS$ ; and
  - 4.4.3.2  $LossAdj_t$  designates any adjustment needed for time-step  $t \in TS$  to correct for any discrepancy between Ontario total system losses calculated using a base case power flow from the *security* assessment function and linearized losses that would be calculated using the marginal loss factors.

## 5 Initialization

### 5.1 Purpose

- 5.1.1 The initialization processes set out in this section 5 shall occur prior to the execution of the *pre-dispatch calculation engine* described in section 2.2.1 above.

### 5.2 Reference Bus

- 5.2.1 The *IESO* shall use Richview Transformer Station as the *pre-dispatch calculation engine's* default *reference bus* for the calculation of *locational marginal prices*.
- 5.2.2 If the default *reference bus* is out of service, another in-service bus shall be selected.



## 5.3 Islanding Conditions

- 5.3.1 In the event of a network split, the *pre-dispatch calculation engine* shall:
- 5.3.1.1 only evaluate *resources* that are within the *main island*;
  - 5.3.1.2 use only forecasts of *demand* forecast areas in the *main island*; and
  - 5.3.1.3 use a bus within the *main island* in place of the *reference bus* if the *reference bus* does not fall within the *main island*.

## 5.4 Variable Generation Tie-Breaking

- 5.4.1 For each time-step  $t \in TS$ , each *variable generation resource* bus  $b \in B^{VG}$  and each *offer lamination*  $k \in K_{t,b}^E$ , the *offer price*  $PDG_{t,b,k}$  shall be modified to  $PDG_{t,b,k} - \left( \frac{TBM_{t,b}}{NumVG_t} \right) \rho$ , where  $\rho$  is a small nominal value of order  $10^{-4}$ .

## 5.5 Pseudo-Unit Constraints

- 5.5.1 Constraints for *pseudo-units* corresponding to minimum and maximum constraints on physical *resources* shall be determined in accordance with section 15.

## 5.6 Dispatch Data Across Two Dispatch Days

- 5.6.1 If the pre-dispatch look-ahead period spans two *dispatch days*, then the *pre-dispatch calculation engine* shall set the parameters below as follows:

- 5.6.1.1  $LNKC$ , which designates the linked *dispatchable* hydroelectric *generation resources* and is defined by:

$$LNKC = \begin{cases} LNK_{tod} & \text{if } DAYS = \{tod\} \\ LNK_{tom} & \text{if } DAYS = \{tod, tom\} \end{cases}.$$

- 5.6.1.2  $LagC_{b_1, b_2}$ , which designates the *time lag* between *dispatchable* hydroelectric *generation resources*  $(b_1, b_2) \in LNKC$  and is defined by:

$$LagC_{b_1, b_2} = \begin{cases} Lag_{tod, b_1, b_2} & \text{if } DAYS = \{tod\} \\ Lag_{tom, b_1, b_2} & \text{if } DAYS = \{tod, tom\} \end{cases}.$$

- 5.6.1.3  $MWhRatioC_{b_1, b_2}$ , which designates the *MWh ratio* for *dispatchable* hydroelectric *generation resources*  $(b_1, b_2) \in LNKC$  and is defined by:

$$MWhRatioC_{b_1, b_2} = \begin{cases} MWhRatio_{tod, b_1, b_2} & \text{if } DAYS = \{tod\} \\ MWhRatio_{tom, b_1, b_2} & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.1.4  $MinQDGC_b$ , which designates the *minimum loading point* for *dispatchable generation resource*  $b \in B^{DG}$  and, subject to section 5.6.2, is defined by:

$$MinQDGC_b = \begin{cases} MinQDG_{tod, b} & \text{if } DAYS = \{tod\} \\ MinQDG_{tom, b} & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.1.5  $MGBRTDGC_b$ , which designates the *minimum generation block run-time* for *non-quick start resource*  $b \in B^{NQS}$  and, subject to section 5.6.2, is defined by:

$$MGBRTDGC_b = \begin{cases} MGBRTDG_{tod, b} & \text{if } DAYS = \{tod\} \\ MGBRTDG_{tom, b} & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.1.6  $MGBDTDGC_b^m$ , which designates the *minimum generation block down-time* for *non-quick start resource*  $b \in B^{NQS}$  for *thermal state*  $m \in THERM$  and is defined by:

$$MGBDTDGC_b^m = \begin{cases} MGBDTDG_{tod, b}^m & \text{if } DAYS = \{tod\} \\ MGBDTDG_{tom, b}^m & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.1.7  $LTC_b^m$ , which designates the *lead time* for *non-quick start resource*  $b \in B^{NQS}$  for *thermal state*  $m \in THERM$  and is defined by

$$LTC_b^m = \begin{cases} LT_{tod, b}^m & \text{if } DAYS = \{tod\} \\ LT_{tom, b}^m & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.1.8  $RampHrsC_b^m$ , which designates the *ramp hours to minimum loading point* for a *non-quick start resource*  $b \in B^{NQS}$  for *thermal state*  $m \in THERM$  and is defined by:

$$RampHrsC_b^m = \begin{cases} RampHrs_{tod, b}^m & \text{if } DAYS = \{tod\} \\ RampHrs_{tom, b}^m & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.1.9  $RampEC_{b,w}^m$  for  $w \in \{1,..,RampHrsC_b^m\}$ , which designates the *ramp up energy to minimum loading point* for a *non-quick start resource*  $b \in B^{NQS}$  for *thermal state*  $m \in THERM$  and is defined by:

$$RampEC_{b,w}^m = \begin{cases} RampE_{tod,b,w}^m & \text{if } DAYS = \{tod\} \\ RampE_{tom,b,w}^m & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.1.10  $RampCTC_{b,w}^m$  for  $w \in \{1,..,RampHrsC_b^m\}$ , which designates the *ramp up energy to minimum loading point* for the combustion turbine resource associated with the *pseudo-unit* at bus  $b \in B^{PSU}$  for *thermal state*  $m \in THERM$  and is defined by:

$$RampCTC_{b,w}^m = \begin{cases} RampCT_{tod,b,w}^m & \text{if } DAYS = \{tod\} \\ RampCT_{tom,b,w}^m & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.1.11  $RampSTC_{b,w}^m$  for  $w \in \{1,..,RampHrsC_b^m\}$ , which designates the *ramp up energy to minimum loading point* for the steam turbine resource's portion of the *pseudo-unit* at bus  $b \in B^{PSU}$  for *thermal state*  $m \in THERM$  and is defined by:

$$RampSTC_{b,w}^m = \begin{cases} RampST_{tod,b,w}^m & \text{if } DAYS = \{tod\} \\ RampST_{tom,b,w}^m & \text{if } DAYS = \{tod, tom\} \end{cases}$$

- 5.6.2 If a *non-quick start resource* receives a commitment prior to the 20:00 EST *pre-dispatch calculation engine* run but that commitment is not yet complete, then:

- 5.6.2.1  $MinQDG_{tod,b}$  and  $MGBRTDG_{tod,b}$  shall continue to be applied until the commitment is complete; and
- 5.6.2.2  $MinQDG_{tom,b}$  and  $MGBRTDG_{tom,b}$  shall be applied for any new commitments made in the 20:00 EST *pre-dispatch calculation engine* run or later.

- 5.6.3 For all other daily *dispatch data*, except the *single cycle mode* flag determined in section 15.5, the current day value shall be used for all *dispatch hours* in the current *dispatch day* and the next day value shall be used for all *dispatch hours* in the next *dispatch day*.

## 5.7 Start-Up Offers for Non-Quick Start Resource Advancements

5.7.1 The *pre-dispatch calculation engine* shall use *start-up offers* for *non-quick start resources* with a *day-ahead operational commitment* as follows:

5.7.1.1 If the time-step  $t$  in the set of hours preceding the start-up time  $t_{DAM} \in TSC_b$  of a *day-ahead operational commitment* in day  $q \in DAYS$  are such that  $t \in \{ \max(t_{DAM} - (MGBRTDG_{q,b} + MGBDTDG_{q,b}^{HOT}), 2), \dots, t_{DAM} \}$ , then:

If  $SUDG_{t,b}^m \geq SUDG_{t,b}^{DAM}$ , then set  $SUAdjDG_{t,b}^m = SUDG_{t,b}^m$

If  $SUDG_{t,b}^m < SUDG_{t,b}^{DAM}$ , then set  $SUAdjDG_{t,b}^m = SUDG_{t,b}^{DAM}$

5.7.1.2 If the time-step  $t$  in the set of hours preceding the start-up time  $t_{DAM} \in TSC_b$  of a *day-ahead operational commitment* in day  $q \in DAYS$  are *offersuch* that  $t \notin \{ \max(t_{DAM} - (MGBRTDG_{q,b} + MGBDTDG_{q,b}^{HOT}), 2), \dots, t_{DAM} \}$ , then:

$$SUAdjDG_{t,b}^m = SUDG_{t,b}^m$$

## 5.8 Non-Quick Start Resource First Time-Step Available to Start

5.8.1 The *pre-dispatch calculation engine* shall determine the first time-step a *non-quick start resource* can be scheduled to its *minimum loading point* as follows:

5.8.1.1 For a *non-quick start resource* at bus  $b \in B^{NQS}$  that has not been scheduled at or above its *minimum loading point* for *InitDownHrs<sub>b</sub>* hours:

5.8.1.1.1 If  $0 \leq \text{InitDownHrs}_b + t - 1 \leq MGBDTDGC_b^{HOT}$ , then the *resource* cannot be scheduled to reach *minimum loading point* in time-step  $t \in TS$ ;

5.8.1.1.2 If  $\text{InitDownHrs}_b + LTC_b^{HOT} + 1 \leq MGBDTDGC_b^{WARM}$ , then a *lead time* of  $LTC_b^{HOT}$  will be applied and the *resource* can be scheduled to its *minimum loading point* in time-step  $t \in TS$  only if  $t \geq LTC_b^{HOT} + 2$ ;

5.8.1.1.3 If  $\text{InitDownHrs}_b + LTC_b^{WARM} + 1 \leq MGBDTDGC_b^{COLD}$ , then a *lead time* of  $LTC_b^{WARM}$  will be applied and the

*resource* can be scheduled to its *minimum loading point* in time-step  $t \in TS$  only if  $t \geq LTC_b^{WARM} + 2$ ; and

- 5.8.1.1.4 If a *lead time* of  $LTC_b^{COLD}$  will be applied and the *resource* can be scheduled to its *minimum loading point* in time-step  $t \in TS$  only if  $t \geq LTC_b^{COLD} + 2$ .

## 5.9 Initial Scheduling Assumptions

### 5.9.1 Initial Schedules

- 5.9.1.1 The following parameters designate the initial *energy* schedules used for time-step 1 of the pre-dispatch look-ahead period and shall be based on the values determined by the *IESO's energy* management system for internal *resources* and the most recent *interchange schedules* for time-step 1 for *boundary entity resources*:

- 5.9.1.1.1  $SDL_{1,b,j}$  designates the amount of *energy* that a *dispatchable load* is scheduled to consume at bus  $b \in B^{DL}$ ;
- 5.9.1.1.2  $SHDR_{1,b,j}$  designates the amount of *energy* an *hourly demand response resource* is scheduled to reduce consumption at bus  $b \in B^{HDR}$ ;
- 5.9.1.1.3  $SXL_{1,d,j}$  designates the amount of *energy* a *boundary entity resource* is scheduled to export at bus  $d \in DX$ ;
- 5.9.1.1.4  $SDG_{1,b,k}$  designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$ ;
- 5.9.1.1.5  $SCT_{1,b}$  designates the schedule of the combustion turbine *resource* associated with the *pseudo-unit* at bus  $b \in B^{PSU}$ ;
- 5.9.1.1.6  $SST_{1,p}$  designates the schedule of the steam turbine *resource*  $p \in PST$ ;
- 5.9.1.1.7  $SIG_{1,d,k}$  designates the amount of *energy* that a *boundary entity resource* is scheduled to import from *intertie zone* source bus  $d \in DI$ ;

- 5.9.1.2 The initial schedules for *non-quick start resources* shall be determined to align with the commitment status logic described in section 5.9.2.
- 5.9.2 The following parameters designate initial commitment status, number of hours in operation and number of hours down for time-step 1 of the pre-dispatch look-ahead period:
- 5.9.2.1  $ODG_{1,b}$  designates whether the *dispatchable generation resource* at bus  $b \in B^{NQS}$  has been scheduled at or above its *minimum loading point* in time-step 1, where  $ODG_{1,b}$  shall be set to  $ODG_{2,b}$  from the previous *pre-dispatch calculation engine run* unless the *real-time calculation engine* has kept such *resource* at or above its *minimum loading point* to respect a *reliability* constraint. In such cases,  $ODG_{1,b}$  shall be determined by the *real-time calculation engine* advisory schedule;
- 5.9.2.2  $InitOperHrs_b$  designates the number of consecutive hours at the end of time-step 1 for which the *resource* at bus  $b \in B^{NQS}$  has been, and is anticipated to be, operating at or above its *minimum loading point*. For *resources* with  $ODG_{1,b} = 0$ ,  $InitOperHrs_b$  shall be set to zero; and
- 5.9.2.3  $InitDownHrs_b$  designates the number of consecutive hours at the end of time-step 1 for which the *resource* at bus  $b \in B^{NQS}$  has not been, and is not anticipated to be, operating at or above its *minimum loading point*. For *resources* with  $ODG_{1,b} = 1$ ,  $InitDownHrs_b$  shall be set to zero.
- 5.9.3 Initial Net Interchange Schedule
- 5.9.3.1 The initial net *interchange schedule* value shall be the difference between all imports to Ontario and all exports from Ontario for time-step 1. By default, this value will be based on fixed schedules for imports and exports from the *real-time calculation engine*.
- 5.9.4 Number of Starts for Non-Quick Start Resources
- 5.9.4.1  $NumStarts_b$  designates the number of starts the *resource* at bus  $b \in B^{NQS}$  has incurred in the current *dispatch day*, plus any anticipated starts in time-step 1.
- 5.9.5 Number of Starts for Hydroelectric Resources
- 5.9.5.1  $NumStartsHE_b$  designates the number of starts the *resource* at bus  $b \in B^{HE}$  has incurred in the current *dispatch day*, plus any anticipated starts in time-step 1.

- 5.9.6 Cumulative Energy Production for Energy Limited Resources and Dispatchable Hydroelectric Resources
- 5.9.6.1  $EngyUsed_b$  designates the *energy* already provided by the *resource* at bus  $b \in B^{ELR} \cup B^{HE}$  in the current *dispatch day*, plus the *energy* scheduled in time-step 1; and
- 5.9.6.2  $EngyUsedSHE_s$  designates the *energy* already provided in the current *dispatch day* by all *resources* sharing a *maximum daily energy limit* or *minimum daily energy limit* in set  $s \in SHE$  plus the *energy* scheduled in time-step 1.
- 5.9.7 Past Hourly Production for Linked Hydroelectric Resources
- 5.9.7.1 For linked hydroelectric *resources*, the past hourly *energy* production of upstream *resources* shall be used to schedule downstream *resources* for time-steps in the pre-dispatch look-ahead period within the *time lag*. These past hourly production schedules shall be equal to the output determined by the *IESO's energy* management system based on real-time telemetry less any production scheduled as part of an *operating reserve* activation. For all linked hydroelectric *resources*  $(b_1, b_2) \in LNKC$  and all time-steps  $t \in TS$  such that  $t \leq LagC_{b_1, b_2}$ ,  $PastMWh_{t, b_1}$  designates the total *energy* produced by *resource*  $b_1$  exactly  $LagC_{b_1, b_2}$  hours prior to time-step  $t$ .
- 5.9.7.2 The schedules of downstream *resources* linked to time-step 1 upstream *resource* schedules shall be pre-determined based on the average value of the upstream *resource* advisory schedules from the last *real-time calculation engine* run that successfully completed before the *pre-dispatch calculation engine* run commenced. If the advisory schedule reflects an *operating reserve* activation for an upstream *resource*, then the schedule determined by the *real-time calculation engine* run prior to the *operating reserve* activation shall be used. For all linked hydroelectric *resources*  $(b_1, b_2) \in LNKC$  and all time-steps  $t \in TS$  such that  $t = LagC_{b_1, b_2} + 1$ ,  $PastMWh_{t, b_1}$  designates the total *energy* determined for *resource*  $b_1$  for time-step 1 to be used for scheduling downstream *resources* in time-step  $t$ .

## 6 Security Assessment Function in the Pre-Dispatch Calculation Engine

### 6.1 Interaction between the Security Assessment Function and Optimization Functions

- 6.1.1 The scheduling and pricing algorithms of the *pre-dispatch calculation engine* shall perform multiple iterations of the optimization functions and the *security* assessment function to check for violations of monitored thermal limits and operating *security limits* using the schedules produced by the optimization functions.
- 6.1.2 As multiple iterations are performed, the transmission constraints produced by the *security* assessment function shall be used by the optimization functions.
- 6.1.3 The *security* assessment function shall use the physical *resource* representation of *combined cycle plant* that are registered as *pseudo-units*.

### 6.2 Inputs into the Security Assessment Function

- 6.2.1 The *security* assessment function shall use the following inputs:
  - 6.2.1.1 the *IESO demand* forecasts; and
  - 6.2.1.2 applicable *IESO-controlled grid* information pursuant to section 3A.1 of Chapter 7.
- 6.2.2 The *security* assessment function shall also use the following outputs of the optimization functions:
  - 6.2.2.1 the schedules for *dispatchable loads* and *hourly demand response resources*;
  - 6.2.2.2 the schedules for *non-dispatchable generation resources* and *dispatchable generation resources*; and
  - 6.2.2.3 the schedules for *boundary entity resources* at each *intertie zone*.

### 6.3 Security Assessment Function Processing

- 6.3.1 The *security* assessment function shall determine the province-wide non-*dispatchable demand* forecast for time-step  $t$ ,  $FL_t$ , as follows:



- 6.3.1.1 determine forecast MW quantities for all *load resources* and losses using the *IESO demand* forecasts for *demand* forecast areas, load distribution factors, and the total of the *bid* quantities submitted for virtual *hourly demand response resources* and physical *hourly demand response resources*, and
  - 6.3.1.2 determine  $FL_t$  by adding the forecast MW quantities determined for each *non-dispatchable load*, each *price responsive load*, and each *dispatchable load* with no *bid*, including forecast MW losses in the *demand* forecast areas.
- 6.3.2 The *security* assessment function shall perform the following calculations and analyses:
- 6.3.2.1 A base case solution function shall prepare a power flow solution for each time-step. The base case solution function shall select the power system model state applicable to the forecast of conditions for the time-step and input schedules.
  - 6.3.2.2 The base case solution function shall use an AC power flow analysis. If the AC power flow analysis fails to converge, the base case solution function shall use a non-linear DC power flow analysis. If the non-linear DC power flow analysis fails to converge, the base case solution function shall use a linear DC power flow analysis.
  - 6.3.2.3 If the AC or non-linear DC power flow analysis converges, continuous thermal limits for all monitored equipment and operating *security limits* shall be monitored to check for pre-contingency limit violations.
  - 6.3.2.4 Violated pre-contingency limits shall be linearized using pre-contingency sensitivity factors and incorporated as constraints for use by the optimization functions.
  - 6.3.2.5 If the linear DC power flow analysis is used, the pre-contingency *security* assessment may develop linear constraints to facilitate the convergence of the AC or non-linear DC power flow analysis in the subsequent iterations.
  - 6.3.2.6 A linear power flow analysis shall be used to simulate contingencies, calculate post-contingency flows and check all monitored equipment for limited-time thermal limit violations.
  - 6.3.2.7 Violated post-contingency limits shall be linearized using post-contingency sensitivity factors and incorporated as constraints for use by the optimization functions.

- 6.3.2.8 The base case solution shall be used to calculate Ontario *transmission system* losses, marginal loss factors and loss adjustment for each time-step. The impact of losses on branches between the *resource* bus and the *resource connection point* to the *IESO-controlled grid* and losses on branches outside Ontario shall be excluded when determining marginal loss factors.
- 6.3.2.9 The Pre-Dispatch Scheduling and the Reference Level Scheduling algorithms described in sections 8 and 12, respectively, shall use the marginal loss factors for each time step calculated by the *security* assessment function.
- 6.3.2.10 The Pre-Dispatch Pricing and Reference Level Pricing algorithms described in sections 9 and 13, respectively, shall use the marginal loss factors used in the last iteration of the optimization function in the corresponding scheduling algorithm.

## **6.4 Outputs from the Security Assessment Function**

- 6.4.1 The outputs of the *security* assessment function used in the optimization functions include the following:
  - 6.4.1.1 a set of linearized constraints for all violated pre-contingency and post-contingency limits for each time-step. The sensitivities and limits associated with the constraints shall be those provided by the most recent *security* assessment function iteration;
  - 6.4.1.2 pre-contingency and post-contingency sensitivity factors for each time step;
  - 6.4.1.3 the marginal loss factors as described in sections 6.3.2.8 - 6.3.2.10; and
  - 6.4.1.4 loss adjustment quantity for each time-step.

## 7 Pass 1: Pre-Dispatch Scheduling Process

7.1.1 Pass 1 shall use *market participant* and *IESO* inputs and *resource* and system constraints to determine a set of *resource* schedules, commitments and *locational marginal prices*. Pass 1 shall consist of the following algorithms and tests:

- the Pre-Dispatch Scheduling algorithm described in section 8;
- the Pre-Dispatch Pricing algorithm described in section 9;
- the Constrained Area Conditions Test described in section 10;
- the Conduct Test described in section 11;
- the Reference Level Scheduling algorithm described in section 12;
- the Reference Level Pricing algorithm described in section 13; and
- the Price Impact Test described in section 14.

## 8 Pre-Dispatch Scheduling

### 8.1 Purpose

8.1.1 The Pre-Dispatch Scheduling algorithm shall perform a *security*-constrained unit commitment and economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, subject to section 14.7.1.3, to meet the *IESO's* province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the pre-dispatch look-ahead period.

### 8.2 Information, Sets, Indices and Parameters

8.2.1 Information, sets, indices and parameters used by the Pre-Dispatch Scheduling algorithm are described in sections 3 and 4.

### 8.3 Variables and Objective Function

8.3.1 The Pre-Dispatch Scheduling algorithm shall solve for the following variables:

- 8.3.1.1  $SDL_{t,b,j}$  , which designates the amount of *energy* that a *dispatchable load* is scheduled to consume at bus  $b \in B^{DL}$  in time-step  $t \in TS$  in association with lamination  $j \in J_{t,b}^E$ ;
- 8.3.1.2  $S10SDL_{t,b,j}$  , which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in time-step  $t \in TS$  in association with lamination  $j \in J_{t,b}^{10S}$ ;
- 8.3.1.3  $S10NDL_{t,b,j}$  , which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in time-step  $t \in TS$  in association with lamination  $j \in J_{t,b}^{10N}$ ;
- 8.3.1.4  $S30RDL_{t,b,j}$  , which designates the amount of *thirty-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in time-step  $t \in TS$  in association with lamination  $j \in J_{t,b}^{30R}$ ;
- 8.3.1.5  $SHDR_{t,b,j}$  , which designates the amount of *energy* reduction scheduled for an *hourly demand response resource* at bus  $b \in B^{HDR}$  in time-step  $t \in TS$  in association with lamination  $j \in J_{t,b}^E$ ;
- 8.3.1.6  $SXL_{t,d,j}$  , which designates the amount of *energy* a *boundary entity resource* is scheduled to export at bus  $d \in DX$  in time-step  $t \in TS$  in association with lamination  $j \in J_{t,d}^E$ ;
- 8.3.1.7  $S10NXL_{t,d,j}$  , which designates the amount of non-synchronized *ten-minute operating reserve* that a *boundary entity resource* is scheduled to provide at bus  $d \in DX$  in time-step  $t \in TS$  in association with lamination  $j \in J_{t,d}^{10N}$ ;
- 8.3.1.8  $S30RXL_{t,d,j}$  , which designates the amount of *thirty-minute operating reserve* that a *boundary entity resource* is scheduled to provide at bus  $d \in DX$  in time-step  $t \in TS$  in association with lamination  $j \in J_{t,d}^{30R}$ ;
- 8.3.1.9  $SNDG_{t,b,k}$  , which designates the amount of *energy* that a *non-dispatchable generation resource* is scheduled to provide at bus  $b \in B^{NDG}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^E$ ;
- 8.3.1.10  $SDG_{t,b,k}$  , which designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide above  $MinQDGC_b$  at bus  $b \in B^{DG}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^E$ ;

- 8.3.1.11  $ODG_{t,b}$  , which designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  has been scheduled at or above its *minimum loading point* in time-step  $t \in TS$ ;
- 8.3.1.12  $IDG_{t,b}$  , which designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  has been scheduled to reach its *minimum loading point* in time-step  $t \in TS$ ;
- 8.3.1.13  $S10SDG_{t,b,k}$  , which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^{10S}$ ;
- 8.3.1.14  $S10NDG_{t,b,k}$  , which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^{10N}$ ;
- 8.3.1.15  $S30RDG_{t,b,k}$  , which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^{30R}$ ;
- 8.3.1.16  $SCT_{t,b}$  , which designates the schedule of the combustion turbine *resource* associated with the *pseudo-unit* at bus  $b \in B^{PSU}$  in time-step  $t \in TS$ ;
- 8.3.1.17  $SST_{t,p}$  , which designates the schedule of steam turbine *resource*  $p \in PST$  in time-step  $t \in TS$ ;
- 8.3.1.18  $O10R_{t,b}$  , which designates whether the *pseudo-unit* at bus  $b \in B^{NO10DF}$  has been scheduled for *ten-minute operating reserve* in time-step  $t \in TS$ ;
- 8.3.1.19  $OHO_{t,b}$  , which designates whether the *dispatchable hydroelectric generation resource* at bus  $b \in B^{HE}$  has been scheduled at or above  $MinHO_{t,b}$  in time-step  $t \in TS$ ;
- 8.3.1.20  $OFR_{t,b,i}$  for  $i \in \{1, \dots, NFor_{q,b}\}$  , which designates whether the *dispatchable hydroelectric generation resource* at bus  $b \in B^{HE}$  has been scheduled at or below  $ForL_{q,b,i}$  or, at or above  $ForU_{q,b,i}$  in time-step  $t \in TS$ ;

- 8.3.1.21  $IHE_{t,b,i}$ , which designates whether the *dispatchable* hydroelectric *generation resource* at bus  $b \in B^{HE}$  registered a start between time-step  $(t-1)$  and  $t$  as a result of its schedule increasing from below  $StartMW_{b,i}$  to at or above  $StartMW_{b,i}$  for  $i \in \{1, \dots, NStartMW_b\}$ ;
- 8.3.1.22  $SIG_{t,d,k}$ , which designates the amount of *energy* that a *boundary entity resource* is scheduled to import from *intertie zone* source bus  $d \in DI$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,d}^E$ ;
- 8.3.1.23  $S10NIG_{t,d,k}$ , which designates the amount of non-synchronized *ten-minute operating reserve* that a *boundary entity resource* is scheduled to provide from *intertie zone* source bus  $d \in DI$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,d}^{10N}$ ;
- 8.3.1.24  $S30RIG_{t,d,k}$ , which designates the amount of *thirty-minute operating reserve* that a *boundary entity resource* is scheduled to provide from *intertie zone* source bus  $d \in DI$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,d}^{30R}$ ;
- 8.3.1.25  $TB_t$ , which designates any adjustment to the objective function to facilitate pro-rata tie-breaking in time-step  $t \in TS$ , as described in section 8.3.2.1; and
- 8.3.1.26  $ViolCost_t$ , which designates the cost incurred in order to avoid having the schedules violate constraints in time-step  $t \in TS$ , as described in section 8.3.2.3.

8.3.2 The objective function for the Pre-Dispatch Scheduling algorithm shall maximize gains from trade by maximizing the following expression:

$$\sum_{t \in TS} \left( \begin{aligned} &ObjDL_t - ObjHDR_t + ObjXL_t - ObjNDG_t \\ &- ObjDG_t - ObjIG_t - TB_t - ViolCost_t \end{aligned} \right)$$

where:

$$ObjDL_t = \sum_{b \in B^{DL}} \left( \begin{aligned} &\sum_{j \in J_{t,b}^E} SDL_{t,b,j} \cdot PDL_{t,b,j} - \sum_{j \in J_{t,b}^{A0S}} S10SDL_{t,b,j} \cdot P10SDL_{t,b,j} - \\ &\sum_{j \in J_{t,b}^{A0N}} S10NDL_{t,b,j} \cdot P10NDL_{t,b,j} - \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,j} \cdot P30RDL_{t,b,j} \end{aligned} \right);$$

$$ObjHDR_t = \sum_{b \in B^{HDR}} \left( \sum_{j \in J_{t,b}^E} SHDR_{t,b,j} \cdot PHDR_{t,b,j} \right);$$

$$ObjXL_t = \sum_{d \in DX} \left( \begin{aligned} &\sum_{j \in J_{t,d}^E} SXL_{t,d,j} \cdot PXL_{t,d,j} - \sum_{j \in J_{t,d}^{A0N}} S10NXL_{t,d,j} \cdot P10NXL_{t,d,j} \\ &- \sum_{j \in J_{t,d}^{30R}} S30RXL_{t,d,j} \cdot P30RXL_{t,d,j} \end{aligned} \right);$$

$$ObjNDG_t = \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{t,b}^E} SNDG_{t,b,k} \cdot PNDG_{t,b,k} \right);$$

$$\begin{aligned} ObjDG_t = & \sum_{b \in B^{DG}} \left( \begin{aligned} &\sum_{k \in K_{t,b}^E} SDG_{t,b,k} \cdot PDG_{t,b,k} + \sum_{k \in K_{t,b}^{A0S}} S10SDG_{t,b,k} \cdot P10SDG_{t,b,k} + \\ &\sum_{k \in K_{t,b}^{A0N}} S10NDG_{t,b,k} \cdot P10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \cdot P30RDG_{t,b,k} \end{aligned} \right) + \sum_{b \in B^{NQS}} \left( \begin{aligned} &ODG_{t,b} \cdot MGODG_{t,b} + \\ &IDG_{t,b} \cdot SUAdjDG_{t,b}^{T_{t,b}} \end{aligned} \right); \end{aligned}$$

and

$$ObjIG_t = \sum_{d \in DI} \left( \begin{aligned} &\sum_{k \in K_{t,d}^E} SIG_{t,d,k} \cdot PIG_{t,d,k} + \sum_{k \in K_{t,d}^{A0N}} S10NIG_{t,d,k} \cdot P10NIG_{t,d,k} \\ &+ \sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \cdot P30RIG_{t,d,k} \end{aligned} \right).$$

8.3.2.1 The tie-breaking term  $TB_t$  shall sum a term for each *bid* or *offer* lamination. For each lamination, this term shall be the product of a

small penalty cost and the quantity of the lamination scheduled. The penalty cost shall be calculated by multiplying a base penalty cost of  $TBPen$  by the amount of the lamination scheduled and then dividing by the maximum amount that could have been scheduled. That is:

$$TB_t = TBDL_t + TBHDR_t + TBXL_t + TBNDG_t + TBDG_t + TBIG_t$$

Where

$$TBDL_t = \sum_{b \in B^{DL}} \left( \sum_{j \in J_{tb}^E} \left( \frac{(SDL_{t,b,j})^2 \cdot TBPen}{QDL_{t,b,j}} \right) + \sum_{j \in J_{tb}^{10S}} \left( \frac{(S10SDL_{t,b,j})^2 \cdot TBPen}{Q10SDL_{t,b,j}} \right) + \sum_{j \in J_{tb}^{10N}} \left( \frac{(S10NDL_{t,b,j})^2 \cdot TBPen}{Q10NDL_{t,b,j}} \right) + \sum_{j \in J_{tb}^{30R}} \left( \frac{(S30RDL_{t,b,j})^2 \cdot TBPen}{Q30RDL_{t,b,j}} \right) \right);$$

$$TBHDR_t = \sum_{b \in B^{HDR}} \left( \sum_{j \in J_{tb}^E} \frac{(SHDR_{t,b,j})^2 \cdot TBPen}{QHDR_{t,b,j}} \right);$$

$$TBXL_t = \sum_{d \in DX} \left( \sum_{j \in J_{td}^E} \left( \frac{(SXL_{t,d,j})^2 \cdot TBPen}{QXL_{t,d,j}} \right) + \sum_{j \in J_{td}^{10N}} \left( \frac{(S10NXL_{t,d,j})^2 \cdot TBPen}{Q10NXL_{t,d,j}} \right) + \sum_{j \in J_{td}^{30R}} \left( \frac{(S30RXL_{t,d,j})^2 \cdot TBPen}{Q30RXL_{t,d,j}} \right) \right);$$

$$TBNDG_t = \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{tb}^E} \left( \frac{(SNDG_{t,b,k})^2 \cdot TBPen}{QNDG_{t,b,k}} \right) \right);$$

$$TBDG_t = \sum_{b \in B^{DG}} \left( \sum_{k \in K_{tb}^E} \left( \frac{(SDG_{t,b,k})^2 \cdot TBPen}{QDG_{t,b,k}} \right) + \sum_{k \in K_{tb}^{10S}} \left( \frac{(S10SDG_{t,b,k})^2 \cdot TBPen}{Q10SDG_{t,b,k}} \right) + \sum_{k \in K_{tb}^{10N}} \left( \frac{(S10NDG_{t,b,k})^2 \cdot TBPen}{Q10NDG_{t,b,k}} \right) + \sum_{k \in K_{tb}^{30R}} \left( \frac{(S30RDG_{t,b,k})^2 \cdot TBPen}{Q30RDG_{t,b,k}} \right) \right);$$

and

$$TBIG_t = \sum_{d \in DI} \left( \sum_{k \in K_{td}^E} \left( \frac{(SIG_{t,d,k})^2 \cdot TBPen}{QIG_{t,d,k}} \right) + \sum_{k \in K_{td}^{10N}} \left( \frac{(S10NIG_{t,d,k})^2 \cdot TBPen}{Q10NIG_{t,d,k}} \right) + \sum_{k \in K_{td}^{30R}} \left( \frac{(S30RIG_{t,d,k})^2 \cdot TBPen}{Q30RIG_{t,d,k}} \right) \right).$$



- 8.3.2.2  $ViolCost_t$  shall be calculated for time-step  $t \in TS$  using the following variables:
- 8.3.2.2.1  $SLdViol_{t,i}$ , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{LdViol_t}\}$  of the penalty curve for the *energy* balance constraint allowing under-generation;
  - 8.3.2.2.2  $SGenViol_{t,i}$ , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{GenViol_t}\}$  of the penalty curve for the *energy* balance constraint allowing over-generation;
  - 8.3.2.2.3  $S10SViol_{t,i}$ , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{10SViol_t}\}$  of the penalty curve for the synchronized *ten-minute operating reserve* requirement;
  - 8.3.2.2.4  $S10RViol_{t,i}$ , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{10RViol_t}\}$  of the penalty curve for the total *ten-minute operating reserve* requirement;
  - 8.3.2.2.5  $S30RViol_{t,i}$ , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{30RViol_t}\}$  of the penalty curve for the *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement;
  - 8.3.2.2.6  $SREG10RViol_{r,t,i}$ , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{REG10RViol_t}\}$  of the penalty curve for violating the area total *ten-minute operating reserve* minimum requirement in region  $r \in ORREG$ ;
  - 8.3.2.2.7  $SREG30RViol_{r,t,i}$ , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{REG30RViol_t}\}$  of the penalty curve for violating the area *thirty-minute operating reserve* minimum requirement in region  $r \in ORREG$ ;
  - 8.3.2.2.8  $SXREG10RViol_{r,t,i}$ , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{XREG10RViol_t}\}$  of the penalty curve for violating the area total *ten-*

*minute operating reserve* maximum restriction in region  $r \in ORREG$ ;

- 8.3.2.2.9  $SXREG30RViol_{r,t,i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{SXREG30RViol_t}\}$  of the penalty curve for violating the area *thirty-minute operating reserve* maximum restriction in region  $r \in ORREG$ ;
- 8.3.2.2.10  $SPreITLViol_{f,t,i}$  , which designates the violation variable affiliated with segment  $I \in \{1, \dots, N_{PreITLViol_{f,t}}\}$  of the penalty curve for violating the pre-contingency transmission limit for *facility*  $f \in F$ ;
- 8.3.2.2.11  $SITLViol_{c,f,t,i}$  , which designates the violation variable affiliated with segment  $I \in \{1, \dots, N_{ITLViol_{c,f,t}}\}$  of the penalty curve for violating the post-contingency transmission limit for *facility*  $f \in F$  and contingency  $c \in C$ ;
- 8.3.2.2.12  $SPreXTLViol_{z,t,i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{PreXTLViol_{z,t}}\}$  of the penalty curve for violating the import/export limit affiliated with *intertie* limit constraint  $z \in Z_{Sch}$ ;
- 8.3.2.2.13  $SNIUViol_{t,i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{NIUViol_t}\}$  of the penalty curve for exceeding the net interchange increase limit between time-steps  $(t-1)$  and  $t$ ;
- 8.3.2.2.14  $SNIDViol_{t,i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{NIDViol_t}\}$  of the penalty curve for exceeding the net interchange decrease limit between time-steps  $(t-1)$  and  $t$ ;
- 8.3.2.2.15  $SMaxDelViol_{t,b,i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{MaxDelViol_t}\}$  of the penalty curve for exceeding the *maximum daily energy limit* constraint for a *resource* at bus  $b \in B^{ELR}$ ;
- 8.3.2.2.16  $SMinDelViol_{t,b,i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{MinDelViol_t}\}$  of the penalty curve for violating the *minimum daily energy limit* constraint for a *resource* at bus  $b \in B^{HE}$ ;

- 8.3.2.2.17  $SSMaxDelViol_{t,s,i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{SSMaxDelViol_t}\}$  of the penalty curve for exceeding the shared *maximum daily energy limit* constraint for *dispatchable hydroelectric generation resources* in set  $s \in SHE$ ;
- 8.3.2.2.18  $SSMinDelViol_{t,s,i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{SSMinDelViol_t}\}$  of the penalty curve for violating the shared *minimum daily energy limit* constraint for *dispatchable hydroelectric generation resources* in set  $s \in SHE$ ;
- 8.3.2.2.19  $SOGenLnkViol_{t,(b_1,b_2),i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{SOGenLnkViol_t}\}$  of the penalty curve for violating the linked *dispatchable hydroelectric generation resources* constraint by over-generating the downstream *resource*, for  $(b_1, b_2) \in LNK$  such that  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ ; and
- 8.3.2.2.20  $SUGenLnkViol_{t,(b_1,b_2),i}$  , which designates the violation variable affiliated with segment  $i \in \{1, \dots, N_{SUGenLnkViol_t}\}$  of the penalty curve for violating the linked *dispatchable hydroelectric generation resources* constraint by under-generating the downstream *resource*, for  $(b_1, b_2) \in LNK$  such that  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ .

8.3.2.3  $ViolCost_t$  shall be calculated as follows:

$$\begin{aligned}
 ViolCost_t = & \sum_{i=1..N_{LdViol_t}} SLdViol_{t,i} \cdot PLdViolSch_{t,i} - \\
 & \sum_{i=1..N_{GenViol_t}} SGenViol_{t,i} \cdot PGenViolSch_{t,i} + \sum_{i=1..N_{10SViol_t}} S10SViol_{t,i} \cdot P10SViolSch_{t,i} + \\
 & \sum_{i=1..N_{10RViol_t}} S10RViol_{t,i} \cdot P10RViolSch_{t,i} + \sum_{i=1..N_{30RViol_t}} S30RViol_{t,i} \cdot P30RViolSch_{t,i} + \\
 & \sum_{r \in ORREG} \left( \sum_{i=1..N_{REG10RViol_t}} SREG10RViol_{r,t,i} \cdot PREG10RViolSch_{t,i} \right) + \\
 & \sum_{r \in ORREG} \left( \sum_{i=1..N_{REG30RViol_t}} SREG30RViol_{r,t,i} \cdot PREG30RViolSch_{t,i} \right) + \\
 & \sum_{r \in ORREG} \left( \sum_{i=1..N_{XREG10RViol_t}} SXREG10RViol_{r,t,i} \cdot PXREG10RViolSch_{t,i} \right) + \\
 & \sum_{r \in ORREG} \left( \sum_{i=1..N_{XREG30RViol_t}} SXREG30RViol_{r,t,i} \cdot PXREG30RViolSch_{t,i} \right) + \dots \\
 & + \sum_{f \in F_t} \left( \sum_{i=1..N_{PreITLViol_{f,t}}} SPreITLViol_{f,t,i} \cdot PPreITLViolSch_{f,t,i} \right) \\
 & + \sum_{c \in C} \sum_{f \in F_{t,c}} \left( \sum_{i=1..N_{ITLViol_{c,f,t}}} SITLViol_{c,f,t,i} \cdot PITLViolSch_{c,f,t,i} \right) \\
 & + \sum_{z \in Z_{Sch}} \left( \sum_{i=1..N_{PreXTLViol_{z,t}}} SPreXTLViol_{z,t,i} \cdot PPreXTLViolSch_{z,t,i} \right) \\
 & + \sum_{i=1..N_{NIUViol_t}} SNIUViol_{t,i} \cdot PNIUViolSch_{t,i} + \sum_{i=1..N_{NIDViol_t}} SNIDViol_{t,i} \cdot PNIDViolSch_{t,i}
 \end{aligned}$$

$$\begin{aligned}
& + \sum_{b \in B^{ELR}} \left( \sum_{i=1..N_{MaxDelViol_t}} SMaxDelViol_{t,b,i} \cdot PMaxDelViolSch_{t,b,i} \right) \\
& + \sum_{b \in B^{HE}} \left( \sum_{i=1..N_{MinDelViol_t}} SMinDelViol_{t,b,i} \cdot PMinDelViolSch_{t,b,i} \right) \\
& + \sum_{s \in SHE} \left( \sum_{i=1..N_{SMaxDelViol_t}} SSMaxDelViol_{t,s,i} \cdot PSMaxDelViolSch_{t,s,i} \right) \\
& + \sum_{s \in SHE} \left( \sum_{i=1..N_{SMinDelViol_t}} SSMinDelViol_{t,s,i} \cdot PSMinDelViolSch_{t,s,i} \right) \\
& + \sum_{(b_1, b_2) \in LNK} \left( \sum_{i=1..N_t} SOGenLnkViol_{t,(b_1, b_2),i} \cdot POGenLnkViolSch_{t,i} \right) / \\
& + \sum_{(b_1, b_2) \in LNK} \left( \sum_{i=1..N_t} SUGenLnkViol_{t,(b_1, b_2),i} \cdot PUGenLnkViolSch_{t,i} \right).
\end{aligned}$$

## 8.4 Constraints

8.4.1 The constraints described in sections 8.5 – 8.7 apply to the optimization function in the Pre-Dispatch Scheduling algorithm.

## 8.5 Dispatch Data Constraints Applying to Individual Hours

8.5.1 Scheduling Variable Bounds

8.5.1.1 A Boolean variable  $ODG_{t,b}$  indicates whether the *resource* at bus  $b \in B^{DG}$  is committed in time-step  $t \in TS$ . A value of zero indicates that a *resource* is not committed, while a value of one indicates that it is committed. Therefore:

$$ODG_{t,b} \in \{0,1\} \text{ for all time-steps } t \in TS \text{ and all buses } b \in B^{DG}.$$

8.5.1.2 *Reliability must-run resources* are considered committed for all must-run hours.

8.5.1.3 *Resources* providing *regulation* are considered committed for all the hours that they are regulating.

8.5.1.4 *Dispatchable generation resources* that have *minimum loading points*, *start-up offers*, *speed no-load offers*, *minimum generation block run-times* and *minimum generation block down-times* equal to zero shall be considered committed for all hours.

8.5.1.5 If the *dispatchable generation resource* at bus  $b \in B^{DG}$  is considered committed according to the requirements in sections 8.5.1.2, 8.5.1.3, and 8.5.1.4 in time-step  $t \in TS$  then:

$$ODG_{t,b} = 1$$

8.5.1.6 No schedule shall be negative, nor shall any schedule exceed the quantity *offered* for the respective *energy* and *operating reserve* market. Therefore:

$$\begin{aligned}
 0 \leq SDL_{t,b,j} &\leq QDL_{t,b,j} && \text{for all } b \in B^{DL}, j \in J_{t,b}^E; \\
 0 \leq S10SDL_{t,b,j} &\leq Q10SDL_{t,b,j} && \text{for all } b \in B^{DL}, j \in J_{t,b}^{10S}; \\
 0 \leq S10NDL_{t,b,j} &\leq Q10NDL_{t,b,j} && \text{for all } b \in B^{DL}, j \in J_{t,b}^{10N}; \\
 0 \leq S30RDL_{t,b,j} &\leq Q30RDL_{t,b,j} && \text{for all } b \in B^{DL}, j \in J_{t,b}^{30R}; \\
 0 \leq SHDR_{t,b,j} &\leq QHDR_{t,b,j} && \text{for all } b \in B^{HDR}, j \in J_{t,b}^E; \\
 0 \leq SXL_{t,d,j} &\leq QXL_{t,d,j} && \text{for all } d \in DX, j \in J_{t,d}^E; \\
 0 \leq S10NXL_{t,d,j} &\leq Q10NXL_{t,d,j} && \text{for all } d \in DX, j \in J_{t,d}^{10N}; \\
 0 \leq S30RXL_{t,d,j} &\leq Q30RXL_{t,d,j} && \text{for all } d \in DX, j \in J_{t,d}^{30R}; \\
 0 \leq SNDG_{t,b,k} &\leq QNDG_{t,b,k} && \text{for all } b \in B^{NDG}, k \in K_{t,b}^E; \\
 0 \leq SIG_{t,d,k} &\leq QIG_{t,d,k} && \text{for all } d \in DI, k \in K_{t,d}^E; \\
 0 \leq S10NIG_{t,d,k} &\leq Q10NIG_{t,d,k} && \text{for all } d \in DI, k \in K_{t,d}^{10N}; \text{ and} \\
 0 \leq S30RIG_{t,d,k} &\leq Q30RIG_{t,d,k} && \text{for all } d \in DI, k \in K_{t,d}^{30R} \\
 &&& \text{for all time-steps } t \in TS.
 \end{aligned}$$

8.5.1.7 *Generation resources* may be scheduled for *energy* and/or *operating reserve* only if their commitment status is equal to 1. Therefore, for all time-steps  $t \in TS$ :

$$0 \leq SDG_{t,b,k} \leq ODG_{t,b} \cdot QDG_{t,b,k} \quad \text{for all } b \in B^{DG}, k \in K_{t,b}^E;$$

$$0 \leq S10SDG_{t,b,k} \leq ODG_{t,b} \cdot Q10SDG_{t,b,k} \quad \text{for all } b \in B^{DG}, k \in K_{t,b}^{10S};$$

$$0 \leq S10NDG_{t,b,k} \leq ODG_{t,b} \cdot Q10NDG_{t,b,k} \quad \text{for all } b \in B^{DG}, k \in K_{t,b}^{10N};$$

and

$$0 \leq S30RDG_{t,b,k} \leq ODG_{t,b} \cdot Q30RDG_{t,b,k} \quad \text{for all } b \in B^{DG}, k \in K_{t,b}^{30R}.$$

## 8.5.2 Resource Minimums and Maximums for Energy

8.5.2.1 A constraint shall limit schedules for *dispatchable loads* within their minimum and maximum consumption for a time-step. For all time-steps  $t \in TS$  and all buses  $b \in B^{DL}$ :

$$MinDL_{t,b} \leq \sum_{j \in J_{t,b}^E} SDL_{t,b,j} \leq MaxDL_{t,b}.$$

8.5.2.2 The non-*dispatchable* portion of a *dispatchable load* shall always be scheduled. For all time-steps  $t \in TS$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{t,b}^E} SDL_{t,b,j} \geq QDLFIRM_{t,b}.$$

8.5.2.3 A constraint shall limit schedules for *non-dispatchable generation resources* within their minimum and maximum output for a time-step. For all time-steps  $t \in TS$  and all buses  $b \in B^{NDG}$ :

$$MinNDG_{t,b} \leq \sum_{k \in K_{t,b}^E} SNDG_{t,b,k} \leq MaxNDG_{t,b}.$$

8.5.2.4 A constraint shall limit schedules for *dispatchable generation resources* within their minimum and maximum output for a time-step. For a *dispatchable variable generation resource*, the maximum schedule shall be limited by its forecast. That is:

For all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$ :

$$AdjMaxDG_{t,b} = \begin{cases} Min(MaxDG_{t,b}, FG_{t,b}) & \text{if } b \in B^{VG} \\ MaxDG_{t,b} & \text{otherwise} \end{cases}$$

and

$$AdjMinDG_{t,b} = Min(MinDG_{t,b}, AdjMaxDG_{t,b}).$$

For all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$ :

$$AdjMinDG_{t,b} \leq MinQDGC_b \cdot ODG_{t,b} + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \leq AdjMaxDG_{t,b}.$$

- 8.5.2.5 If the commitment status,  $ODG_{t,b}$ , of a *dispatchable generation resource* is equal to 1 and if this status is inconsistent with the adjusted minimum and maximum constraints,  $MinQDGC_b > AdjMaxDG_{t,b}$ , then the commitment status value,  $ODG_{t,b}$ , shall be changed to a value between 0 and 1.
- 8.5.2.6 If the total *offered* quantity does not exceed the minimum,  $MinQDGC_b + \sum_{k \in K_{t,b}^E} QDG_{t,b,k} < AdjMinDG_{t,b}$ , then the *resource* shall receive a schedule of zero.
- 8.5.2.7 Minimum and maximum limits placed on *hourly demand response resource* schedules for the purposes of reflecting activation/non-activation decisions shall be respected. For all time-steps  $t \in TS$  and all buses  $b \in B^{HDR}$ :

$$MinHDR_{t,b} \leq \sum_{j \in J_{t,b}^E} SHDR_{t,b,j} \leq MaxHDR_{t,b}.$$

### 8.5.3 Off-Market Transactions

- 8.5.3.1 For all time-steps  $t \in TS$  and all *intertie zone* buses corresponding to an inadvertent *energy* payback export transaction  $d \in DX_t^{INP}$ :

$$\sum_{j \in J_{t,d}^E} SXL_{t,d,j} = \sum_{j \in J_{t,d}^E} QXL_{t,d,j}.$$



- 8.5.3.2 For all time-steps  $t \in TS$  and all *intertie zone* buses corresponding to an inadvertent *energy* payback import transaction  $d \in DI_t^{INP}$ :

$$\sum_{k \in K_{t,d}^E} SIG_{t,d,k} = \sum_{k \in K_{t,d}^E} QIG_{t,d,k}$$

- 8.5.3.3 For all time-steps  $t \in TS$  and all *intertie zone* buses corresponding to an *emergency energy* export  $d \in DX_t^{EM}$ :

$$\sum_{j \in J_{t,d}^E} SXL_{t,d,j} = \sum_{j \in J_{t,d}^E} QXL_{t,d,j}$$

- 8.5.3.4 For all time-steps  $t \in TS$  and all *intertie zone* buses corresponding to *emergency energy* import  $d \in DI_t^{EM}$ :

$$\sum_{k \in K_{t,d}^E} SIG_{t,d,k} = \sum_{k \in K_{t,d}^E} QIG_{t,d,k}$$

#### 8.5.4 Intertie Minimum and Maximum Constraints

- 8.5.4.1 A constraint shall limit export schedules beyond the first two forecast hours of the pre-dispatch look-ahead period to the corresponding *day-ahead market* schedules for export transactions, subject to Chapter 7, section 5.2.2. For time-step  $t \in \{4, \dots, n_{LAP}\}$  and *intertie zone* sink bus  $d \in DX$  such that  $d \notin DX_t^{CAPEX} \cup DX_t^{EM} \cup DX_t^{INP}$ :

$$\sum_{j \in J_{t,d}^E} SXL_{t,d,j} \leq SXL T_{t,d}^{DAM};$$

$$\sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} \leq S10NXL T_{t,d}^{DAM};$$

and

$$\sum_{j \in J_{t,d}^{30R}} S30RXL_{t,d,j} \leq S30RXL T_{t,d}^{DAM}.$$

- 8.5.4.2 Import *offers* with no *day-ahead market* schedule may be evaluated beyond the first two forecast hours of the look-ahead period for the purpose of *reliability*.

- 8.5.4.3 A constraint shall limit import schedules beyond the first two forecast hours of the pre-dispatch look-ahead period to the corresponding *day-ahead market* schedules for import transactions plus any additional *offered* quantities permitted for *reliability* reasons, with the exception of transactions flagged as capacity imports or off-market transactions, subject to Chapter 7, section 5.2.2. For time-step  $t \in \{4, \dots, n_{LAP}\}$  and *intertie zone* source bus  $d \in DI$  such that  $d \notin DI_t^{CAPEX} \cup DI_t^{EM} \cup DI_t^{INP}$ :

$$\sum_{k \in K_{t,d}^E} SIG_{t,d,k} \leq SIG_{t,d}^{DAM} + SIG_{t,d}^{EXTRA};$$

$$\sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \leq S10NIG_{t,d}^{DAM} + S10NIG_{t,d}^{EXTRA};$$

and

$$\sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \leq S30RIG_{t,d}^{DAM} + S30RIG_{t,d}^{EXTRA}.$$

- 8.5.4.4 A constraint shall limit *intertie* schedules as a result of *intertie* curtailments. For *intertie zone* sink bus  $d \in DX$  and time-step  $t \in TS$ :

$$ICMinXL_{t,d} \leq \sum_{j \in J_{t,d}^E} SXL_{t,d,j} \leq ICMaXL_{t,d}.$$

- 8.5.4.4.1 For *intertie zone* source bus  $d \in DI$  and time-step  $t \in TS$ :

$$ICMinIG_{t,d} \leq \sum_{k \in K_{t,d}^E} SIG_{t,d,k} \leq ICMaIG_{t,d};$$

$$ICMin10NIG_{t,d} \leq \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \leq ICMa10NIG_{t,d};$$

and

$$ICMin30RIG_{t,d} \leq \sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \leq ICMa30RIG_{t,d}.$$

## 8.5.5 Operating Reserve Requirements

- 8.5.5.1 The total synchronized *ten-minute operating reserve*, non-synchronized *ten-minute operating reserve* and *thirty-minute*

*operating reserve* scheduled from a *dispatchable load* shall not exceed:

8.5.5.1.1 the *dispatchable load's* ramp capability over 30 minutes;

8.5.5.1.2 the total scheduled load less the non-*dispatchable* portion; and

8.5.5.1.3 the remaining portion of its capacity that is *dispatchable* after considering minimum load consumption constraints.

8.5.5.1.4 These restrictions shall be enforced by the following constraints for all time-steps  $t \in TS$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} + \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} + \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,j} \leq 30 \cdot ORRD L_b;$$

$$\sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} + \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} + \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,j} \leq \sum_{j \in J_{t,b}^E} SDL_{t,b,j} - QDLFIRM_{t,b};$$

and

$$\sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} + \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} + \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,j} \leq \sum_{j \in J_{t,b}^E} SDL_{t,b,j} - MinDL_{t,b}.$$

8.5.5.2 The amount of both synchronized and non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide shall not exceed the amount by which the *dispatchable load* can decrease its load over 10 minutes, as limited by its *operating reserve* ramp rate. This restriction shall be enforced by the following constraint for all time-steps  $t \in TS$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} + \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} \leq 10 \cdot ORRD L_b.$$

8.5.5.3 The total non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* scheduled for an hour shall not exceed total scheduled exports. This restriction shall be enforced by the following constraint for all all time-steps  $t \in TS$  and all *inertie zone* sink buses  $d \in DX$ :

$$\sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} + \sum_{j \in J_{t,d}^{30R}} S30RXL_{t,d,j} \leq \sum_{j \in J_{t,d}^E} SXL_{t,d,j}$$

- 8.5.5.4 The total *operating reserve* scheduled from a committed *dispatchable generation resource* shall not exceed that *resource's*: (i) ramp capability over 30 minutes; (ii) remaining capacity; and (iii) unscheduled capacity. These restrictions shall be enforced by the following constraints for all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \leq 30 \cdot ORRDG_b;$$

$$\sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \leq \sum_{k \in K_{t,b}^E} (QDG_{t,b,k} - SDG_{t,b,k});$$

and

$$\sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \leq AdjMaxDG_{t,b} - \sum_{k \in K_{t,b}^E} SDG_{t,b,k} - MinQDGC_b.$$

- 8.5.5.5 The amount of both synchronized and non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall not exceed the amount by which the *resource* can increase its output over 10 minutes, as limited by its *operating reserve* ramp rate. This restriction shall be enforced by the following constraint for all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \leq 10 \cdot ORRDG_b.$$

- 8.5.5.6 The amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall be limited by its *reserve loading point* for synchronized *ten-minute operating reserve*. This restriction shall be enforced by the following

constraint for all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$  with  $RLP10S_{t,b} > 0$ :

$$\sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \leq \left( MinQDGC_b \cdot ODG_{t,b} + \sum_{k \in K_{t,b}^B} SDG_{t,b,k} \right) \cdot \left( \frac{1}{RLP10S_{t,b}} \right) \cdot \left( \min \left\{ 10 \cdot ORRDG_b, \sum_{k \in K_{t,b}^{10S}} Q10SDG_{t,b,k} \right\} \right).$$

- 8.5.5.7 The amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall be limited by its *reserve loading point* for *thirty-minute operating reserve*. This restriction shall be enforced by the following constraint for all all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$  with  $RLP30R_{t,b} > 0$ :

$$\sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \leq \left( MinQDGC_b \cdot ODG_{t,b} + \sum_{k \in K_{t,b}^B} SDG_{t,b,k} \right) \cdot \left( \frac{1}{RLP30R_{t,b}} \right) \cdot \left( \min \left\{ 30 \cdot ORRDG_b, \sum_{k \in K_{t,b}^{30R}} Q30RDG_{t,b,k} \right\} \right).$$

- 8.5.5.8 The total non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* scheduled for an hour shall not exceed the remaining maximum import *offers* minus scheduled *energy* imports. This restriction shall be enforced by the following constraint for all time-steps  $t \in TS$  and all *intertie zone* source buses  $d \in DI$ :

$$\sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} + \sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \leq \sum_{k \in K_{t,d}^B} (QIG_{t,d,k} - SIG_{t,d,k}).$$

## 8.5.6 Pseudo-Units

- 8.5.6.1 A constraint shall be required to calculate physical *generation resource* schedules from *pseudo-unit* schedules using the steam turbine *resource's* shares in the operating regions of the *pseudo-unit* determined in section 15. For all time-steps  $t \in TS$  and *pseudo-unit* buses  $b \in B^{PSU}$ :

$$SCT_{t,b} = (1 - STShareMLP_b) \cdot MinQDGC_b \cdot ODG_{t,b} + (1 - STShareDR_b) \cdot \left( \sum_{k \in K_{t,b}^{DR}} SDG_{t,b,k} \right),$$

and for all time-steps  $t \in TS$  and steam turbine *resources*  $p \in PST$ :

$$SST_{t,p} = \sum_{b \in B_p^{ST}} \left( STShareMLP_b \cdot MinQDGC_b \cdot ODG_{t,b} + STShareDR_b \cdot \left( \sum_{k \in K_{t,b}^{DR}} SDG_{t,b,k} \right) + \sum_{k \in K_{t,b}^{DF}} SDG_{t,b,k} \right).$$

- 8.5.6.2 Maximum constraints shall be enforced on the operating region to which they apply for both *energy* and *operating reserve* schedules. For all time-steps  $t \in TS$  and *pseudo-unit* buses  $b \in B^{PSU}$ :

$$MinQDGC_b \cdot ODG_{t,b} \leq MaxMLP_{t,b},$$

$$\sum_{k \in K_{t,b}^{DR}} SDG_{t,b,k} \leq MaxDR_{t,b},$$

$$\sum_{k \in K_{t,b}^{DF}} SDG_{t,b,k} \leq MaxDF_{t,b},$$

and

$$\begin{aligned} \sum_{k \in K_{t,b}^B} SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \\ + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \leq MaxDR_{t,b} + MaxDF_{t,b}. \end{aligned}$$

- 8.5.6.3 For a *pseudo-unit* that cannot provide *ten-minute operating reserve* from its duct firing region, constraints shall limit the *pseudo-unit* from being scheduled in its duct firing region whenever the *pseudo-unit* is

scheduled for *ten-minute operating reserve*. For all all time-steps  $t \in TS$  and *pseudo-unit* buses  $b \in B^{NO10DF}$ :

$$O10R_{t,b} \in \{0,1\},$$

and

$$\sum_{k \in K_{t,b}^B} SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \leq MaxDR_{t,b} + (1 - O10R_{t,b}) \cdot MaxDF_{t,b}$$

8.5.6.3.1 For all time-steps  $t \in TS$ , *pseudo-unit* buses  $b \in B^{NO10DF}$ , and laminations  $k \in K_{t,b}^{10S}$ :

$$S10SDG_{t,b,k} \leq O10R_{t,b} \cdot Q10SDG_{t,b,k}.$$

8.5.6.3.2 For all time-steps  $t \in TS$ , *pseudo-unit* buses  $b \in B^{NO10DF}$ , and laminations  $k \in K_{t,b}^{10N}$ :

$$S10NDG_{t,b,k} \leq O10R_{t,b} \cdot Q10NDG_{t,b,k}.$$

8.5.6.4 For the purposes of the *energy* balance constraint in section 8.7.1 and the transmission constraints in section 8.7.3, the combustion turbine *resource's* schedule for the *pseudo-unit* at bus  $b \in B^{PSU}$  in in time-step  $t \in TS$  will be equal to:

8.5.6.4.1  $SCT_{t,b}$  if the *pseudo-unit* is scheduled at or above *minimum loading point*;

8.5.6.4.2  $RampCTC_{b,w}^m$  if the *pseudo-unit* is scheduled to reach *minimum loading point* in *thermal state*  $m \in THERM$  in time-step  $t + w$  for  $w \in \{1, \dots, RampHrsC_b^m\}$ ; or

8.5.6.4.3 0 otherwise.

8.5.6.5 For the purposes of the *energy* balance constraint in section 8.7.1 and the transmission constraints in section 8.7.3, the steam turbine *resource's* schedule for  $p \in PST$  shall be equal to  $SST_{h,p}$  plus any contribution from *pseudo-unit*  $b \in B_p^{ST}$  ramping to *minimum loading point* as given by  $RampSTC_{b,w}^m$  for a *pseudo-unit* scheduled to reach *minimum loading point* in *thermal state*  $m \in THERM$  in time-step  $(t + w)$  for  $w \in \{1, \dots, RampHrsC_b^m\}$ .

## 8.5.7 Dispatchable Hydroelectric Generation Resources

- 8.5.7.1 A *dispatchable* hydroelectric *generation resource* shall be scheduled to at least its *hourly must-run* quantity. For all time-steps  $t \in TS$  and *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$ :

$$ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \geq MinHMR_{t,b}.$$

- 8.5.7.2 A *dispatchable* hydroelectric *generation resource* shall either be scheduled to 0 or to at least its *minimum hourly output*. For all time-steps  $t \in TS$  and all hydroelectric *generation resource* buses  $b \in B^{HE}$ :

$$OHO_{t,b} \in \{0,1\};$$

$$ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \geq MinHO_{t,b} \cdot OHO_{t,b};$$

and for all  $k \in K_{t,b}^E$ :

$$0 \leq SDG_{t,b,k} \leq OHO_{t,b} \cdot QDG_{t,b,k}.$$

- 8.5.7.3 A *dispatchable* hydroelectric *generation resource* shall not be scheduled within its *forbidden regions*. For *dispatch days*  $q \in DAYS$ , all time-steps  $t \in TS$  in *dispatch day*  $q$ , all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$  and all  $i \in \{1, \dots, NFor_{q,b}\}$ :

$$OFR_{t,b,i} \in \{0,1\};$$

$$\begin{aligned} & ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \\ & \leq OFR_{t,b,i} \cdot ForL_{q,b,i} + (1 - OFR_{t,b,i}) \\ & \quad \cdot \left( MinQDGC_b + \sum_{k \in K_{t,b}^E} QDG_{t,b,k} \right); \end{aligned}$$

and

$$ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \geq (1 - OFR_{t,b,i}) \cdot ForU_{q,b,i}.$$

## 8.5.8 Linked Wheeling Through Transactions

- 8.5.8.1 The amount of scheduled export *energy* must be equal to the amount of scheduled import *energy* for *linked wheeling through transactions*.



For all time-steps  $t \in TS$  and all linked *boundary entity resource* buses  $(dx, di) \in L_t$ :

$$\sum_{j \in J_{t,dx}^B} SXL_{t,dx,j} = \sum_{k \in K_{t,di}^B} SIG_{t,di,k}.$$

## 8.6 Dispatch Data Inter-Hour/Multi-Hour Constraints

### 8.6.1 Energy Ramping

- 8.6.1.1 For *dispatchable loads*, the constraints in section 8.6.1.5 and section 8.6.2.1 use  $URRDL_b$  to represent a ramp up rate selected from  $URRDL_{t,b,w}$  and uses  $DRRDL_b$  to represent a ramp down rate selected from  $DRRDL_{t,b,w}$ .
- 8.6.1.2 For *dispatchable generation resources*, the constraints in section 8.6.1.7 and section 8.6.2.2 use  $URRDG_b$  to represent a ramp up rate selected from  $URRDG_{t,b,w}$  and uses  $DRRDG_b$  to represent a ramp down rate selected from  $DRRDG_{t,b,w}$ .
- 8.6.1.3 The *pre-dispatch calculation engine* shall respect the ramping restrictions determined by the up to five *offered* MW quantity, ramp up rate and ramp down rate value sets.
- 8.6.1.4 In all ramping constraints, the schedules for time-step 1 are obtained from the initial scheduling assumptions in section 5.9. For all time-steps  $t \in TS$  the ramping rates in all ramping constraints shall be adjusted to allow the applicable *resource* to:
  - 8.6.1.4.1 ramp down from its lower limit in time-step  $(t - 1)$  to its upper limit in time-step  $t$ ; and
  - 8.6.1.4.2 ramp up from its upper limit in time-step  $(t - 1)$  to its lower limit in time-step  $t$ .
- 8.6.1.5 *Energy* schedules for *dispatchable loads* cannot vary by more than an hour's ramping capability for the applicable *resource*. This constraint

shall be enforced by the following for all time-steps  $t \in TS$  and buses  $b \in B^{DL}$ :

$$\begin{aligned} \sum_{j \in J_{t-1,b}^B} SDL_{t-1,b,j} - 60 \cdot DRRDL_b &\leq \sum_{j \in J_{t,b}^B} SDL_{t,b,j} \\ &\leq \sum_{j \in J_{t-1,b}^B} SDL_{t-1,b,j} + 60 \cdot URRDL_b. \end{aligned}$$

- 8.6.1.6 *Energy* schedules for *hourly demand response resources* cannot vary by more than an hour's ramping capability for the applicable *resource*. This constraint shall be enforced by the following for all time-steps  $t \in TS$  and all buses  $b \in B^{HDR}$ :

$$\begin{aligned} \sum_{j \in J_{t-1,b}^B} (QHDR_{t-1,b,j} - SHDR_{t-1,b,j}) - 60 \cdot URRHDR_b \\ &\leq \sum_{j \in J_{t,b}^B} (QHDR_{t,b,j} - SHDR_{t,b,j}) \\ &\leq \sum_{j \in J_{t-1,b}^B} (QHDR_{t-1,b,j} - SHDR_{t-1,b,j}) + 60 \cdot DRRHDR_b. \end{aligned}$$

- 8.6.1.7 *Energy* schedules for a *dispatchable generation resource* that is committed cannot vary by more than an hour's ramping capability for the applicable *resource*. For all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$ :

- 8.6.1.7.1 For the first hour a *resource* reaches its *minimum loading point*, where  $ODG_{t,b} = 1$ ,  $ODG_{t-1,b} = 0$ , the following constraint shall be applied:

$$0 \leq \sum_{k \in K_{t,b}^B} SDG_{t,b,k} \leq 30 \cdot URRDG_b$$

- 8.6.1.7.2 If the *resource* stays on at or above *minimum loading point* and  $ODG_{t,b} = 1$ ,  $ODG_{t-1,b} = 1$ , the following constraint shall be applied:

$$\begin{aligned} \sum_{k \in K_{t-1,b}^B} SDG_{t-1,b,k} - 60 \cdot DRRDG_b &\leq \sum_{k \in K_{t,b}^B} SDG_{t,b,k} \\ &\leq \sum_{k \in K_{t-1,b}^B} SDG_{t-1,b,k} + 60 \cdot URRDG_b \end{aligned}$$

8.6.1.7.3 For the last hour the *resource* is scheduled at or above *minimum loading point* before being scheduled off, where  $ODG_{t,b} = 1$ ,  $ODG_{t+1,b} = 0$ , the following constraint shall be applied:

$$0 \leq \sum_{k \in K_{t,b}^B} SDG_{t,b,k} \leq 30 \cdot DRRDG_b$$

8.6.1.8 The first and third constraint in section 8.6.1.6 do not apply to a *quick start resource*.

8.6.1.9 For time-steps where *non-quick start resources* are ramping up to *minimum loading point*, *energy* shall be scheduled for these *resources* using the submitted *ramp up energy to minimum loading point*.

## 8.6.2 Operating Reserve Ramping

8.6.2.1 The total synchronized *ten-minute operating reserve*, non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* from *dispatchable loads* shall not exceed the their ramp capability to decrease load consumption and for all time-steps  $t \in TS$  and all buses  $b \in B^{DL}$ :

$$\begin{aligned} \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} + \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} + \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,j} \\ \leq \sum_{j \in J_{t,b}^B} SDL_{t,b,j} - \sum_{j \in J_{t-1,b}^B} SDL_{t-1,b,j} + 60 \cdot DRRDL_b. \end{aligned}$$

8.6.2.2 The total synchronized *ten-minute operating reserve*, non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* from a committed *dispatchable generation resource* shall not exceed its ramp capability to increase generation and for all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$ :

$$\begin{aligned}
& \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \\
& \leq \sum_{k \in K_{t-1,b}^E} SDG_{t-1,b,k} - \sum_{k \in K_{t,b}^E} SDG_{t,b,k} + 60 \cdot URRDG_b; \\
& \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \\
& + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \leq [(t-n) \cdot 60 + 30] \cdot URRDG_b \cdot ODG_{t,b}
\end{aligned}$$

where  $n$  is the time – step of the last start before or in time – step  $t$ , and

$$\begin{aligned}
& \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \\
& + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \leq [(m-t) \cdot 60 + 30] \cdot DRRDG_b \cdot ODG_{t,b}
\end{aligned}$$

where  $m$  is the time-step of the last shutdown in or after time-step  $t$ .

### 8.6.3 Non-Quick Start Resources

8.6.3.1 Schedules for a *non-quick start resource* shall not violate such *resource's minimum generation block run-times, minimum generation block down-times and maximum number of starts per day*.

8.6.3.2 In the first forecast hour of the pre-dispatch look-ahead period, a *resource's* current hours on shall determine any remaining *minimum generation block run-time* to enforce. If  $0 < \text{InitOperHrs}_b < \text{MGBRTDG}_{\text{tod},b}$ , then the *resource* at bus  $b \in B^{NQS}$  has yet to complete its *minimum generation block run-time*, and:

$$ODG_{2,b}, ODG_{3,b}, \dots, ODG_{\min(n_{LAP}, \text{MGBRTDG}_{\text{tod},b} - \text{InitOperHrs}_b + 1),b} = 1.$$

8.6.3.3 In the first forecast hour of the pre-dispatch look-ahead period (i.e. time-step 2), the number of hours a *resource* has been down shall determine any remaining *minimum generation block down-time* to enforce and shall respect the *minimum generation block down-time* for a hot *thermal state*. If  $0 < \text{InitDownHrs}_b < \text{MGBDTDG}_{\text{tod},b}^{\text{HOT}}$ , then the

*resource* at bus  $b \in B^{NQS}$  has yet to complete its *minimum generation block down-time*, and:

$$ODG_{2,b}, ODG_{3,b}, \dots, ODG_{\min(n_{LAP}, MGBDTDG_{tod,b}^{HOT} - InitDownHrs_b + 1),b} = 0.$$

- 8.6.3.4 If  $ODG_{t-1,b} = 0$  and  $ODG_{t,b} = 1$  for time-step  $t \in TS$ , then the *resource* at bus  $b \in B^{NQS}$  has been scheduled to start up during time-step  $t$  and shall be scheduled to remain in operation until it has completed its *minimum generation block run-time* or to the end of the pre-dispatch look-ahead period. Therefore:

$$ODG_{t+1,b}, ODG_{t+2,b}, \dots, ODG_{\min(n_{LAP}, t + MGBRTDGC_b - 1),b} = 1.$$

- 8.6.3.5 If  $ODG_{t-1,b} = 1$  and  $ODG_{t,b} = 0$  for time-step  $t \in TS$ , then the *resource* at bus  $b \in B^{NQS}$  has been scheduled to shut down during time-step  $t$  and shall be scheduled to remain off until it has completed its hot *minimum generation block down-time* or to the end of the pre-dispatch look-ahead period. Therefore:

$$ODG_{t+1,b}, ODG_{t+2,b}, \dots, ODG_{\min(n_{LAP}, t + MGBDTDGC_b^{HOT} - 1),b} = 0.$$

- 8.6.3.6 A Boolean variable  $IDG_{t,b}$  indicates that the *non-quick start resource* at bus  $b \in B^{NQS}$  is scheduled to reach its *minimum loading point* in time-step  $t \in TS$  after being scheduled below its *minimum loading point* in the preceding time-step. A value of zero indicates that a *resource* is not scheduled to reach its *minimum loading point*, while a value of one indicates that it is scheduled to reach its *minimum loading point*. Therefore, for all time-steps  $t \in TS$  and all buses  $b \in B^{NQS}$ :

$$IDG_{t,b} = \begin{cases} 1 & \text{if } ODG_{t-1,b} = 0 \text{ and } ODG_{t,b} = 1 \\ 0 & \text{otherwise.} \end{cases}$$

- 8.6.3.7 A *non-quick start resource* shall not be scheduled more than its *maximum number of starts per day*. For all buses  $b \in B^{NQS}$ :

$$\sum_{t \in TS_{tod}} IDG_{t,b} \leq MaxStartsDG_{tod,b} - NumStarts_{tod,b}.$$

- 8.6.3.7.1 and if the pre-dispatch look-ahead period spans two *dispatch days* then:

$$\sum_{t \in TS_{tom}} IDG_{t,b} \leq MaxStartsDG_{tom,b}.$$

8.6.3.8 For a *non-quick start resource* at bus  $b \in B^{NQS}$  that has been offline  $InitDownHrs_b$  hours, and for future *minimum loading point* time-step  $t \in \{2, \dots, n_{LAP}\}$ , the *pre-dispatch calculation engine* shall assign a *start-up offer* and *ramp energy* to *minimum loading point* profile as follows:

8.6.3.8.1 If  $0 \leq InitDownHrs_b + t - 1 \leq MGBD TDGC_b^{HOT}$ , then the *resource* cannot be scheduled in time-step  $t$ ;

8.6.3.8.2 If  $MGBD TDGC_b^{HOT} < InitDownHrs_b + t - 1 \leq MGBD TDGC_b^{WARM}$ , then the *resource* will be assigned a "HOT" *thermal state* for time-step  $t$  and the *start-up offer*  $SUDG_{t,b}^{HOT}$  shall apply. The *ramp up energy* to *minimum loading point* profile shall be  $RampEC_{b,w}^{HOT}$  for  $w \in \{1, \dots, RampHrsC_b^m\}$ ;

8.6.3.8.3 If  $MGBD TDGC_b^{WARM} < InitDownHrs_b + t - 1 \leq MGBD TDGC_b^{COLD}$ , then the *resource* will be assigned a "WARM" *thermal state* for time-step  $t$  and the *start-up offer*  $SUDG_{t,b}^{WARM}$  shall apply. The *ramp up energy* to *minimum loading point* profile shall be  $RampEC_{b,w}^{WARM}$  for  $w \in \{1, \dots, RampHrsC_b^m\}$ ; and

8.6.3.8.4 If  $MGBD TDGC_b^{COLD} < InitDownHrs_b + t - 1$  then the *resource* will be assigned a "COLD" *thermal state* for time-step  $t$  and the *start-up offer*  $SUDG_{t,b}^{COLD}$  shall apply. The *ramp up energy* to *minimum loading point* profile shall be  $RampEC_{b,w}^{COLD}$  for  $w \in \{1, \dots, RampHrsC_b^m\}$ .

8.6.3.9 For a *non-quick start resource* at bus  $b \in B^{NQS}$  that is in-service as determined by its initial condition, the *pre-dispatch calculation engine* shall assign a *start-up offer* and *ramp up energy* to *minimum loading point* profile associated with the future *thermal state* as specified in section 8.6.3.8.

#### 8.6.4 Energy Limited Resources

8.6.4.1 An *energy limited resource* shall not be scheduled to provide:

8.6.4.1.1 more *energy* than the *maximum daily energy limit* specified for such *resource*; or

8.6.4.1.2 *energy* in amounts that would preclude such *resource* from providing *operating reserve* when activated;

8.6.4.1.3 for all buses  $b \in B^{ELR}$  where an *energy limited resource* is located and all time-steps  $T \in TS_{tod}$ :

$$\begin{aligned} & \sum_{t=2..T} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \\ & + 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k} \right) \\ & + 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k} \right) \\ & - \sum_{i=1..N_{MaxDelViol_T}} SMaxDelViol_{T,b,i} \\ & \leq MaxDEL_{tod,b} - EngyUsed_b. \end{aligned}$$

8.6.4.2 If the pre-dispatch look-ahead period spans two *dispatch days*, the constraints in section 8.6.4.1 shall apply to an *energy limited resource* for each *dispatch day*, and shall consider the amount of *energy* already provided by the *resource* for the current *dispatch day*. Therefore, for all buses  $b \in B^{ELR}$  where an *energy limited resource* is located and all time-steps  $T \in TS_{tom}$ :

$$\begin{aligned} & \sum_{t=t_{tom}..T} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \\ & + 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k} \right) \\ & + 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k} \right) \\ & - \sum_{i=1..N_{MaxDelViol_T}} SMaxDelViol_{T,b,i} \leq MaxDEL_{tom,b}. \end{aligned}$$

where the factors 10 *ORConv* and 30 *ORConv* are applied to scheduled *ten-minute operating reserve* and *thirty-minute operating reserve* for *energy limited resources* to convert MW into MWh. Violation variables for over-scheduling a *resource's maximum daily energy limit* may be used to allow the *pre-dispatch calculation engine* to find a solution.

## 8.6.5 Dispatchable Hydroelectric Generation Resources

8.6.5.1 *Dispatchable hydroelectric generation resources* shall be scheduled for at least their *minimum daily energy limit*. If the pre-dispatch look-ahead period spans two *dispatch days*, the constraint shall be applied for both days. Violation variables for under-scheduling a *resource's minimum daily energy limit* may be used to allow the *pre-dispatch calculation engine* to find a solution. For all *dispatchable hydroelectric generation resource buses*  $b \in B^{HE}$ :

$$\sum_{t \in TS_{tod}} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} + \sum_{i=1..N_{MinDelViol_t}} SMinDelViol_{t,b,i} \right) \geq MinDEL_{tod,b} - EngyUsed_b.$$

8.6.5.1.1 and if the pre-dispatch look-ahead period spans two *dispatch days*, for all hydroelectric *resource buses*  $b \in B^{HE}$ :

$$\sum_{t \in TS_{tom}} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} + \sum_{i=1..N_{MinDelViol_t}} SMinDelViol_{t,b,i} \right) \geq MinDEL_{tom,b}.$$

8.6.5.2 A Boolean variable  $IHE_{t,b,i}$  indicates that a start for the *dispatchable hydroelectric generation resource* at bus  $b \in B^{HE}$  was counted in time-step  $t \in TS$  as a result of the *resource* schedule increasing from below its  $i$ -th *start indication value* to at or above its  $i$ -th start indication for  $i \in \{1, \dots, N_{StartMW_b}\}$ . A value of zero indicates that a start was not counted, while a value of one indicates that a start was



counted. Therefore, for all time-steps  $t \in TS$ , buses  $b \in B^{HE}$  and *start indication values*  $i \in \{1, \dots, NStartMW_b\}$ :

$$IHE_{t,b,i} = \begin{cases} 1 & \text{if } \left( ODG_{t-1,b} \cdot MinQDGC_b + \sum_{k \in K_{t-1,b}^B} SDG_{t-1,b,k} < StartMW_{b,i} \right) \\ & \text{and } \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^B} SDG_{t,b,k} \geq StartMW_{b,i} \right) \\ 0 & \text{otherwise.} \end{cases}$$

- 8.6.5.3 *Dispatchable hydroelectric generation resources* shall not be scheduled to be started more times than permitted by their *maximum number of starts per day*. If the pre-dispatch look-ahead period spans two *dispatch days*, this constraint shall be applied for both days. The following constraint shall apply for all buses  $b \in B^{HE}$ :

$$\sum_{t \in TS_{tod}} \left( \sum_{i=1..NStartMW_b} IHE_{t,b,i} \right) \leq MaxStartsHE_{tod,b} - NumStartsHE_b.$$

- 8.6.5.3.1 and if the pre-dispatch look-ahead period spans two *dispatch days*, for buses  $b \in B^{HE}$ :

$$\sum_{t \in TS_{tom}} \left( \sum_{i=1..NStartMW_b} IHE_{t,b,i} \right) \leq MaxStartsHE_{tom,b}.$$

- 8.6.5.4 The schedules for multiple *dispatchable hydroelectric generation resources* with a registered *forebay* shall not exceed shared *maximum daily energy limits*. If the pre-dispatch look-ahead period spans two *dispatch days*, the constraint shall be applied for both days, where the constraint for today shall consider the amount of *energy* already provided by *resources* with a registered *forebay*. Violation variables for over-scheduling the *maximum daily energy limit* may be used to

allow the *pre-dispatch calculation engine* to find a solution. For all sets  $s \in SHE$  and all time-steps  $T \in TS_{tod}$ :

$$\begin{aligned} & \sum_{t=2..T} \left( \sum_{b \in B_S^{HE}} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \right) \\ & + \sum_{b \in B_S^{HE}} \left( 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k} \right) \right) \\ & + 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k} \right) \\ & - \sum_{i=1..N_{SMaxDelViol_T}} SSMaxDelViol_{T,s,i} \leq MaxSDEL_{tod,s} - EngyUsedSH \end{aligned}$$

8.6.5.4.1 and if the look-ahead period spans two *dispatch days*, then for all sets  $s \in SHE$  and all time-steps  $T \in TS_{tom}$ :

$$\begin{aligned} & \sum_{t=t_{tom}..T} \left( \sum_{b \in B_S^{HE}} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \right) \\ & + \sum_{b \in B_S^{HE}} \left( 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k} \right) \right) \\ & + 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k} \right) \\ & - \sum_{i=1..N_{SMaxDelViol_T}} SSMaxDelViol_{T,s,i} \leq MaxSDEL_{tom,s} \end{aligned}$$

where the factors 10 *ORConv* and 30 *ORConv* shall be applied to scheduled *ten-minute operating reserve* and *thirty-minute operating reserve* to convert MW into MWh.

8.6.5.5 Schedules for multiple *dispatchable hydroelectric generation resources* with a registered *forebay* shall respect shared *minimum daily energy limits*. If the pre-dispatch look-ahead period spans two *dispatch days*, the constraint shall be applied for both days, where the constraint for

today shall consider the amount of *energy* already provided by *resources* with a registered *forebay*. Violation variables for under-scheduling the *minimum daily energy limit* may be used to allow the *pre-dispatch calculation engine* to find a solution. For all sets  $s \in SHE$ :

$$\sum_{t \in TS_{tod}} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) + \sum_{i=1..N_{SMinDelViol_t}} SSMinDelViol_{t,s,i} \right) \geq MinSDEL_{tod,s} - EngyUsed$$

8.6.5.5.1 and if the pre-dispatch look-ahead period spans two *dispatch days*, then for all sets  $s \in SHE$ :

$$\sum_{t \in TS_{tom}} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) + \sum_{i=1..N_{SMinDelViol_t}} SSMinDelViol_{t,s,i} \right) \geq MinSDEL_{tom,s}.$$

- 8.6.5.6 For linked *dispatchable* hydroelectric *generation resources* with a registered *forebay*, *energy* scheduled at the upstream *resource* in one time-step shall result in a proportional amount of *energy* being scheduled at the linked downstream *resource* in the time-step determined by the *time lag*.
- 8.6.5.7 For linked *dispatchable* hydroelectric *generation resources*, time-steps in which the upstream *resources* schedule is not determined in the *pre-dispatch calculation engine* optimization, the constraint shall link either the historical or time-step 1 anticipated production for the upstream *resources* to the schedule for the downstream *resources*.
- 8.6.5.8 For all linked *dispatchable* hydroelectric *generation resources* between upstream *resources*  $b_1 \in B_{up}^{HE}$  and downstream *resources*  $b_2 \in B_{dn}^{HE}$  for  $(b_1, b_2) \in LNKC$  and all time-steps  $t \in TS$  such that  $t \leq LagC_{b_1, b_2} + 1$ :

$$\begin{aligned}
& \sum_{b_2 \in B_{dn}^{HE}} \left( ODG_{t,b_2} \cdot MinQDGC_{b_2} + \sum_{k \in K_{t,b_2}^E} SDG_{t,b_2,k} \right) \\
& \quad - \sum_{i=1..N_{OGenLnkViol_t}} SOGenLnkViol_{t,(b_1,b_2),i} \\
& \quad + \sum_{i=1..N_{UGenLnkViol_t}} SUGenLnkViol_{t,(b_1,b_2),i} \\
& = MWhRatioC_{b_1,b_2} \cdot PastMWh_{t,b_1}.
\end{aligned}$$

8.6.5.9 For linked *dispatchable* hydroelectric *generation resources*, time-steps in which both the upstream and downstream *resource* schedules are determined in the *pre-dispatch calculation engine* optimization, the constraint will link the scheduling variables for both the upstream and downstream *resources*.

8.6.5.10 For all linked *dispatchable* hydroelectric *generation resources* between upstream *resources*  $b_1 \in B_{up}^{HE}$  and downstream *resources*  $b_2 \in B_{dn}^{HE}$  for  $(b_1, b_2) \in LNKC$  and time-steps  $t \in TS$  such that  $t + LagC_{b_1,b_2} \leq n_{LAP}$ :

$$\begin{aligned}
& \sum_{b_2 \in B_{dn}^{HE}} \left( ODG_{t+LagC_{b_1,b_2},b_2} \cdot MinQDGC_{b_2} + \sum_{k \in K_{t+LagC_{b_1,b_2},b_2}^E} SDG_{t+LagC_{b_1,b_2},b_2,k} \right) \\
& \quad - \sum_{i=1..N_{OGenLnkViol_{t+LagC_{b_1,b_2}}}} SOGenLnkViol_{t+LagC_{b_1,b_2},(b_1,b_2),i} \\
& \quad + \sum_{i=1..N_{UGenLnkViol_{t+LagC_{b_1,b_2}}}} SUGenLnkViol_{t+LagC_{b_1,b_2},(b_1,b_2),i} \\
& = MWhRatioC_{b_1,b_2} \cdot \sum_{b_1 \in B_{up}^{HE}} \left( ODG_{t,b_1} \cdot MinQDGC_{b_1} + \sum_{k \in K_{t,b_1}^E} SDG_{t,b_1,k} \right)
\end{aligned}$$

## 8.7 Constraints for Reliability Requirements

### 8.7.1 Energy Balance

8.7.1.1 The total amount of *energy* withdrawals scheduled at load bus  $b \in B$  in time-step  $t \in TS$ ,  $With_{t,b}$  shall be represented by:

$$With_{t,b} = \begin{cases} \sum_{j \in J_{t,b}^E} SDL_{t,b,j} & \text{if } b \in B^{DL} \\ \sum_{j \in J_{t,b}^E} (QHDr_{t,b,j} - SHDr_{t,b,j}) & \text{if } b \in B^{HDR} \end{cases}$$

8.7.1.2 The total amount of export *energy* scheduled at *intertie zone* bus  $d \in DX$  in time-step  $t \in TS$ ,  $With_{t,d}$ , as the exports from Ontario to the *intertie zone* bus shall be represented by:

$$With_{t,d} = \sum_{j \in J_{t,d}^E} SXL_{t,d,j}.$$

8.7.1.3 The total amount of injections scheduled at internal bus  $b \in B$  in time-step  $t \in TS$ ,  $Inj_{t,b}$ , shall be represented by:

$$Inj_{t,b} = OfferInj_{t,b} + RampInj_{t,b}$$

where:

$$OfferInj_{t,b} = \begin{cases} \sum_{k \in K_{t,b}^E} SNDG_{t,b,k} & \text{if } b \in B^{NDG} \\ ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} & \text{if } b \in B^{DG} \end{cases}$$

and

$$RampInj_{t,b} = \begin{cases} \sum_{w=1..min(RampHrsC_b^m, n_{LAP}-t)} RampEC_{b,w}^m \cdot IDG_{t+w,b} & \text{if } b \in B^{NQS} \\ 0 & \text{otherwise} \end{cases}$$

- 8.7.1.4 The total amount of import *energy* scheduled at *intertie zone* bus  $d \in DI$  in time-step  $t \in TS$ ,  $Inj_{t,d}$ , as the imports into Ontario from that *intertie zone* bus shall be represented by:

$$Inj_{t,d} = \sum_{k \in K_{t,d}^B} SIG_{t,d,k}.$$

- 8.7.1.5 Injections and withdrawals at each bus shall be multiplied by one plus the marginal loss factor calculated by the *security* assessment function to reflect the losses or reduction in losses that result when injections or withdrawals occur at locations other than the *reference bus*. These loss-adjusted injections and withdrawals must then be equal to each other after taking into account the adjustment for any discrepancy between total and marginal losses. Load or generation reduction associated with the *demand* constraint violation shall be subtracted from the total load or generation for the *pre-dispatch calculation engine* to produce a solution. For time-step  $t \in TS$ , the *energy* balance shall be:

$$\begin{aligned} FL_t + \sum_{b \in B^{DL} \cup B^{HDR}} (1 + MglLoss_{t,b}) \cdot With_{t,b} \\ + \sum_{d \in DX} (1 + MglLoss_{t,d}) \cdot With_{t,d} - \sum_{i=1..N_{LdViol_t}} SLdViol_{t,i} \\ = \sum_{b \in B^{NDG} \cup B^{DG}} (1 + MglLoss_{t,b}) \cdot Inj_{t,b} \\ + \sum_{d \in DI} (1 + MglLoss_{t,d}) \cdot Inj_{t,d} - \sum_{i=1..N_{GenViol_t}} SGenViol_{t,i} \\ + LossAdj_t. \end{aligned}$$

## 8.7.2 Operating Reserve Requirements

- 8.7.2.1 *Operating reserve* shall be scheduled to meet system-wide requirements for synchronized *ten-minute operating reserve*, total *ten-minute operating reserve*, and *thirty-minute operating reserve* while respecting all applicable regional minimum requirements and regional maximum restrictions for *operating reserve*.
- 8.7.2.2 Constraint violation penalty curves may be used to impose a penalty cost for not meeting the *IESO's* system-wide *operating reserve* requirements, not meeting a regional minimum requirement, or not adhering to a regional maximum restriction. Full *operating reserve*

requirements shall be scheduled unless the cost of doing so would be higher than the applicable penalty cost. For each time-step  $t \in TS$ :

$$\sum_{b \in B^{DL}} \left( \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \right) + \sum_{i=1..N_{10SViol_t}} S10SViol_{t,i} \geq TOT10S_t;$$

$$\begin{aligned} & \sum_{b \in B^{DL}} \left( \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \right) \\ & + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} \right) + \sum_{d \in DX} \left( \sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} \right) \\ & + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \right) + \sum_{d \in DI} \left( \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \right) \\ & + \sum_{i=1..N_{10RViol_t}} S10RViol_{t,i} \geq TOT10R_t; \end{aligned}$$

and

$$\begin{aligned} & \sum_{b \in B^{DL}} \left( \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \right) + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} \right) \\ & + \sum_{d \in DX} \left( \sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \right) \\ & + \sum_{d \in DI} \left( \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \right) + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,j} \right) \\ & + \sum_{d \in DX} \left( \sum_{j \in J_{t,d}^{30R}} S30RXL_{t,d,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \right) \\ & + \sum_{d \in DI} \left( \sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \right) + \sum_{i=1..N_{30RViol_t}} S30RViol_{t,i} \geq TOT30R_t. \end{aligned}$$

8.7.2.3 The following constraints shall be applied for each time-step  $t \in TS$  and each region  $r \in ORREG$ :

$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} \right) + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \right) + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \right) \\
& + \sum_{i=1..N_{REG10RViol_t}} SREG10RViol_{r,t,i} \geq REGMin10R_{t,r};
\end{aligned}$$

$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} \right) + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \right) + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \right) \\
& - \sum_{i=1..N_{XREG10RViol_t}} SXREG10RViol_{r,t,i} \leq REGMax10R_{t,r};
\end{aligned}$$

$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} \right) + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \right) + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,j} \right) + \sum_{d \in D_r^{REG} \cap DX} \left( \sum_{j \in J_{t,d}^{30R}} S30RXL_{t,d,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \right) + \sum_{d \in D_r^{REG} \cap DI} \left( \sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \right) \\
& + \sum_{i=1..N_{REG30RViol_t}} SREG30RViol_{r,t,i} \geq REGMin30R_{t,r};
\end{aligned}$$



and

$$\begin{aligned}
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} \right) \\
& + \sum_{d \in D_r^{REG} \cap D^X} \left( \sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap D^I} \left( \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \right) + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap D^X} \left( \sum_{j \in J_{t,d}^{30R}} S30RXL_{t,d,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap D^I} \left( \sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \right) - \sum_{i=1..N_{XREG30RViol_t}} SXREG30RViol_{r,t,i} \\
& \leq REGMax30R_{t,r}.
\end{aligned}$$

### 8.7.3 IESO Internal Transmission Limits

- 8.7.3.1 The Pre-Dispatch Scheduling algorithm shall produce a set of *energy* schedules that do not violate any *security limits* in the pre-contingency state and the post-contingency state subject to the remainder of this section 8.7.3. The total amount of *energy* scheduled to be injected and withdrawn at each bus used by the *energy* balance constraint in section 8.7.1.5, shall be used to produce these schedules.
- 8.7.3.2 Pre-contingency,  $SPreITLViol_{f,t,i}$ , and post-contingency,  $SITLViol_{c,f,t,i}$ , transmission limit violation variables shall allow the *pre-dispatch calculation engine* to find a solution.

8.7.3.3 For all time-steps  $t \in TS$  and facilities  $f \in F_t$ , the linearized constraints for violated pre-contingency limits obtained from the *security* assesment function shall take the form:

$$\begin{aligned} & \sum_{b \in B^{NDG} \cup B^{DG}} PreConSF_{t,f,b} \cdot Inj_{t,b} - \sum_{b \in B^{DL} \cup B^{HDR}} PreConSF_{t,f,b} \cdot With_{t,b} \\ & + \sum_{d \in DI} PreConSF_{t,f,d} \cdot Inj_{t,d} - \sum_{d \in DX} PreConSF_{t,f,d} \cdot With_{t,d} \\ & - \sum_{i=1..N_{PreITLViol_{f,t}}} SPreITLViol_{f,t,i} \leq AdjNormMaxFlow_{t,f}. \end{aligned}$$

8.7.3.4 For all time-steps  $t \in TS$ , contingencies  $c \in C$ , and facilities  $f \in F_{t,c}$  the linearized constraints for violated post-contingency limits obtained from the *security* assesment function shall take the form:

$$\begin{aligned} & \sum_{b \in B^{NDG} \cup B^{DG}} SF_{t,c,f,b} \cdot Inj_{t,b} - \sum_{b \in B^{DL} \cup B^{HDR}} SF_{t,c,f,b} \cdot With_{t,b} + \sum_{d \in DI} SF_{t,c,f,d} \\ & \cdot Inj_{t,d} - \sum_{d \in DX} SF_{t,c,f,d} \cdot With_{t,d} \\ & - \sum_{i=1..N_{ITLViol_{c,f,t}}} SITLViol_{c,f,t,i} \leq AdjEmMaxFlow_{t,c,f}. \end{aligned}$$

#### 8.7.4 Intertie Limits

8.7.4.1 The Pre-Dispatch Scheduling algorithm shall produce a set of *energy* and *operating reserve* schedules that respect any *security limits* associated with *interties* between Ontario and *intertie zones*. For all time-steps  $t \in TS$  and all constraints  $z \in Z_{Sch}$ :

$$\begin{aligned} & \sum_{a \in A: EnCoeff_{a,z} \neq 0} \left[ EnCoeff_{a,z} \left( \sum_{d \in DI_a} \sum_{k \in K_{t,d}^E} SIG_{t,d,k} - \sum_{d \in DX_a} \sum_{j \in J_{t,d}^E} SXL_{t,d,j} \right) \right. \\ & \left. + 0.5 \cdot (EnCoeff_{a,z} + 1) \left( \sum_{d \in DI_a} \left( \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} + \sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \right) + \right. \right. \\ & \left. \left. \sum_{d \in DX_a} \left( \sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} + \sum_{j \in J_{t,d}^{30R}} S30RXL_{t,d,j} \right) \right) \right] \\ & - \sum_{i=1..N_{PreConXTLViol_{z,t}}} SPreXTLViol_{z,t,i} \leq MaxExtSch_{t,z}. \end{aligned}$$

where for out-of-service *intertie zones*, the *intertie* limits shall be set to zero and all *boundary entity resources* shall receive a zero schedule for *energy* and *operating reserve*.

8.7.4.2 Changes in the hour-to-hour net *energy* schedule over all *interties* shall not exceed the net interchange scheduling limit. The net import schedule shall be summed over all *intertie zones* for a given time-step to obtain the net *interchange schedule* for the time-step, and shall not:

8.7.4.2.1 exceed the net *interchange schedule* for the previous time-step plus the net interchange scheduling limit; and

8.7.4.2.2 be less than the net *interchange schedule* for the previous time-step minus the net interchange scheduling limit.

8.7.4.3 Violation variables shall be provided for both the up and down ramp limits to allow the *pre-dispatch calculation engine* to find a solution and for all time-steps  $t \in TS$ :

$$\begin{aligned}
 & \sum_{d \in DI} \sum_{k \in K_{t-1,d}^E} SIG_{t-1,d,k} - \sum_{d \in DX} \sum_{j \in J_{t-1,d}^E} SXL_{t-1,d,j} - ExtDSC_t - \sum_{i=1..N_{NIDViol_t}} SNIDViol_{t,i} \\
 & \leq \sum_{d \in DI} \sum_{k \in K_{t,d}^E} SIG_{t,d,k} - \sum_{d \in DX} \sum_{j \in J_{t,d}^E} SXL_{t,d,j} \\
 & \leq \sum_{d \in DI} \sum_{k \in K_{t-1,d}^E} SIG_{t-1,d,k} - \sum_{d \in DX} \sum_{j \in J_{t-1,d}^E} SXL_{t-1,d,j} + ExtUSC_t \\
 & + \sum_{i=1..N_{NIUViol_t}} SNIUViol_{t,i}.
 \end{aligned}$$

8.7.5 Penalty Price Variable Bounds

8.7.5.1 Penalty price variables shall be restricted to the ranges determined by the constraint violation penalty curves for the Pre-Dispatch Scheduling algorithm and for time-steps  $t \in TS$ :

$$\begin{aligned}
0 \leq SLdViol_{t,i} \leq QLdViolSch_{t,i} & \quad \text{for all } i \in \{1, \dots, N_{LdViol_t}\}; \\
0 \leq SGenViol_{t,i} \leq QGenViolSch_{t,i} & \quad \text{for all } i \in \{1, \dots, N_{GenViol_t}\}; \\
0 \leq S10SViol_{t,i} \leq Q10SViolSch_{t,i} & \quad \text{for all } i \in \{1, \dots, N_{10SViol_t}\}; \\
0 \leq S10RViol_{t,i} \leq Q10RViolSch_{t,i} & \quad \text{for all } i \in \{1, \dots, N_{10RViol_t}\}; \\
0 \leq S30RViol_{t,i} \leq Q30RViolSch_{t,i} & \quad \text{for all } i \in \{1, \dots, N_{30RViol_t}\}; \\
0 \leq SREG10RViol_{r,t,i} \leq QREG10RViolSch_{t,i} & \quad \text{for all } r \in ORREG, i \in \{1, \dots, N_{REG10RViol_t}\}; \\
0 \leq SREG30RViol_{r,t,i} \leq QREG30RViolSch_{t,i} & \quad \text{for all } r \in ORREG, i \in \{1, \dots, N_{REG30RViol_t}\}; \\
0 \leq SXREG10RViol_{r,t,i} \leq QXREG10RViolSch_{t,i} & \quad \text{for all } r \in ORREG, i \in \{1, \dots, N_{XREG10RViol_t}\}; \\
0 \leq SXREG30RViol_{r,t,i} \leq QXREG30RViolSch_{t,i} & \quad \text{for all } r \in ORREG, i \in \{1, \dots, N_{XREG30RViol_t}\}; \\
0 \leq SPreITLViol_{f,t,i} \leq QPreITLViolSch_{f,t,i} & \quad \text{for all } f \in F_b, i \in \{1, \dots, N_{PreITLViol_{f,t}}\}; \\
0 \leq SITLViol_{c,f,t,i} \leq QITLViolSch_{c,f,t,i} & \quad \text{for all } c \in C, f \in F_{t,c}, i \in \{1, \dots, N_{ITLViol_{c,f,t}}\}; \\
0 \leq SPreXTLViol_{z,t,i} \leq QPreXTLViolSch_{z,t,i} & \quad \text{for all } z \in Z_{Sch}, i \in \{1, \dots, N_{PreXTLViol_{z,t}}\}; \\
0 \leq SNIUViol_{t,i} \leq QNIUViolSch_{t,i} & \quad \text{for all } i \in \{1, \dots, N_{NIUViol_t}\}; \\
0 \leq SNIDViol_{t,i} \leq QNIDViolSch_{t,i} & \quad \text{for all } i \in \{1, \dots, N_{NIDViol_t}\}; \\
0 \leq SMaxDelViol_{t,b,i} \leq QMaxDelViolSch_{t,b,i} & \quad \text{for all } b \in B^{ELR}, i \in \{1, \dots, N_{MaxDelViol_t}\}; \\
0 \leq SMinDelViol_{t,b,i} \leq QMinDelViolSch_{t,b,i} & \quad \text{for all } b \in B^{HE}, i \in \{1, \dots, N_{MinDelViol_t}\}; \\
0 \leq SMaxDelViol_{t,s,i} \leq QMaxDelViolSch_{t,s,i} & \quad \text{for all } s \in SHE, i \in \{1, \dots, N_{SMaxDelViol_t}\}; \\
0 \leq SMinDelViol_{t,s,i} \leq QMinDelViolSch_{t,s,i} & \quad \text{for all } s \in SHE, i \in \{1, \dots, N_{SMinDelViol_t}\}; \\
0 \leq SOGenLnkViol_{t(b_1,b_2),i} \leq QOGenLnkViol_{t(b_1,b_2),i} & \quad \text{for all } (b_1,b_2) \in LNK, i \in \{1, \dots, N_{OGenLnkViol_t}\}; \\
\text{and} \\
0 \leq SUGenLnkViol_{t(b_1,b_2),i} \leq QUGenLnkViol_{t(b_1,b_2),i} & \quad \text{for all } (b_1,b_2) \in LNK, i \in \{1, \dots, N_{UGenLnkViol_t}\}.
\end{aligned}$$

## 8.8 Outputs

8.8.1 Outputs for the Pre-Dispatch Scheduling algorithm include *resource* schedules and commitments.

## 9 Pre-Dispatch Pricing

### 9.1 Purpose

- 9.1.1 The Pre-Dispatch Pricing algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, subject to section 14.7.1.3, and *resource* schedules and commitments produced by the Pre-Dispatch Scheduling algorithm to meet the *IESO's* province-wide non-dispatchable *demand* forecast and IESO-specified *operating reserve* requirements for each hour of the pre-dispatch look-ahead period.

### 9.2 Information, Sets, Indices and Parameters

- 9.2.1 Information, sets, indices and parameters used by the Pre-Dispatch Pricing algorithm are described in section 3. In addition, the following *resource* schedules and commitments determined by the Pre-Dispatch Scheduling algorithm shall be used by the Pre-Dispatch Pricing algorithm:
- 9.2.1.1  $SDG_{t,b,k}^{PDS}$  designates the amount of *energy* that the *dispatchable generation resource* is scheduled to provide above  $MinQDGC_b$  at bus  $b \in B^{ELR} \cup B^{HE}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^E$ ;
- 9.2.1.2  $ODG_{t,b}^{PDS}$  designates whether the *dispatchable generation resource* at bus  $b \in B^{DG}$  was scheduled at or above its *minimum loading point* in time-step  $t \in TS$ ;
- 9.2.1.3  $S10SDG_{t,b,k}^{PDS}$  designates the amount of synchronized *ten-minute operating reserve* that the *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^{10S}$ ;
- 9.2.1.4  $S10NDG_{t,b,k}^{PDS}$  designates the amount of non-synchronized *ten-minute operating reserve* that the *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^{10N}$ ;
- 9.2.1.5  $S30RDG_{t,b,k}^{PDS}$  designates the amount of *thirty-minute operating reserve* that the *dispatchable generation resource* is scheduled to provide at

bus  $b \in \mathcal{B}^{ELR} \cup \mathcal{B}^{HE}$  in time-step  $t \in TS$  in association with lamination  $k \in \mathcal{K}_{t,b}^{20R}$ ; and

- 9.2.1.6  $OHO_{t,b}^{PDS}$  designates whether the *dispatchable* hydroelectric *generation resource* at bus  $b \in \mathcal{B}^{HE}$  has been scheduled at or above  $MinHO_{t,b}$  in time-step  $t \in TS$ .

### 9.3 Variables and Objective Function

9.3.1 The Pre-Dispatch Pricing algorithm shall solve for the same variables as in the Pre-Dispatch Scheduling algorithm, section 8.3.1, with the following exceptions:

- 9.3.1.1  $IDG_{t,b}$  for bus  $b \in \mathcal{B}^{DG}$  and time-step  $t \in TS$  shall not appear in the formulation;
- 9.3.1.2  $ODG_{t,b}$  for bus  $b \in \mathcal{B}^{DG}$  and time-step  $t \in TS$  will be fixed to a constant value, as determined by the Pre-Dispatch Scheduling algorithm;
- 9.3.1.3  $OHO_{t,b}$  for bus  $b \in \mathcal{B}^{HE}$  and time-step  $t \in TS$  will be fixed to a constant value, as determined by the Pre-Dispatch Scheduling algorithm;
- 9.3.1.4  $IHE_{t,b,i}$  for  $b \in \mathcal{B}^{HE}$ , time-step  $t \in TS$  and *start indication value*  $i \in \{1, \dots, N_{StartMW_b}\}$  shall not appear in the formulation;
- 9.3.1.5  $SOGenLnkViol_{t,(b_1,b_2),i}$  for  $(b_1,b_2) \in LNK$  such that  $b_1 \in \mathcal{B}_{up}^{HE}$  and  $b_2 \in \mathcal{B}_{dn}^{HE}$ , time-step  $t \in TS$  and  $i \in \{1, \dots, N_{OGenLnkViol_t}\}$  shall not appear in the formulation; and
- 9.3.1.6  $SUGenLnkViol_{t,(b_1,b_2),i}$  for  $(b_1,b_2) \in LNK$  such that  $b_1 \in \mathcal{B}_{up}^{HE}$  and  $b_2 \in \mathcal{B}_{dn}^{HE}$ , time-step  $t \in TS$  and  $i \in \{1, \dots, N_{UGenLnkViol_t}\}$  shall not appear in the formulation.

9.3.2 The objective function for the Pre-Dispatch Pricing algorithm shall maximize gains from trade by maximizing the following expression:

$$\sum_{t \in TS} \left( ObjDL_t - ObjHDR_t + ObjXL_t - ObjNDG_t - ObjDG_t - ObjIG_t - TB_t - ViolCost_t \right)$$

where:

$$\begin{aligned} ObjDL_t &= \sum_{b \in B^{DL}} \left( \sum_{j \in J_{t,b}^E} SDL_{t,b,j} \cdot PDL_{t,b,j} - \sum_{j \in J_{t,b}^{10S}} S10SDL_{t,b,j} \cdot P10SDL_{t,b,j} - \sum_{j \in J_{t,b}^{10N}} S10NDL_{t,b,j} \cdot P10NDL_{t,b,j} - \sum_{j \in J_{t,b}^{30R}} S30RDL_{t,b,j} \cdot P30RDL_{t,b,j} \right); \\ ObjHDR_t &= \sum_{b \in B^{HDR}} \left( \sum_{j \in J_{t,b}^E} SHDR_{t,b,j} \cdot PHDR_{t,b,j} \right); \\ ObjXL_t &= \sum_{d \in DX} \left( \sum_{j \in J_{t,d}^E} SXL_{t,d,j} \cdot PXL_{t,d,j} - \sum_{j \in J_{t,d}^{10N}} S10NXL_{t,d,j} \cdot P10NXL_{t,d,j} - \sum_{j \in J_{t,d}^{30R}} S30RXL_{t,d,j} \cdot P30RXL_{t,d,j} \right); \\ ObjNDG_t &= \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{t,b}^E} SNDG_{t,b,k} \cdot PNDG_{t,b,k} \right); \\ ObjDG_t &= \sum_{b \in B^{DG}} \left( \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \cdot PDG_{t,b,k} + \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} \cdot P10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} \cdot P10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \cdot P30RDG_{t,b,k} \right); \\ ObjIG_t &= \sum_{d \in DI} \left( \sum_{k \in K_{t,d}^E} SIG_{t,d,k} \cdot PIG_{t,d,k} + \sum_{k \in K_{t,d}^{10N}} S10NIG_{t,d,k} \cdot P10NIG_{t,d,k} + \sum_{k \in K_{t,d}^{30R}} S30RIG_{t,d,k} \cdot P30RIG_{t,d,k} \right). \end{aligned}$$

9.3.2.1 The tie-breaking term,  $TB_t$ , shall be the same term described in section 8.3.2.1.

9.3.2.2  $ViolCost_t$  shall be calculated as follows:

$$\begin{aligned}
ViolCost_t = & \sum_{i=1..N_{LdViol_t}} SLdViol_{t,i} \cdot PLdViolPrc_{t,i} \\
& - \sum_{i=1..N_{GenViol_t}} SGenViol_{t,i} \cdot PGenViolPrc_{t,i} \\
& + \sum_{i=1..N_{10SViol_t}} S10SViol_{t,i} \cdot P10SViolPrc_{t,i} \\
& + \sum_{i=1..N_{10RViol_t}} S10RViol_{t,i} \cdot P10RViolPrc_{t,i} \\
& + \sum_{i=1..N_{30RViol_t}} S30RViol_{t,i} \cdot P30RViolPrc_{t,i} \\
& + \sum_{r \in ORREG} \left( \sum_{i=1..N_{REG10RViol_t}} SREG10RViol_{r,t,i} \cdot PREG10RViolPrc_{t,i} \right) \\
& + \sum_{r \in ORREG} \left( \sum_{i=1..N_{REG30RViol_t}} SREG30RViol_{r,t,i} \cdot PREG30RViolPrc_{t,i} \right) \\
& + \sum_{r \in ORREG} \left( \sum_{i=1..N_{XREG10RViol_t}} SXREG10RViol_{r,t,i} \cdot PXREG10RViolPrc_{t,i} \right) \\
& + \sum_{r \in ORREG} \left( \sum_{i=1..N_{XREG30RViol_t}} SXREG30RViol_{r,t,i} \cdot PXREG30RViolPrc_{t,i} \right) \\
& + \sum_{f \in F_t} \left( \sum_{i=1..N_{PreITLViol_{f,t}}} SPreITLViol_{f,t,i} \cdot PPreITLViolPrc_{f,t,i} \right) \\
& + \sum_{c \in C} \sum_{f \in F_{t,c}} \left( \sum_{i=1..N_{ITLViol_{c,f,t}}} SITLViol_{c,f,t,i} \cdot PITLViolPrc_{c,f,t,i} \right) \\
& + \sum_{z \in Z_{Sch}} \left( \sum_{i=1..N_{PreXTLViol_t}} SPreXTLViol_{z,t,i} \cdot PPreXTLViolPrc_{z,t,i} \right) \\
& + \sum_{i=1..N_{NIUViol_t}} SNIUViol_{t,i} \cdot PNIUViolPrc_{t,i} \\
& + \sum_{i=1..N_{NIDViol_t}} SNIDViol_{t,i} \cdot PNIDViolPrc_{t,i} \\
& + \sum_{b \in B^{ELR}} \left( \sum_{i=1..N_{MaxDelViol_t}} SMaxDelViol_{t,b,i} \cdot PMaxDelViolPrc_{t,b,i} \right)
\end{aligned}$$



$$\begin{aligned}
& + \sum_{b \in B^{HE}} \left( \sum_{i=1..N_{MinDelViol_t}} SMinDelViol_{t,b,i} \cdot PMinDelViolPrc_{t,b,i} \right) \\
& + \sum_{s \in SHE} \left( \sum_{i=1..N_{SMaxDelViol_t}} SMaxDelViol_{t,s,i} \cdot PSMaDelViolPrc_{t,s,i} \right) \\
& + \sum_{s \in SHE} \left( \sum_{i=1..N_{SMinDelViol_t}} SMinDelViol_{t,s,i} \cdot PSMiDelViolPrc_{t,s,i} \right)
\end{aligned}$$

9.3.2.3 The objective function of the Pre-Dispatch Pricing algorithm in section 9.3.2 shall be subject to the constraints described in sections 9.4 - 9.8.

## 9.4 Constraints

9.4.1 The constraints described in sections 9.5, 9.6, 9.7 and 9.8 apply to the optimization function in the Pre-Dispatch Pricing algorithm.

## 9.5 Dispatch Data Constraints Applying to Individual Hours

### 9.5.1 Scheduling Variable Bounds

9.5.1.1 *Energy and operating reserve* schedules shall not be negative and shall not exceed the quantity respectively offered for *energy* and *operating reserve*. For all time-steps  $t \in TS$ :

$$\begin{aligned}
 0 \leq SDL_{t,b,j} &\leq QDL_{t,b,j} && \text{for all } b \in B^{DL}, j \in J_{t,b}^E; \\
 0 \leq S10SDL_{t,b,j} &\leq Q10SDL_{t,b,j} && \text{for all } b \in B^{DL}, j \in J_{t,b}^{10S}; \\
 0 \leq S10NDL_{t,b,j} &\leq Q10NDL_{t,b,j} && \text{for all } b \in B^{DL}, j \in J_{t,b}^{10N}; \\
 0 \leq S30RDL_{t,b,j} &\leq Q30RDL_{t,b,j} && \text{for all } b \in B^{DL}, j \in J_{t,b}^{30R}; \\
 0 \leq SHDR_{t,b,j} &\leq QHDR_{t,b,j} && \text{for all } b \in B^{HDR}, j \in J_{t,b}^E; \\
 0 \leq SXL_{t,d,j} &\leq QXL_{t,d,j} && \text{for all } d \in DX, j \in J_{t,d}^E; \\
 0 \leq S10NXL_{t,d,j} &\leq Q10NXL_{t,d,j} && \text{for all } d \in DX, j \in J_{t,d}^{10N}; \\
 0 \leq S30RXL_{t,d,j} &\leq Q30RXL_{t,d,j} && \text{for all } d \in DX, j \in J_{t,d}^{30R}; \\
 0 \leq SNDG_{t,b,k} &\leq QNDG_{t,b,k} && \text{for all } b \in B^{NDG}, k \in K_{t,b}^E; \\
 0 \leq SIG_{t,d,k} &\leq QIG_{t,d,k} && \text{for all } d \in DI, k \in K_{t,d}^E; \\
 0 \leq S10NIG_{t,d,k} &\leq Q10NIG_{t,d,k} && \text{for all } d \in DI, k \in K_{t,d}^{10N}; \text{ and} \\
 0 \leq S30RIG_{t,d,k} &\leq Q30RIG_{t,d,k} && \text{for all } d \in DI, k \in K_{t,d}^{30R}.
 \end{aligned}$$

9.5.1.2 A *dispatchable generation resource* may be scheduled for *energy* and *operating reserve* only if its commitment status variable, as determined by the Pre-Dispatch Scheduling algorithm, is equal to 1. For all time-steps  $t \in TS$ :

$$\begin{aligned}
 0 \leq SDG_{t,b,k} &\leq ODG_{t,b}^{PDS} \cdot QDG_{t,b,k} && \text{for all } b \in B^{DG}, k \in K_{t,b}^E; \\
 0 \leq S10SDG_{t,b,k} &\leq ODG_{t,b}^{PDS} \cdot Q10SDG_{t,b,k} && \text{for all } b \in B^{DG}, k \in K_{t,b}^{10S}; \\
 0 \leq S10NDG_{t,b,k} &\leq ODG_{t,b}^{PDS} \cdot Q10NDG_{t,b,k} && \text{for all } b \in B^{DG}, k \in K_{t,b}^{10N}; \text{ and} \\
 0 \leq S30RDG_{t,b,k} &\leq ODG_{t,b}^{PDS} \cdot Q30RDG_{t,b,k} && \text{for all } b \in B^{DG}, k \in K_{t,b}^{30R}.
 \end{aligned}$$

where

$ODG_{t,b}^{PDS}$  is a fixed constant in the above constraints, per section 9.8.1.1.

#### 9.5.2 Resource Minimums and Maximums

9.5.2.1 The constraints in section 8.5.2 shall apply in the Pre-Dispatch Pricing algorithm.

#### 9.5.3 Off-Market Transactions

9.5.3.1 The constraints in sections 8.5.3.1 and 8.5.3.2 for inadvertent payback transactions shall apply in the Pre-Dispatch Pricing algorithm.

9.5.3.2 In the case of *emergency energy* transactions, subject to section 9.5.3.3, the constraints in sections 8.5.3.3 and 8.5.3.4 shall apply in the Pre-Dispatch Pricing algorithm.

9.5.3.3 For all time-steps  $t \in TS$  and all *boundary entity resources* scheduled to import *emergency energy* that does not support an export  $d \in DI_t^{EMNS}$ :

$$\sum_{k \in K_{t,d}^E} SIG_{t,d,k} = 0.$$

#### 9.5.4 Intertie Minimum and Maximum Constraints

9.5.4.1 The constraints in section 8.5.4 shall apply in the Pre-Dispatch Pricing algorithm as well.

#### 9.5.5 Operating Reserve Scheduling

9.5.5.1 The constraints in section 8.5.5 shall apply in the Pre-Dispatch Pricing algorithm as well.

#### 9.5.6 Pseudo-Units

9.5.6.1 The constraints in section 8.5.6 shall apply in the Pre-Dispatch Pricing algorithm as well.

#### 9.5.7 Dispatchable Hydroelectric Generation Resources

9.5.7.1 The constraints in section 8.5.7 shall apply in the Pre-Dispatch Pricing algorithm as well, with the following exceptions:

9.5.7.1.1 *energy offer* laminations corresponding to the *hourly must-run* amount shall be ineligible to set prices;

9.5.7.1.2 *minimum hourly output* constraints shall be replaced by the constraints in section 9.8; and

9.5.7.1.3 a *dispatchable* hydroelectric *generation resource's* schedule shall respect its *forbidden regions* and may only set prices within the operating range determined by the adjacent *forbidden regions* between which the *resource* was scheduled.

9.5.8 Linked Wheeling Through Transactions

9.5.8.1 The constraints in section 8.5.8 shall apply in the Pre-Dispatch Pricing algorithm as well.

## 9.6 Dispatch Data Inter-Hour/Multi-Hour Constraints

9.6.1 Energy Ramping

9.6.1.1 The constraints in section 8.6.1 shall apply in the Pre-Dispatch Pricing algorithm as well.

9.6.2 Operating Reserve Ramping

9.6.2.1 The constraints in section 8.6.2 shall apply in the Pre-Dispatch Pricing algorithm as well.

9.6.3 Energy Limited Resources

9.6.3.1 The constraints in section 8.6.4 shall apply to *energy limited resources*. If a *resource's maximum daily energy limit* is binding, then the constraints in section 9.8 shall also apply.

9.6.4 Dispatchable Hydroelectric Generation Resources

9.6.4.1 A *dispatchable* hydroelectric *generation resource* shall be scheduled for *energy* to at least its *minimum daily energy limit*. Violation variables for under-scheduling a *resource's minimum daily energy limit* shall be provided to allow the *pre-dispatch calculation engine* to

find a solution. For all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$ :

$$\sum_{t \in TS_{tod}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} + \sum_{i=1..N_{MinDelViol_t}} SMinDelViol_{t,b,i} \right) \geq MinDEL_{tod,b} - EngyUsed_b.$$

9.6.4.1.1 If the pre-dispatch look-ahead period spans two *dispatch days*, for all hydroelectric *resource* buses  $b \in B^{HE}$ :

$$\sum_{t \in TS_{tom}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} + \sum_{i=1..N_{MinDelViol_t}} SMinDelViol_{t,b,i} \right) \geq MinDEL_{tom,b}.$$

9.6.4.2 The constraints in section 9.8.3.3 shall apply to a *dispatchable* hydroelectric *generation resource* with a binding *minimum daily energy limit* in the Pre-Dispatch Scheduling algorithm.

9.6.4.3 The schedules for multiple *dispatchable* hydroelectric *generation resources* with a registered *forebay* shall respect shared *maximum daily energy limits*. Violation variables for scheduling *resources* above the *maximum daily energy limit* may be used to allow the *pre-*

*dispatch calculation engine* to find a solution. For all sets  $s \in SHE$  and all time-steps  $T \in TS_{tod}$ :

$$\begin{aligned} & \sum_{t=2..T} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \right) \\ & + \sum_{b \in B_s^{HE}} \left( 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k} \right) \right) \\ & + 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k} \right) \\ & - \sum_{i=1..N_{SMaxDelViol_T}} SSMaxDelViol_{T,s,i} \leq MaxSDEL_{tod,s} - EngyUsedSHE_s \end{aligned}$$

9.6.4.3.1 If the look-ahead period spans two *dispatch days*, then for all sets  $s \in SHE$  and all time-steps  $T \in TS_{tom}$ :

$$\begin{aligned} & \sum_{t=t_{tom}..T} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \right) \\ & + \sum_{b \in B_s^{HE}} \left( 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k} \right) \right) \\ & + 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k} \right) \\ & - \sum_{i=1..N_{SMaxDelViol_T}} SSMaxDelViol_{T,s,i} \leq MaxSDEL_{tom,s} \end{aligned}$$

where the factors 10 *ORConv* and 30 *ORConv* shall be applied to scheduled *ten-minute operating reserve* and *thirty-minute operating reserve* to convert MW into MWh.

9.6.4.4 The schedules for multiple *dispatchable hydroelectric generation resources* with a registered *forebay* shall not violate shared *minimum daily energy limits*. Violation variables for scheduling *resources* below the *minimum daily energy limit* may be used to allow the *pre-dispatch*

*calculation engine* to find a solution. For all sets  $s \in SHE_{tod}$  and all time-steps  $t \in TS_{tod}$ :

$$\begin{aligned} \sum_{t \in TS_{tod}} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \right. \\ \left. + \sum_{i=1..N_{SMinDelViol_t}} SSMinDelViol_{t,s,i} \right) \\ \geq MinSDEL_{tod,s} - EngyUsedSHE_s. \end{aligned}$$

9.6.4.4.1 If the look-ahead period spans two *dispatch days*, then for all sets  $s \in SHE$  and all time-steps  $t \in TS_{tom}$ :

$$\begin{aligned} \sum_{t \in TS_{tom}} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \right. \\ \left. + \sum_{i=1..N_{SMinDelViol_t}} SSMinDelViol_{t,s,i} \right) \geq MinSDEL_{tom,s}. \end{aligned}$$

## 9.7 Constraints for Reliability Requirements

### 9.7.1 Energy Balance

9.7.1.1 The constraint in section 8.7.1 shall also apply in the Pre-Dispatch Pricing algorithm, except the marginal loss factors used in the *energy* balance constraint in the Pre-Dispatch Pricing algorithm shall be fixed to the marginal loss factors used in the last optimization function iteration of the Pre-Dispatch Scheduling algorithm.

### 9.7.2 Operating Reserve Requirements

9.7.2.1 The constraints in section 8.7.2 shall also apply in the Pre-Dispatch Pricing algorithm.

### 9.7.3 IESO Internal Transmission Limits

9.7.3.1 The constraints in section 8.7.3 shall also apply in the Pre-Dispatch Pricing algorithm, except the sensitivities and limits considered shall be those provided by the most recent *security* assessment function iteration of the Pre-Dispatch Pricing algorithm.

#### 9.7.4 Intertie Limits

9.7.4.1 The constraints in section 8.7.4 shall also apply in the Pre-Dispatch Pricing algorithm.

#### 9.7.5 Penalty Price Variable Bounds

9.7.5.1 The following constraints shall restrict the penalty price variables to the ranges determined by the constraint violation penalty curves for the pricing algorithm. For all time-steps  $t \in TS$ :

$$\begin{aligned} 0 \leq SLdViol_{t,i} &\leq QLdViolPrc_{t,i} && \text{for all } i \in \{1, \dots, N_{LdViol_t}\}; \\ 0 \leq SGenViol_{t,i} &\leq QGenViolPrc_{t,i} && \text{for all } i \in \{1, \dots, N_{GenViol_t}\}; \\ 0 \leq S10SViol_{t,i} &\leq Q10SViolPrc_{t,i} && \text{for all } i \in \{1, \dots, N_{10SViol_t}\}; \\ 0 \leq S10RViol_{t,i} &\leq Q10RViolPrc_{t,i} && \text{for all } i \in \{1, \dots, N_{10RPrct_t}\}; \\ 0 \leq S30RViol_{t,i} &\leq Q30RViolPrc_{t,i} && \text{for all } i \in \{1, \dots, N_{30RPrct_t}\}; \\ 0 \leq SREG10RViol_{r,t,i} &\leq QREG10RViolPrc_{t,i} && \text{for all } r \in ORREG, i \in \{1, \dots, N_{REG10RPrct_t}\}; \\ 0 \leq SREG30RViol_{r,t,i} &\leq QREG30RViolPrc_{t,i} && \text{for all } r \in ORREG, i \in \{1, \dots, N_{REG30RPrct_t}\}; \\ 0 \leq SXREG10RViol_{r,t,i} &\leq QXREG10RViolPrc_{t,i} && \text{for all } r \in ORREG, i \in \{1, \dots, N_{XREG10RPrct_t}\}; \\ 0 \leq SXREG30RViol_{r,t,i} &\leq QXREG30RViolPrc_{t,i} && \text{for all } r \in ORREG, i \in \{1, \dots, N_{XREG30RPrct_t}\}; \\ 0 \leq SPreITLViol_{f,t,i} &\leq QPreITLViolPrc_{f,t,i} && \text{for all } f \in F_b, i \in \{1, \dots, N_{PreITLPrc_{f,t}}\}; \\ 0 \leq SITLViol_{f,c,t,i} &\leq QITLViolPrc_{f,c,t,i} && \text{for all } c \in C, f \in F_{c,b}, i \in \{1, \dots, N_{PITLPrc_{c,f,t}}\}; \\ 0 \leq SPreXTLViol_{z,t,i} &\leq QPreXTLViolPrc_{z,t,i} && \text{for all } z \in Z_{Sch}, i \in \{1, \dots, N_{PreXTLPrc_{z,t}}\}; \\ 0 \leq SNIUViol_{t,i} &\leq QNIUViolPrc_{t,i} && \text{for all } i \in \{1, \dots, N_{NIUPrc_t}\}; \\ 0 \leq SNIDViol_{t,i} &\leq QNIDViolPrc_{t,i} && \text{for all } i \in \{1, \dots, N_{NIDPrct_t}\}; \\ 0 \leq SMaxDelViol_{t,b,i} &\leq QMaxDelViolPrc_{t,b,i} && \text{for all } b \in B^{ELR}, i \in \{1, \dots, N_{MaxDelViol_t}\}; \\ 0 \leq SMinDelViol_{t,b,i} &\leq QMinDelViolPrc_{t,b,i} && \text{for all } b \in B^{HE}, i \in \{1, \dots, N_{MinDelViol_t}\}; \\ 0 \leq SMaxDelViol_{t,s,i} &\leq QMaxDelViolPrc_{t,s,i} && \text{for all } s \in SHE, i \in \{1, \dots, N_{SMaxDelViol_t}\}; \text{ and} \\ 0 \leq SMinDelViol_{t,s,i} &\leq QMinDelViolPrc_{t,s,i} && \text{for all } s \in SHE, i \in \{1, \dots, N_{SMinDelViol_t}\}.\end{aligned}$$



## 9.8 Constraints to Ensure the Price Setting Eligibility of Offer/Bid Laminations

### 9.8.1 Commitment Status Variables

9.8.1.1 Commitment decisions shall be fixed to the commitment statuses of *resources* calculated by the Pre-Dispatch Scheduling algorithm in section 8. For all time-steps  $t \in TS$  and all buses  $b \in B^{DG}$ :

$$ODG_{t,b} = ODG_{t,b}^{PDS}.$$

### 9.8.2 Energy Limited Resources

9.8.2.1 For an *energy limited resource* with a *maximum daily energy limit* that was binding in the Pre-Dispatch Scheduling algorithm, the schedules calculated by the Pre-Dispatch Scheduling algorithm shall determine the price-setting eligibility of the *resource's energy* and *operating reserve offer* laminations. In each time-step, *energy* or *operating reserve* laminations up to the total amount of *energy* and *operating reserve* scheduled in the Pre-Dispatch Scheduling algorithm shall be eligible to set prices. For bus  $b \in B^{ELR}$ , if there exists a time-step  $T \in TS_{tod}$  such that:

$$\begin{aligned} \sum_{t=2..T} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right) \\ + 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k}^{PDS} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k}^{PDS} \right) \\ + 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k}^{PDS} \right) = MaxDEL_{tod,b} - EngyUsed_b \end{aligned}$$

9.8.2.1.1 then the *maximum daily energy limit* constraint shall be considered binding in the Pre-Dispatch Scheduling algorithm. In such circumstances, the following constraints must hold for bus  $b \in B^{ELR}$  for all time-steps  $t \in TS_{tod}$ :

$$\begin{aligned}
\sum_{k \in K_{t,b}^E} SDG_{t,b,k} &\leq \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} + \epsilon, \\
\sum_{k \in K_{t,b}^E} SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \\
&\leq MaxDEL_{tod,b} - EngyUsed_b - \sum_{\tau=2}^{t-1} \sum_{k \in K_{\tau,b}^E} SDG_{\tau,b,k}^{PDS}
\end{aligned}$$

where  $\epsilon$  is a small positive constant.

9.8.2.2 If the pre-dispatch look-ahead period spans two *dispatch days*, then for bus  $b \in B^{ELR}$ , if there exists a time-step  $T \in TS_{tom}$  such that:

$$\begin{aligned}
\sum_{t=t_{tom}..T} &\left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right) \\
&+ 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k}^{PDS} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k}^{PDS} \right) \\
&+ 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k}^{PDS} \right) = MaxDEL_{tom,b}
\end{aligned}$$

9.8.2.2.1 then the *maximum daily energy limit* constraint is considered to be binding for the next *dispatch day* in Pre-Dispatch Scheduling algorithm. In such circumstances, the following constraints must hold for bus  $b \in B^{ELR}$  for all time-steps  $t \in TS_{tom}$ :

$$\begin{aligned}
\sum_{k \in K_{t,b}^E} SDG_{t,b,k} &\leq \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} + \epsilon, \\
\sum_{k \in K_{t,b}^E} SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \\
&\leq MaxDEL_{tom,b} - \sum_{\tau=tom}^{t-1} \sum_{k \in K_{\tau,b}^E} SDG_{\tau,b,k}^{PDS}.
\end{aligned}$$

where  $\epsilon$  is a small positive constant.

### 9.8.3 Dispatchable Hydroelectric Generation Resources

- 9.8.3.1 If a *dispatchable* hydroelectric *generation resource* is scheduled to provide *energy* at or above its *minimum hourly output* in the Pre-Dispatch Scheduling algorithm, such *resource* shall also be scheduled at or above its *minimum hourly output* in the Pre-Dispatch Pricing algorithm. The *energy offer* laminations corresponding to the *minimum hourly output* amount shall be ineligible to set prices. If a *dispatchable* hydroelectric *generation resource* with a *minimum hourly output* amount receives a zero schedule in the Pre-Dispatch Scheduling algorithm, the *resource* shall also receive a zero schedule in the Pre-Dispatch Pricing algorithm and shall be ineligible to set prices in the *energy* market. For all time-steps  $t \in TS$  and *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$ :

$$ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \geq MinHO_{t,b} \cdot OHO_{t,b}^{PDS}$$

and for all  $k \in K_{t,b}^E$ :

$$0 \leq SDG_{t,b,k} \leq OHO_{t,b}^{PDS} \cdot QDG_{t,b,k}.$$

- 9.8.3.2 For a *dispatchable* hydroelectric *generation resource* with a limited number of starts, such *resource* shall be scheduled such that it is limited to set prices within an operating range consistent with the number of starts utilized by the *resource's* schedule determined by the Pre-Dispatch Scheduling algorithm. The *resource's* schedule shall be between the same *start indication values* as determined in the Pre-Dispatch Scheduling algorithm. For all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$  and all time-steps  $t \in TS$ :

$$\text{If } 0 \leq ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} < StartMW_{b,1},$$

then

$$0 \leq ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \leq StartMW_{b,1} - 0.1$$

If  $StartMW_{b,i} \leq ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} < StartMW_{b,i+1}$  for  $i \in \{1, \dots, (NStartMW_b - 1)\}$ ,

then

$$\begin{aligned} StartMW_{b,i} &\leq ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \\ &\leq StartMW_{b,i+1} - 0.1 \end{aligned}$$

If  $ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \geq StartMW_{b,NStartMW_b}$ ,

then

$$ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \geq StartMW_{b,NStartMW_b}.$$

9.8.3.3 For a *dispatchable* hydroelectric *generation resource* with a *minimum daily energy limit* that was binding in the Pre-Dispatch Scheduling algorithm, the *offer* laminations corresponding to the *energy* schedules calculated in the Pre-Dispatch Scheduling algorithm shall be ineligible to set prices. For all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$  such that  $MinDEL_{tod,b} > 0$  and

$$\sum_{t \in TS_{tod}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right) \leq MinDEL_{tod,b} - EngyUsed_b,$$

9.8.3.3.1 the following constraints must hold for all time-steps  $t \in TS_{tod}$  and *offer* laminations  $k \in K_{t,b}^E$ :

$$SDG_{t,b,k} \geq SDG_{t,b,k}^{PDS}.$$

9.8.3.3.2 If the pre-dispatch look-ahead period spans two *dispatch days*, for all *dispatchable* hydroelectric *generation resource* buses  $b \in B^{HE}$  such that  $MinDEL_{tom,b} > 0$  and

$$\sum_{t \in TS_{tom}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right) \leq MinDEL_{tom,b},$$

9.8.3.3.3 the following constraints must hold for all time-steps  $t \in TS_{tom}$  and *offer* laminations  $k \in K_{t,b}^E$ :

$$SDG_{t,b,k} \geq SDG_{t,b,k}^{PDS}.$$

9.8.3.4 For a *dispatchable hydroelectric generation resource* with a shared *minimum daily energy limit* that was binding in the Pre-Dispatch Scheduling algorithm, the *offer* laminations corresponding to the *energy* schedules calculated for all *resources* in the set  $s \in SHE$  in the Pre-Dispatch Scheduling algorithm shall be ineligible to set prices. Thus, for each set  $s \in SHE$ :

$$\sum_{t \in TS_{tod}} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right) \right) \leq MinSDEL_{tod,s} - EngyUsedSHE_s,$$

9.8.3.4.1 the following constraints must hold for all time-steps  $t \in TS_{tod} \in$ :

$$\sum_{b \in B_s^{HE}} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \geq \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right).$$

9.8.3.4.2 If the pre-dispatch look-ahead period spans two *dispatch days*, then for each set  $s \in SHE$ :

$$\sum_{t \in TS_{tom}} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right) \right) \leq MinSDEL_{tom,s}$$

9.8.3.4.3 the following constraints must hold for all time-steps  $t \in TS_{tom}$ :

$$\sum_{b \in B_s^{HE}} \left( ODG_{t,b} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k} \right) \geq \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right).$$

9.8.3.5 For a *dispatchable hydroelectric generation resource* with a binding *maximum daily energy limit* in the Pre-Dispatch Scheduling algorithm, the schedules calculated in the Pre-Dispatch Scheduling algorithm shall determine the price-setting eligibility of the *resource's energy* and *operating reserve offer* laminations as described in section 9.8.2.

9.8.3.6 For a *dispatchable hydroelectric generation resource* with a shared *maximum daily energy limit* that was binding in the Pre-Dispatch Scheduling algorithm, in each hour, the *offer* laminations up to the sum of *energy* and *operating reserve* schedules calculated in Pre-Dispatch Scheduling algorithm for all *resources* in each set  $s \in SHE$  will be eligible to set prices. For each set  $s \in SHE$ , if there exists  $T \in TS_{tod}$  such that:

$$\begin{aligned} & \sum_{t=2..T} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right) \right) \\ & + \sum_{b \in B_s^{HE}} \left( 10ORConv \left( \sum_{k \in K_{T,b}^{1oS}} S10SDG_{T,b,k}^{PDS} + \sum_{k \in K_{T,b}^{1oN}} S10NDG_{T,b,k}^{PDS} \right) \right. \\ & \left. + 30ORConv \left( \sum_{k \in K_{T,b}^{3oR}} S30RDG_{T,b,k}^{PDS} \right) \right) = MaxSDEL_{tod,s} - EngyUsedSHE_s. \end{aligned}$$

9.8.3.6.1 then the *maximum daily energy limit* constraint is considered to be binding for the current *dispatch day* in the Pre-Dispatch Scheduling algorithm. In such circumstances, the following constraints shall apply for all time-steps  $t \in TS_{tod}$ :

$$\begin{aligned}
\sum_{b \in B_s^{HE}} \sum_{k \in K_{t,b}^E} SDG_{t,b,k} &\leq \sum_{b \in B_s^{HE}} \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} + \epsilon, \\
\sum_{b \in B_s^{HE}} \left( \sum_{k \in K_{t,b}^E} SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \right) \\
&\leq MaxSDEL_{tod,s} - EngyUsedSHE_s - \sum_{b \in B_s^{HE}} \sum_{\tau=2}^{t-1} \sum_{k \in K_{\tau,b}^E} SDG_{\tau,b,k}^{PDS}.
\end{aligned}$$

where  $\epsilon$  is a small positive constant.

9.8.3.6.2 If the pre-dispatch look-ahead period spans two *dispatch days*, if there exists a time-step  $T \in TS_{tom}$  such that:

$$\begin{aligned}
\sum_{t=t_{tom}..T} \left( \sum_{b \in B_s^{HE}} \left( ODG_{t,b}^{PDS} \cdot MinQDGC_b + \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} \right) \right) \\
+ \sum_{b \in B_s^{HE}} \left( 10ORConv \left( \sum_{k \in K_{T,b}^{10S}} S10SDG_{T,b,k}^{PDS} + \sum_{k \in K_{T,b}^{10N}} S10NDG_{T,b,k}^{PDS} \right) \right) \\
+ 30ORConv \left( \sum_{k \in K_{T,b}^{30R}} S30RDG_{T,b,k}^{PDS} \right) = MaxSDEL_{tom,s}
\end{aligned}$$

9.8.3.6.3 then the *maximum daily energy limit* constraint is considered to be binding for the next *dispatch day* in the Pre-Dispatch Scheduling algorithm. In such circumstances, the following constraints shall apply for all time-steps  $t \in TS_{tom}$ :

$$\begin{aligned}
\sum_{b \in B_s^{HE}} \sum_{k \in K_{t,b}^E} SDG_{t,b,k} &\leq \sum_{b \in B_s^{HE}} \sum_{k \in K_{t,b}^E} SDG_{t,b,k}^{PDS} + \epsilon, \\
\sum_{b \in B_s^{HE}} \left( \sum_{k \in K_{t,b}^E} SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10S}} S10SDG_{t,b,k} + \sum_{k \in K_{t,b}^{10N}} S10NDG_{t,b,k} + \sum_{k \in K_{t,b}^{30R}} S30RDG_{t,b,k} \right) \\
&\leq MaxSDEL_{tom,s} - \sum_{b \in B_s^{HE}} \sum_{\tau=tom}^{t-1} \sum_{k \in K_{\tau,b}^E} SDG_{\tau,b,k}^{PDS}.
\end{aligned}$$

where  $\epsilon$  is a small positive constant.

9.8.3.7 For a *dispatchable* hydroelectric *generation resource* for which a *MWh ratio* was respected in the Pre-Dispatch Scheduling algorithm, such *resource* shall be scheduled between its Pre-Dispatch Scheduling algorithm schedule plus or minus a tolerance  $\Delta$  specified by the *IESO*. The *resource* schedule shall be limited by its *offer* quantity bounds, in section 9.5.1, and any applicable *resource* minimum or maximum constraints, in section 9.5.2. For all linked downstream *dispatchable* hydroelectric *generation resources*  $b_2$  such that  $(b_1, b_2) \in LNKC$  where  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$  and all time-steps  $t \in TS$ :

$$\begin{aligned} ODG_{t,b_2}^{PDS} \cdot MinQDGC_{b_2} + \sum_{k \in K_{t,b_2}^E} SDG_{t,b_2,k}^{PDS} - \Delta &\leq ODG_{t,b_2}^{PDS} \cdot MinQDGC_{b_2} + \sum_{k \in K_{t,b_2}^E} SDG_{t,b_2,k} \\ &\leq ODG_{t,b_2}^{PDS} \cdot MinQDGC_{b_2} + \sum_{k \in K_{t,b_2}^E} SDG_{t,b_2,k}^{PDS} + \Delta. \end{aligned}$$

9.8.3.7.1 For all linked *dispatchable* hydroelectric *generation resources*  $b_1$  such that  $(b_1, b_2) \in LNKC$  where  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$  and all time-steps  $t \in TS$  such that  $t + LagC_{b_1,b_2} \leq n_{LAP}$ :

$$\begin{aligned} ODG_{t,b_1}^{PDS} \cdot MinQDGC_{b_1} + \sum_{k \in K_{t,b_1}^E} SDG_{t,b_1,k}^{PDS} - \Delta &\leq ODG_{t,b_1}^{PDS} \cdot MinQDGC_{b_1} + \sum_{k \in K_{t,b_1}^E} SDG_{t,b_1,k} \\ &\leq ODG_{t,b_1}^{PDS} \cdot MinQDGC_{b_1} + \sum_{k \in K_{t,b_1}^E} SDG_{t,b_1,k}^{PDS} + \Delta. \end{aligned}$$

## 9.9 Outputs

9.9.1 Outputs for the Pre-Dispatch Pricing algorithm include the following:

- 9.9.1.1 shadow prices;
- 9.9.1.2 *locational marginal prices* and their components; and
- 9.9.1.3 sensitivity factors.



# 10 Constrained Area Conditions Test

## 10.1 Purpose

- 10.1.1 The Constrained Area Conditions Test shall:
  - 10.1.1.1 identify when and where competition is restricted; and
  - 10.1.1.2 determine which *resources* shall have their *financial dispatch data parameters* be subject to the Conduct Test in section 11 and the thresholds above the *reference levels* that shall be used in the Conduct Test.

## 10.2 Information, Sets, Indices and Parameters

- 10.2.1 The *narrow constrained areas* and *dynamic constrained areas* and the information published therein in accordance with section 22 of Chapter 7 shall be inputs for the Constrained Area Conditions Test.
- 10.2.2 Information, sets, indices and parameters for the Constrained Area Conditions Test are described in sections 3 and 4. In addition, the following prices produced by the Pre-Dispatch Pricing algorithm shall be used by the Constrained Area Conditions Test:
  - 10.2.2.1  $LMP_{t,b}^{PDP}$ , which designates the *locational marginal price* for bus  $b \in B$  in time-step  $t \in TS$ ;
  - 10.2.2.2  $PCong_{t,b}^{PDP}$ , which designates the congestion component of the *locational marginal price* for bus  $b \in B$  in time-step  $t \in TS$ ;
  - 10.2.2.3  $ExtLMP_{t,d}^{PDP}$ , which designates the locational marginal price for intertie bus  $d \in D$  in time-step  $t \in TS$ ;
  - 10.2.2.4  $PExtCong_{t,d}^{PDP}$ , which designates the *intertie* congestion component of the *locational marginal price* for *intertie* bus  $d \in D$  in time-step  $t \in TS$ ;
  - 10.2.2.5  $PIntCong_{t,d}^{PDP}$ , which designates the internal congestion component of the *locational marginal price* for *intertie* bus  $d \in D$  in time-step  $t \in TS$ ;
  - 10.2.2.6  $IntLMP_{t,d}^{PDP}$ , which designates the *intertie border price* for *intertie* bus  $d \in D$  in time-step  $t \in TS$ ;

- 10.2.2.7  $SPNormT_{tf}^{PDP}$ , which designates the shadow price for the pre-contingency transmission constraint for *facility*  $f \in F$  in time-step  $t \in TS$ ;
- 10.2.2.8  $SPEmT_{h,cf}^{PDP}$ , which designates the shadow price for the post-contingency transmission constraint for *facility*  $f \in F$  in contingency  $c \in C$  in time-step  $t \in TS$ ;
- 10.2.2.9  $SPNIUExtBwdT_t^{PDP}$ , which designates the shadow price for the net *interchange schedule* limit constraint limiting increases in net imports between time-step  $(t - 1)$  and time-step  $t$ ;
- 10.2.2.10  $L30RP_{tb}^{PDP}$ , which designates the *locational marginal price* for *thirty-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$ ;
- 10.2.2.11  $L10NP_{tb}^{PDP}$ , which designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$ ; and
- 10.2.2.12  $L10SP_{tb}^{PDP}$ , which designates the *locational marginal price* for synchronized *ten-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$ .

## 10.3 Variables

- 10.3.1 The *pre-dispatch calculation engine* shall use the constrained area conditions tests in sections 10.4 and 10.5 to identify the *resources* that are part of the following data sets:
  - 10.3.1.1  $BCond_t^{NCA}$ , which designates the *resources* in a *narrow constrained area* that must be checked for local market power for *energy* in time-step  $t \in TS$ ;
  - 10.3.1.2  $BCond_t^{DCA}$ , which designates the *resources* in a *dynamic constrained area* that must be checked for local market power for *energy* in time-step  $t \in TS$ ;
  - 10.3.1.3  $BCond_t^{BCA}$ , which designates the *resources* in a broad constrained area to be checked for local market power for *energy* in time-step  $t \in TS$ ;
  - 10.3.1.4  $BCond_t^{GMP}$ , which designates the *resources* to be checked for global market power for *energy* in time-step  $t \in TS$ ;

- 10.3.1.5  $BCond_t^{10S}$ , which designates that *resources* to be checked for local market power for synchronized *ten-minute operating reserve* in time-step  $t \in TS$ ;
- 10.3.1.6  $BCond_t^{10N}$ , which designates that *resources* to be checked for local market power for non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$ ;
- 10.3.1.7  $BCond_t^{30R}$ , which designates that *resources* to be checked for local market power for *thirty-minute operating reserve* in time-step  $t \in TS$ ;
- 10.3.1.8  $BCond_t^{GMP10S}$ , which designates that *resources* to be checked for global market power for synchronized *ten-minute operating reserve* in time-step  $t \in TS$ ;
- 10.3.1.9  $BCond_t^{GMP10N}$ , which designates that *resources* to be checked for global market power for non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$ ; and
- 10.3.1.10  $BCond_t^{GMP30R}$ , which designates that *resources* to be checked for global market power for *thirty-minute operating reserve* in time-step  $t \in TS$ .

## 10.4 Constrained Area Conditions Test for Local Market Power (Energy)

- 10.4.1 Constrained Area Conditions Test for *narrow constrained areas* and *dynamic constrained area*
  - 10.4.1.1 If at least one transmission constraint for a *narrow constrained area* or *dynamic constrained area* is binding in the Pre-Dispatch Pricing algorithm, then all *resources* identified within the *narrow constrained area* or *dynamic constrained area* shall undergo the applicable Conduct Test in section 11 and:
    - 10.4.1.1.1 For each  $n \in NCA$  and time-step  $t \in TS$ : For each transmission *facility* that transmits flow into  $n$ ,  $f \in F_n^{NCA}$ , if  $SPNormT_{t,f}^{DDP} \neq 0$  or  $SPEmT_{t,f}^{DDP} \neq 0$  for the inbound flow limit, the *pre-dispatch calculation engine* will place  $n$  in the set  $NCA_t'$  and assign the *resources* in  $n$  to the set  $BCond_t^{NCA}$ ; and
    - 10.4.1.1.2 For each  $d \in DCA$  and time-step  $t \in TS$ : For each transmission *facility* that transmits flow into  $d$ ,  $f \in F_d^{DCA}$ , if

$SPNormT_{t,f}^{DDP} \neq 0$  or  $SPEmT_{t,c,f}^{DDP} \neq 0$  for the inbound flow limit, the *pre-dispatch calculation engine* will place  $d$  in the set  $DCA_t'$  and assign the *resources* in  $n$  to the set  $BCond_t^{DCA}$ .

10.4.1.2 Each *narrow constrained area* and *dynamic constrained area* that meets the criteria in section 10.4.1.1 shall be assigned to one of the following subsets, as appropriate:

10.4.1.2.1  $NCA_t'$ , which designates the *narrow constrained areas* that qualify for market power mitigation for *energy* in time-step  $t \in TS$ ; and

10.4.1.2.2  $DCA_t'$ , which designates the *dynamic constrained areas* that qualify for market power mitigation for *energy* in time-step  $t \in TS$ .

10.4.2 Constrained Area Conditions Test for the Broad Constrained Area

10.4.2.1 If the congestion component of the *locational marginal price* of a *resource* is greater than  $BCACondThresh$  and the *resource* is not part of a *narrow constrained area* or *dynamic constrained area* that has a binding transmission constraint, then the *resource* shall be tested using the broad constrained area thresholds. For each time-step  $t \in TS$  and bus  $b \in B^{DG}$  such that  $b \notin BCond_t^{NCA} \cup BCond_t^{DCA}$ , if  $PCong_{t,b}^{DDP} > BCACondThresh$ , the *pre-dispatch calculation engine* will then place *resource*  $b$  in the set  $BCond_t^{BCA}$ .

## 10.5 Constrained Area Conditions Test for Global Market Power (Energy)

10.5.1 The *pre-dispatch calculation engine* shall test *resources* that can meet incremental load within Ontario for global market power, subject to section 10.5.2, if:

10.5.1.1 the *intertie border prices* at the *global market power reference intertie zones* are greater than the  $IBPThresh$  threshold value, indicated in time-step  $t \in TS$  by:

10.5.1.1.1  $IntLMP_{t,d}^{DDP} > IBPThresh$  for *bids* and *offers*,  $d \in D^{GMPRef}$ , corresponding to the *boundary entity resource* bus for the *global market power reference intertie zones*; and

10.5.1.2 at least one of the following conditions is met:

10.5.1.2.1 import congestion, represented by a negative *intertie* congestion component, is present on all of the *global market power reference intertie zones*, indicated in time-steps  $t = \{2,3\}$  by:

10.5.1.2.1.1  $PExtCong_{t,d}^{PDP} < 0$  for *bids* and *offers*,  $d \in D^{GMPRef}$ , corresponding to the *boundary entity resource* bus for the *global market power reference intertie zone*; or

10.5.1.2.1.2 the net *interchange schedule* limit is binding for imports, represented by a non-zero net *interchange schedule* limit shadow price for incremental imports, indicated in time-steps  $t = \{2,3\}$  by:

$$SPNIUExtBwdT_t^{PDP} \neq 0$$

10.5.2 If the conditions in sections 10.5.1 are met, then the *pre-dispatch calculation engine* shall test *resources* that can meet incremental load within Ontario for global market power, for each time-step  $t \in TS$ , place all  $b \in B^{DG}$  in the set  $BCond_t^{GMP}$ , unless they are excluded because one of the following two conditions:

10.5.2.1 the *resources* in any zone have congestion components at least \$1/MWh below the internal congestion component at all of the *global market power reference intertie zones*:

10.5.2.1.1 if  $PCong_{t,b}^{PDP} < PIntCong_{t,d}^{PDP} - \$1/\text{MWh}$  where  $d \in D^{GMPRef}$  is true for all *global market power reference intertie zones*, or

10.5.2.2 the *resources* cannot meet the incremental load because of a binding transmission constraint:

10.5.2.2.1 if *resources* cannot meet incremental load because of any binding transmission *facility* where  $SPNormT_{t,f}^{PDP} \neq 0$  or  $SPEmT_{t,c,f}^{PDP} \neq 0$ .

## 10.6 Constrained Area Conditions Test for Local Market Power (Operating Reserve)

10.6.1 Subject to section 10.6.2, for a regional minimum requirement of greater than zero for a specific class of *operating reserve*, then all *resources* within the region with *offers* for classes of *operating reserve* that can satisfy the requirements of the specific class of *operating reserve* shall be tested for local market power:

10.6.1.1 if  $b$  is in a region with a non-zero minimum requirement, then  $b$  is subject to the Conduct Test and is placed in the set  $BCond_t^{10S}$ ,  $BCond_t^{10N}$ , or  $BCond_t^{80R}$

10.6.2 A *resource* shall not qualify for local market power mitigation testing for *operating reserve* if the *resource* is located in a region with a binding maximum constraint and for each *resource*  $b \in B^{DG} \cup B^{DL}$  and time-step  $t \in TS$ :

10.6.2.1 if  $b$  is in a region with a binding maximum restriction constraint, then  $b$  is exempt from the Conduct Test.

## 10.7 Constrained Area Conditions Test for Global Market Power (Operating Reserve)

10.7.1 A *resource* shall be subject to global market power mitigation testing for *operating reserve* if its *offers* for a class of *operating reserve* where the *locational marginal price* for that class of *operating reserve* is greater than *ORGCondThresh*.

10.7.2 Subject to section 10.7.3, if the condition in section 10.7.1 has been met for a class of *operating reserve*, then all *resources* with *offers* for classes of *operating reserve* that can satisfy the requirements of that class of *operating reserve* shall be tested and for each  $b \in B^{DG} \cup B^{DL}$  and time-step  $t \in TS$ :

10.7.2.1 if  $L10SP_{t,b}^{DDP} > ORGCondThresh$ , the *pre-dispatch calculation engine* shall add *resource*  $b$  to  $BCond_t^{GMP10S}$ ;

10.7.2.2 if  $L10NP_{t,b}^{DDP} > ORGCondThresh$ , the *pre-dispatch calculation engine* shall add *resource*  $b$  to  $BCond_t^{GMP10N}$ ; and

10.7.2.2 if  $L30RP_{t,b}^{DDP} > ORGCondThresh$ , the *pre-dispatch calculation engine* shall add *resource*  $b$  to  $BCond_t^{GMP30R}$ .

10.7.3 If a *resource* is located in a region with a binding regional maximum constraint, then the *resource* shall not qualify for global market power mitigation testing for *operating reserve*:

- 10.7.3.1 if  $b$  is in a region with a binding maximum constraint, then  $b$  shall be exempt from the Conduct Test.

## 10.8 Outputs

- 10.8.1 Outputs of the Constrained Area Conditions Test include the list of *resources* that will be subject to the Conduct Test in section 11 and the thresholds that will be used in the Conduct Test for those *resources*.

# 11 Conduct Test

## 11.1 Purpose

- 11.1.1 The Conduct Test shall verify whether the *financial dispatch data parameter* values submitted by *registered market participants* for *resources* identified in section 10.8.1 are within the applicable threshold level of the *reference level values* for those *resources*.

## 11.2 Information, Sets, Indices and Parameters

- 11.2.1 Information, sets, indices and parameters for the Conduct Test are described in sections 3 and 4. In addition, the list of *resources* produced pursuant to section 10.8.1 shall be used by the Conduct Test.

## 11.3 Variables

- 11.3.1 The *pre-dispatch calculation engine* shall apply the Conduct Test set out in sections 11.4 and 11.5 to the *resources* identified by the Constrained Area Conditions Test in accordance with section 10.8, to identify the following data sets:

- 11.3.1.1 The sets of *resources* that failed the Conduct Test for at least one *financial dispatch data parameter*, where:

11.3.1.1.1  $BCT_t^{NCA}$  designates the *resources* in a *narrow constrained area* that failed the Conduct Test for at least one *financial dispatch data parameter* in time-step  $t \in TS$ ;

11.3.1.1.2  $BCT_t^{DCA}$  designates the *resources* in a *dynamic constrained area* that failed the Conduct Test for at

least one *financial dispatch data parameter* in time-step  $t \in TS$ ;

11.3.1.1.3  $BCT_t^{BCA}$  designates the *resources* in a broad constrained area that failed the Conduct Test for at least one *financial dispatch data parameter* in time-step  $t \in TS$ ;

11.3.1.1.4  $BCT_t^{GMP}$  designates the *resources* that failed the global market power for *energy* Conduct Test for at least one *financial dispatch data parameter* in time-step  $t \in TS$ ;

11.3.1.1.5  $BCT_t^{ORL}$  designates the *resources* that failed the local market power for *operating reserve* Conduct Test for at least one *dispatch data parameter* in time-step  $t \in TS$ ; and

11.3.1.1.6  $BCT_t^{ORG}$  designates the *resources* that failed the global market power Conduct Test for *operating reserve* for at least one *financial dispatch data parameter* in time-step  $t \in TS$ .

11.3.1.2 The following *financial dispatch data parameters* for all time-steps  $t \in TS$ :

11.3.1.2.1  $PARAME_{t,br}$  which designates the set of *dispatch data parameters* that failed the *energy* Conduct Test at bus  $b \in \{BCT_t^{NCA} \cup BCT_t^{DCA} \cup BCT_t^{BCA} \cup BCT_t^{GMP}\}$  in time-step  $t$ , and may include the following *financial dispatch data parameters*:

11.3.1.2.1.1  $EnergyOffer_k$ , which designates a non-zero quantity of *energy* above the *minimum loading point* in association with *offer lamination*  $k \in K_{t,b}^E$  failed the Conduct Test;

11.3.1.2.2 For all hours prior to and including the last hour where conditions are met for the *energy* Conduct Test:

11.3.1.2.2.1  $EnergyToMLR_k$ , which designates the non-zero quantity of *energy* up to the *minimum loading point* in association with *offer lamination*  $k \in K_{t,b}^{LTMPLP}$  failed the Conduct Test;



- 11.3.1.2.2.2 *SUOffer*, which designates the *start-up offer* failed the Conduct Test; and
- 11.3.1.2.2.3 *SNLOffer*, which designates the *speed no-load offer* failed the Conduct Test.
- 11.3.1.2.3 *PARAMOR<sub>t,b</sub>* designates the set of *financial dispatch data parameter* that failed the *operating reserve* Conduct Test for bus  $b \in \{BCT_t^{ORL} \cup BCT_t^{ORG}\}$  in time-step  $t$ , and may include the following *financial dispatch data parameter*:
  - 11.3.1.2.3.1 *OR10SOffer<sub>kt</sub>* which designates the non-zero quantity of synchronized *ten-minute operating reserve* in association with *offer* lamination  $k \in K_{t,b}^{10S}$  failed the Conduct Test;
  - 11.3.1.2.3.2 *OR10NOffer<sub>kt</sub>* which designates the non-zero quantity of non-synchronized *ten-minute operating reserve* in association with *offer* lamination  $k \in K_{t,b}^{10N}$  failed the Conduct Test; and
  - 11.3.1.2.3.3 *OR30ROffer<sub>kt</sub>* which designates the non-zero quantity of *thirty-minute operating reserve* in association with *offer* lamination  $k \in K_{t,b}^{30R}$  failed the Conduct Test;
- 11.3.1.2.4 For all hours prior to and including the last hour where conditions are met for the *operating reserve* Conduct Test:
  - 11.3.1.2.4.1 *SUOffer*, which designates the *start-up offer* failed the Conduct Test;
  - 11.3.1.2.4.2 *SNLOffer*, which designates the *speed no-load offer* failed the Conduct Test; and
  - 11.3.1.2.4.3 *EnergyToMLP<sub>kt</sub>* which designates the non-zero quantity of up to the *minimum loading point* in association

with offer lamination  $k \in K_{t,b}^E$  failed the Conduct Test.

## 11.4 Conduct Test for Energy

11.4.1 The *pre-dispatch calculation engine* shall perform the Conduct Test for *energy* for *resources* in a *narrow constrained area* that were identified pursuant to section 10.8.1 as follows, subject to sections 11.4.2 and 11.4.3. For each time-step  $t \in TS$  and  $b \in BCond_t^{NCA}$ , the *pre-dispatch calculation engine* shall:

- 11.4.1.1 Evaluate *energy offers above minimum loading point*. For all  $k \in K_{t,b}^E$ , if  $PDG_{t,b,k} > \min (PDGRef_{t,b,k'} + (abs(PDGRef_{t,b,k'}) * CTEnThresh1^{NCA}), PDGRef_{t,b,k'} + CTEnThresh2^{NCA})$ , where  $k' \in K_{t,b}^E$ , then the Conduct Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{NCA}$  and add  $EnergyOffer_k$  to  $PARAME_{t,b}$ ;
- 11.4.1.2 Evaluate *offers for energy* for the range of production up to *minimum loading point*. For all time-steps prior to and including the last time-step where conditions are met for the Constrained Area Conditions Test, for all  $k \in K_{t,b}^{LTMLP}$ , if  $PLTMLP_{t,b,k} > CTEnMinOffer$  and  $PLTMLP_{t,b,k} > \min (PLTMLPRef_{t,b,k'} + (abs(PLTMLPRef_{t,b,k'}) * CTEnThresh1^{NCA}), PLTMLPRef_{t,b,k'} + CTEnThresh2^{NCA})$ , where  $k' \in K_{t,b}^E$ , then the Conduct Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{NCA}$  and add  $EnergyToMLP_k$  to  $PARAME_{t,b}$  and  $PARAMOR_{t,b}$ ;
- 11.4.1.3 Evaluate *start-up offers*. For all time-steps prior to and including the last time-step  $t$  where conditions are met for the Constrained Area Conditions Test in section 10, if  $SUDG_{t,b} > SUDGRef_{t,b} + (abs(SUDGRef_{t,b}) * CTSUThresh^{NCA})$ , then the Conduct Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{NCA}$  and add  $SUOffer$  to  $PARAME_{t,b}$  and  $PARAMOR_{t,b}$ ; and
- 11.4.1.4 Evaluate *speed no-load offers*. For all time-steps prior to and including the last time-step where conditions are met for the Constrained Area Conditions Test, if  $SNL_{t,b} > SNLRef_{t,b} + (abs(SNLRef_{t,b}) * CTSNLThresh^{NCA})$ , then the Conduct Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{NCA}$  and add  $SNLOffer$  to  $PARAME_{t,b}$  and  $PARAMOR_{t,b}$ .

- 11.4.2 For *resources* identified pursuant to section 10.8.1 in a *dynamic constrained area* or broad constrained area, the *pre-dispatch calculation engine* shall use the steps in section 11.4.1, using *resources* in  $BCond_t^{DCA}$  or  $BCond_t^{BCA}$ , as the case may be, in place of  $BCond_t^{NCA}$  and using the applicable Conduct Test thresholds  $CTEnThresh1^{DCA}$ ,  $CTEnThresh2^{DCA}$ ,  $CTEnThresh1^{BCA}$ ,  $CTEnThresh2^{BCA}$ ,  $CTSUThresh^{DCA}$ ,  $CTSUThresh^{BCA}$ ,  $CTSNLThresh^{DCA}$ ,  $CTSNLThresh^{BCA}$ . If any of the *financial dispatch data parameters* of a *resource* fail the Conduct Test, the *resource* shall be assigned to subset  $BCT_h^{DCA}$  or  $BCT_h^{BCA}$ , as the case may be.
- 11.4.3 For *resources* identified pursuant to section 10.8.1 that were selected for global market power mitigation testing for *energy*, the *pre-dispatch calculation engine* shall use the steps in section 11.4.1, using *resources* in  $BCond_t^{GMP}$  in place of  $BCond_t^{NCA}$  and the applicable global market power Conduct Test thresholds  $CTEnThresh1^{GMP}$ ,  $CTEnThresh2^{GMP}$ ,  $CTSUThresh^{GMP}$ ,  $CTSNLThresh^{GMP}$ . If any of the applicable *financial dispatch data parameters* of a *resource* fails the Conduct Test, the *resource* shall be assigned to subset  $BCT_h^{GMP}$ .
- 11.4.4 If a *resource* is assigned to more than one of the sets,  $BCond_t^{NCA}$ ,  $BCond_t^{DCA}$ ,  $BCond_t^{BCA}$ , and  $BCond_t^{GMP}$ , only the Conduct Test with the most restrictive threshold levels shall be performed for that *resource*.

## 11.5 Conduct Test for Operating Reserve

- 11.5.1 The *pre-dispatch calculation engine* shall perform the Conduct Test for local market power for *operating reserve* for *resources* that were identified pursuant to section 10.8.1, as follows, subject to 11.5.3. For each time-step  $t \in TS$  and  $b \in BCond_t^{10S} \cup BCond_t^{10N} \cup BCond_t^{30R}$ , the *pre-dispatch calculation engine* shall:

11.5.1.1 Evaluate *offers* for *operating reserve* as follows:

- 11.5.1.1.1 for all  $k \in K_{t,b}^{10S}$  such that  $P10SDG_{t,b,k} > CTORMinOffer$  and  $P10SDG_{t,b,k} > \min(P10SDGRef_{t,b,k} + (abs(P10SDGRef_{t,b,k}) * CTORTresh1^{ORL}), P10SDGRef_{t,b,k} + CTORTresh2^{ORL})$ , where  $k' \in K_{t,b}^{10S}$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $OR10SOffer_k$  to  $PARAMOR_{t,b}$ ;
- 11.5.1.1.2 for all  $k \in K_{t,b}^{10N}$  such that  $P10NDG_{t,b,k} > CTORMinOffer$  and  $P10NDG_{t,b,k} > \min(P10NDGRef_{t,b,k} + (abs(P10NDGRef_{t,b,k}) * CTORTresh1^{ORL}), P10NDGRef_{t,b,k} + CTORTresh2^{ORL})$ ,

where  $k' \in K_{h,b}^{10N}$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $OR10NOffer_k$  to  $PARAMOR_{t,b}$ ;

- 11.5.1.1.3 for all  $k \in K_{t,b}^{30R}$  such that  $P30RDG_{t,b,k} > CTORMinOffer$  and  
 $P30RDG_{t,b,k} > \min(P30RDGRef_{t,b,k} + (abs(P30RDGRef_{t,b,k}) * CTORThresh1^{ORL}), P30RDGRef_{t,b,k} + CTORThresh2^{ORL})$ ,  
 where  $k' \in K_{h,b}^{30R}$ , then the Conduct Test was failed for the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $OR30ROffer_k$  to  $PARAMOR_{t,b}$ ;
- 11.5.1.1.4 for all  $j \in J_{t,b}^{10S}$  if  $P10SDL_{t,b,j} > CTORMinOffer$  and  
 $P10SDL_{t,b,j} > \min(P10SDLRef_{t,b,j} + (abs(P10SDLRef_{t,b,j}) * CTORThresh1^{ORL}), P10SDLRef_{t,b,j} + CTORThresh2^{ORL})$ , where  $j' \in J_{t,b}^{10S}$ , then the Conduct Test was failed for the *dispatchable load* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $OR10SOffer_k$  to  $PARAMOR_{t,b}$ ;
- 11.5.1.1.5 for all  $j \in J_{t,b}^{10N}$  if  $P10NDL_{t,b,j} > CTORMinOffer$  and  
 $P10NDL_{t,b,j} > \min(P10NDLRef_{t,b,j} + (abs(P10NDLRef_{t,b,j}) * CTORThresh1^{ORL}), P10NDLRef_{t,b,j} + CTORThresh2^{ORL})$ , where  $j' \in J_{t,b}^{10N}$ , then the Conduct Test was failed for the *dispatchable load* at bus  $b$  and the *day-ahead market calculation engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $OR10NOffer_k$  to  $PARAMOR_{t,b}$ ; and
- 11.5.1.1.6 for all  $j \in J_{t,b}^{30R}$  if  $P30RDL_{t,b,j} > CTORMinOffer$  and  
 $P30RDL_{t,b,j} > \min(P30RDLRef_{t,b,j} + (abs(P30RDLRef_{t,b,j}) * CTORThresh1^{ORL}), P30RDLRef_{t,b,j} + CTORThresh2^{ORL})$ , where  $j' \in J_{t,b}^{30R}$ , then the Conduct Test was failed for the *dispatchable load* at bus  $b$  and the *day-ahead market calculation*

*engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $OR30ROffer_k$  to  $PARAMOR_{t,b}$ ;

11.5.1.2 Evaluate *start-up offers*. For all time-steps prior to and including the last time-step where conditions are met for the Constrained Area Conditions Test, if  $SUDG_{t,b} > SUDGRef_{t,b} + (abs(SUDGRef_{t,b}) * CTSUThresh^{ORL})$ , then the Conduct Test failed for the *resource* at bus *b* and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $SUOffer$  to  $PARAMOR_{t,b}$  and  $PARAME_{t,b}$ ;

11.5.1.3 Evaluate *speed no-load offers*. For all time-steps prior to and including the last time-step where conditions are met for the Constrained Area Conditions Test, if  $SNL_{t,b} > SNLRef_{t,b} + (abs(SNLRef_{t,b}) * CTSNLThresh^{ORL})$ , then the Conduct Test was failed for the *resource* at bus *b* and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $SNLOffer$  to  $PARAMOR_{t,b}$  and  $PARAME_{t,b}$ ; and

11.5.1.4 Evaluate *offers for energy* for the range of production up to the *minimum loading point*. For all time-steps prior to and including the last time-step where conditions are met for the Constrained Area Conditions Test, for all  $k \in K_{t,b}^{LTMLP}$ , if  $PLTMLP_{t,b,k} > min(PLTMLPRef_{t,b,k} + (abs(PLTMLPRef_{t,b,k}) * CTEnThresh1^{ORL}), PLTMLPRef_{t,b,k} + CTEnThresh2^{ORL})$ , where  $k' \in K_{t,b}^E$ , then the Conduct Test was failed for the *resource* at bus *b* and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BCT_t^{ORL}$  and add  $EnergyToMLP_k$  to  $PARAMOR_{t,b}$  and  $PARAME_{t,b}$ .

11.5.2 The *pre-dispatch calculation engine* shall perform the Conduct Test for global market power for *operating reserve* for *resources* that were identified pursuant to section 10.8.1. The *pre-dispatch calculation engine* shall use the steps set out in section 11.5.1 using *resources* in  $BCond_t^{GMP10S}$ ,  $BCond_t^{GMP10N}$ , and  $BCond_t^{GMP30R}$  in place of  $BCond_t^{10S}$ ,  $BCond_t^{10N}$ , and  $BCond_t^{30R}$ , respectively, and the applicable Conduct Test thresholds ( $CTORThresh1^{ORG}$ ,  $CTORThresh2^{ORG}$ ,  $CTSUThresh^{ORG}$ ,  $CTSNLThresh^{ORG}$ ,  $CTEnThresh1^{ORG}$ ,  $CTEnThresh2^{ORG}$ ). The *resources* shall be assigned to the subset  $BCT_h^{ORG}$ .

11.5.3 If a *resource* is assigned to more than one of  $BCond_t^{GMP10S}$ ,  $BCond_t^{GMP10N}$ , and  $BCond_t^{GMP30R}$ , only the Conduct Test with the most restrictive threshold levels shall be performed for that *resource*.

## 11.6 Outputs

- 11.6.1 Subject to section 11.6.2, the outputs of the Conduct Test shall include the following for each time-step  $t \in TS$ :
  - 11.6.1.1 The set of *resources* that failed the Conduct Test for at least one *financial dispatch data parameter* by condition type;
  - 11.6.1.2 The *financial dispatch data parameters* that failed the Conduct Test for the *resource* at bus  $b$ ; and
  - 11.6.1.3 A revised set of *financial dispatch data parameters* replaced with *reference level values* for *resources* that:
    - 11.6.1.3.1 has one or more *financial dispatch data parameters* that failed a Conduct Test for the current *pre-dispatch calculation engine* run; and
    - 11.6.1.3.2 has one or more *financial dispatch data parameters* that failed both the Conduct Test and failed the Price Impact Test in previous *pre-dispatch calculation engine* runs.
  - 11.6.1.4 For *offers* for *energy* and *operating reserve* with multiple laminations:
    - 11.6.1.4.1 if the *offer* lamination for *energy* that corresponds to the *minimum loading point* fails the Conduct Test, the *pre-dispatch calculation engine* shall replace all *offer* laminations for *energy* up to the *minimum loading point*;
    - 11.6.1.4.2 if one or more offer laminations for *energy* above the *minimum loading point* fails the Conduct Test, the *pre-dispatch calculation engine* shall replace all *offer* laminations for *energy* up to and above the *minimum loading point*; and
    - 11.6.1.4.3 if one or more *offer* laminations for *operating reserve* fails the Conduct Test, the *pre-dispatch calculation engine* shall replace all *offer* laminations for *operating reserve*.
  - 11.6.1.5 For a *non-quick start resource* whose *start-up offer* failed the Conduct Test, identified in section 11.6.1.1, the *pre-dispatch calculation engine*

shall use the *start-up offer reference level value* to evaluate any advancements pursuant to section 5.7.

- 11.6.2 The *pre-dispatch calculation engine* shall not replace the *financial dispatch data parameter* for a *resource* with that *resource's* applicable *reference level value* if the *financial dispatch data parameter* is less than the corresponding *reference level value*.

## 12 Reference Level Scheduling

### 12.1 Purpose

- 12.1.1 The *pre-dispatch calculation engine* shall perform the Reference Level Scheduling algorithm where at least one *financial dispatch data parameter* for a *resource* failed the Conduct Test in section 11.
- 12.1.2 The Reference Level Scheduling algorithm shall perform a *security*-constrained unit commitment and economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, including *reference level value* for *resources* subject to 14.7.1.3 and 12.2.2, to meet the *IESO's* province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the pre-dispatch look-ahead period.

### 12.2 Information, Sets, Indices and Parameters

- 12.2.1 Information, sets, indices and parameters used by the Reference Level Scheduling algorithm are described in section 3 and section 4. In addition, the list of *resources* that failed the Conduct Test from section 11.6.1.1 and a revised set of *financial dispatch data parameters* from section 11.6.1.3, for those *resources* shall be used by the Reference Level Scheduling algorithm
- 12.2.2 The Reference Level Scheduling algorithm shall use the *reference level value* that corresponds to any *financial dispatch data parameter* submitted for a *resource* that failed the Conduct Test.

### 12.3 Variables and Objective Function

- 12.3.1 The *pre-dispatch calculation engine* shall solve for the variables listed in section 8.3.1.
- 12.3.2 The objective function for the Reference Level Scheduling algorithm shall be the same as the objective function in section 8.3.2, subject to section 12.4.

## 12.4 Constraints

- 12.4.1 The constraints in sections 8.4 through 8.7 apply in the Reference Level Scheduling algorithm, except that the sensitivities and limits considered for IESO internal transmission limits shall be those provided by the most recent *security* assessment function iteration of the Reference Level Scheduling algorithm.

## 12.5 Outputs

- 12.5.1 Outputs of the Reference Level Scheduling algorithm include *resource* schedules and commitments.

# 13 Reference Level Pricing

## 13.1 Purpose

- 13.1.1 The *pre-dispatch calculation engine* shall perform the Reference Level Pricing algorithm whenever the Reference Level Scheduling algorithm has been performed.
- 13.1.2 The Reference Level Pricing algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants*, *reference level value* for *resources* subject to 14.7.1.3 and 13.2.2, and *resource* schedules and commitments produced by the Reference Level Scheduling algorithm, to meet the *IESO's* province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each hour of the pre-dispatch look-ahead period.

## 13.2 Information, Sets, Indices and Parameters

- 13.2.1 Information, sets, indices and parameters used by the Reference Level Pricing algorithm are described in sections 3 and 4. In addition, the following *resource* schedule and commitments from the Reference Level Scheduling algorithm shall be used by the Reference Level Pricing algorithm:

- 13.2.1.1  $SDG_{t,b,k}^{RLS}$ , which designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide above  $MinQDGC_b$  at bus  $b \in B^{ELR} \cup B^{HE}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^E$ ;



- 13.2.1.2  $ODG_{t,b}^{RLS}$ , which designates whether a *dispatchable generation resource* at bus  $b \in B^{DG}$  was scheduled at or above its *minimum loading point* in time-step  $t \in TS$ ;
- 13.2.1.3  $S10SDG_{t,b,k}^{RLS}$ , which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^{10S}$ ;
- 13.2.1.4  $S10NDG_{t,b,k}^{RLS}$ , which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^{10N}$ ;
- 13.2.1.5  $S30RDG_{t,b,k}^{RLS}$ , which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{ELR} \cup B^{HE}$  in time-step  $t \in TS$  in association with lamination  $k \in K_{t,b}^{30R}$ ; and
- 13.2.1.6  $OHO_{t,b}^{RLS}$ , which designates whether the *dispatchable hydroelectric generation resource* at bus  $b \in B^{HE}$  has been scheduled at or above  $MinHO_{t,b}$  in time-step  $t \in TS$ .

- 13.2.2 The Reference Level Pricing algorithm shall use a *resource's reference level value* for any *financial dispatch data parameters* submitted by *registered market participants* that failed the Conduct Test in Section 11.

### 13.3 Variables and Objective Function

- 13.3.1 The *pre-dispatch calculation engine* shall solve for the variables set out in section 9.3.1.
- 13.3.2 The objective function used in the Reference Level Pricing algorithm shall be the same as the objective function set out in section 9.3.2, subject to section 13.4.

### 13.4 Constraints

- 13.4.1 The constraints that apply in the Reference Level Pricing algorithm shall be the same as the constraints in sections 9.4 through 9.8, with the following exceptions:
  - 13.4.1.1 the marginal loss factors used in the *energy balance constraint* in section 9.7.1 shall be fixed to the marginal loss factors used in the

last optimization function iteration of the Reference Level Scheduling algorithm;

13.4.1.2 the sensitivities and limits in section 9.7.3 shall be replaced with the most recent *security* assessment function iteration of the Reference Level Pricing algorithm; and

13.4.1.3 for the constraints in section 9.8, the outputs from the Pre-Dispatch Scheduling algorithm shall be replaced with the outputs from the Reference Level Scheduling algorithm as follows:

13.4.1.3.1  $SDG_{t,b,k}^{PDS}$  shall be replaced by  $SDG_{t,b,k}^{RLS}$  for all  $t \in TS$ ,  $b \in B^{ELR} \cup B^{HE}$ ,  $k \in K_{t,d}^E$ ;

13.4.1.3.2  $ODG_{t,b}^{PDS}$  shall be replaced by  $ODG_{t,b}^{RLS}$  for all  $t \in TS$ ,  $b \in B^{DG}$ ;

13.4.1.3.3  $IDG_{t,b}^{PDS}$  shall be replaced by  $IDG_{t,b}^{RLS}$  for all  $t \in TS$ ,  $b \in B^{DG}$ ;

13.4.1.3.4  $S10SDG_{t,b,k}^{PDS}$  shall be replaced by  $S10SDG_{t,b,k}^{RLS}$  for all  $t \in TS$ ,  $b \in B^{ELR} \cup B^{HE}$ ,  $k \in K_{t,b}^{10S}$ ;

13.4.1.3.5  $S10NDG_{t,b,k}^{PDS}$  shall be replaced by  $S10NDG_{t,b,k}^{RLS}$  for all  $t \in TS$ ,  $b \in B^{ELR} \cup B^{HE}$ ,  $k \in K_{t,b}^{10N}$ ;

13.4.1.3.6  $S30RDG_{t,b,k}^{PDS}$  shall be replaced by  $S30RDG_{t,b,k}^{RLS}$  for all  $t \in TS$ ,  $b \in B^{ELR} \cup B^{HE}$ ,  $k \in K_{t,b}^{30R}$ ; and

13.4.1.3.7  $OHO_{t,b}^{PDS}$  shall be replaced by  $OHO_{t,b}^{RLS}$  for all  $t \in TS$ ,  $b \in B^{HE}$ .

## 13.5 Outputs

13.5.1 Outputs of the Reference Level Pricing algorithm include the following:

13.5.1.1 shadow prices; and

13.5.1.2 *locational marginal prices* and their components.

# 14 Price Impact Test

## 14.1 Purpose

- 14.1.1 The *pre-dispatch calculation engine* shall perform the Price Impact Test whenever at least one *financial dispatch data parameter* for a *resource* failed the Conduct Test.
- 14.1.2 The Price Impact Test shall:
  - 14.1.2.1 compare the *locational marginal prices* for *energy* or *operating reserve* produced by the Pre-Dispatch Pricing algorithm with those produced by the Reference Level Pricing algorithm; and
  - 14.1.2.2 consider the corresponding *offer* parameters to have failed the price impact test if the difference in price in section 14.1.2.1 is greater than the applicable impact threshold in section 4.3.9.

## 14.2 Information, Sets, Indices and Parameters

- 14.2.1 Information, sets, indices and parameters for the Price Impact Test are described in sections 3 and 4. In addition, the following *locational marginal prices* from the Pre-Dispatch Pricing algorithm and the Reference Level Pricing algorithm shall be used:
  - 14.2.1.1  $LMP_{t,b}^{DDP}$ , which designates the *locational marginal price* for *energy* at bus  $b \in B$  in time-step  $t \in TS$  from the Pre-Dispatch Pricing algorithm;
  - 14.2.1.2  $L30RP_{t,b}^{DDP}$ , which designates the *locational marginal price* for *thirty-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$  from the Pre-Dispatch Pricing algorithm;
  - 14.2.1.3  $L10NP_{t,b}^{DDP}$ , which designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$  from the Pre-Dispatch Pricing algorithm;
  - 14.2.1.4  $L10SP_{t,b}^{DDP}$ , which designates the *locational marginal price* for synchronized *ten-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$  from the Pre-Dispatch Pricing algorithm;
  - 14.2.1.5  $LMP_{t,b}^{RLP}$ , which designates the *locational marginal price* for *energy* at bus  $b \in B$  in time-step  $t \in TS$  from the Reference Level Pricing algorithm;

- 14.2.1.6  $L30RP_{t,b}^{RLP}$ , which designates the *locational marginal price* for *thirty-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$  from the Reference Level Pricing algorithm;
- 14.2.1.7  $L10NP_{t,b}^{RLP}$ , which designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$  from the Reference Level Pricing algorithm; and
- 14.2.1.8  $L10SP_{t,b}^{RLP}$ , which designates the *locational marginal price* for synchronized *ten-minute operating reserve* at bus  $b \in B$  in time-step  $t \in TS$  from the Reference Level Pricing algorithm.

## 14.3 Variables

- 14.3.1 The *pre-dispatch calculation engine* shall apply the Price Impact Test as set out in sections 14.4 and 14.5 for the *resources* identified in accordance with section 10.3.1, to identify:
  - 14.3.1.1 A set of *resources* that failed the Price Impact Test for each condition for all time-steps  $t \in TS$ , where:
    - 14.3.1.1.1  $BIT_t^{NCA}$  designates the *resources* in a *narrow constrained area* that failed the Price Impact Test for the *locational marginal price for energy*;
    - 14.3.1.1.2  $BIT_t^{DCA}$  designates the *resources* in a *dynamic constrained area* that failed the Price Impact Test for *energy locational marginal price*;
    - 14.3.1.1.3  $BIT_t^{BCA}$  designates the *resources* in a broad constrained area that failed Price Impact Test for *energy locational marginal price*;
    - 14.3.1.1.4  $BIT_t^{GMP}$  designates the *resources* that failed the Global Market Power (*energy*) Price Impact Test for *energy locational marginal price*;
    - 14.3.1.1.5  $BIT_t^{ORL}$  designates the *resources* that failed the Local Market Power (*operating reserve*) Price Impact Test for at least one type of *operating reserve locational marginal price*;
    - 14.3.1.1.6  $BIT_t^{ORG}$  designates the *resources* that failed the Global Market Power (*operating reserve*) Price Impact Test for

at least one type of *operating reserve locational marginal price*; and

14.3.1.1.7  $LMPIT_{t,b}$  designates the *locational marginal price* that failed the Price Impact Test for bus  $b \in BIT_t^{NCA} \cup BIT_t^{DCA} \cup BIT_t^{BCA} \cup BIT_t^{GMP} \cup BIT_t^{ORL} \cup BIT_t^{ORG}$  in time-step  $t \in TS$  and

14.3.1.2 *Locational marginal prices* for *energy* and *operating reserve* for each *resource* at bus  $b \in B^{DG} \cup B^{DL}$  that failed the Price Impact Test, where:

14.3.1.2.1  $EnergyLMP$  designates that the *locational marginal price* for *energy* failed the Price Impact Test;

14.3.1.2.2  $OR10SLMP$  designates that the *synchronized ten-minute operating reserve locational marginal price* failed the Price Impact Test;

14.3.1.2.3  $OR10NLMP$  designates that the *non-synchronized ten-minute operating reserve locational marginal price* failed the Price Impact Test; and

14.3.1.2.4  $OR30RLMP$  designates that the *thirty-minute operating reserve locational marginal price* failed the Price Impact Test.

## 14.4 Price Impact Test for Energy

14.4.1 The *pre-dispatch calculation engine* shall perform the Price Impact Test for *resources* that were identified in the corresponding Conduct Test for *energy* in section 11.6.1.1, as follows:

14.4.1.1 For local market power for *energy*:

14.4.1.1.1 For each time-step  $t \in TS$  and  $b \in BCT_t^{NCA}$ , if  $LMP_{t,b}^{PDP} > \min(LMP_{t,b}^{RLP} + (abs(LMP_{t,b}^{RLP}) * ITThresh1^{NCA}), LMP_{t,b}^{RLP} + ITThresh2^{NCA})$ , the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{NCA}$  and add  $EnergyLMP$  to  $LMPIT_{t,b}$ ;

14.4.1.1.2 For each time-step  $t \in TS$  and  $b \in BCT_t^{DCA}$ , if  $LMP_{t,b}^{DDP} > \min(LMP_{t,b}^{RLP} + (abs(LMP_{t,b}^{RLP}) * ITThresh1^{DCA}), LMP_{t,b}^{RLP} + ITThresh2^{DCA})$ , the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{DCA}$  and add *EnergyLMP* to  $LMPIT_{t,b}$ ; and

14.4.1.1.3 For each time-step  $t \in TS$  and  $b \in BCT_t^{BCA}$ , if  $LMP_{t,b}^{DDP} > \min(LMP_{t,b}^{RLP} + (abs(LMP_{t,b}^{RLP}) * ITThresh1^{BCA}), LMP_{t,b}^{RLP} + ITThresh2^{BCA})$ , the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{BCA}$  and add *EnergyLMP* to  $LMPIT_{t,b}$ ; and

14.4.1.2 For global market power for *energy*:

14.4.1.2.1 For each time-step  $t \in TS$  and  $b \in BCT_t^{GMP}$ , if  $LMP_{t,b}^{DDP} > \min(LMP_{t,b}^{RLP} + (abs(LMP_{t,b}^{RLP}) * ITThresh1^{GMP}), LMP_{t,b}^{RLP} + ITThresh2^{GMP})$ , the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{GMP}$  and add *EnergyLMP* to  $LMPIT_{t,b}$ .

## 14.5 Price Impact Test for Operating Reserve

14.5.1 The *pre-dispatch calculation engine* shall perform the Price Impact Test for *resources* that were identified in the corresponding Conduct Test for *operating reserve* in section 11.6.1.1, as follows:

14.5.1.1 For local market power for *operating reserve*, for each time-step  $t \in TS$  and  $b \in BCT_t^{ORL}$ :

14.5.1.1.1 If  $L30RP_{t,b}^{DDP} > L30RP_{t,b}^{RLP}$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{ORL}$  and add *OR30RLMP* to  $LMPIT_{t,b}$ ;

- 14.5.1.1.2 If  $L10NP_{t,b}^{DDP} > L10NP_{t,b}^{RLP}$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{ORL}$  and add  $OR10NLMP$  to  $LMPIT_{t,b}$ ; and
- 14.5.1.1.3 If  $L10SP_{t,b}^{DDP} > L10SP_{t,b}^{RLP}$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{ORL}$  and add  $OR10SLMP$  to  $LMPIT_{t,b}$ ; and
- 14.5.1.2 For global market power for *operating reserve*, for each time-step  $t \in TS$  and  $b \in BCT_t^{ORG}$ :
- 14.5.1.2.1 If  $L30RP_{t,b}^{DDP} > \min(L30RP_{t,b}^{RLP} + (abs(L30RP_{t,b}^{RLP}) * ITThresh1^{ORG}), L30RP_{t,b}^{RLP} + ITThresh2^{ORG})$ , then the Price Impact Test was failed by *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{ORG}$  and add  $OR30RLMP$  to  $LMPIT_{t,b}$ ;
- 14.5.1.2.2 If  $L10NP_{t,b}^{DDP} > \min(L10NP_{t,b}^{RLP} + (abs(L10NP_{t,b}^{RLP}) * ITThresh1^{ORG}), L10NP_{t,b}^{RLP} + ITThresh2^{ORG})$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign the *resource* to subset  $BIT_t^{ORG}$  and add  $OR10NLMP$  to  $LMPIT_{t,b}$ ; and
- 14.5.1.2.3 If  $L10SP_{t,b}^{DDP} > \min(L10SP_{t,b}^{RLP} + (abs(L10SP_{t,b}^{RLP}) * ITThresh1^{ORG}), L10SP_{t,b}^{RLP} + ITThresh2^{ORG})$ , then the Price Impact Test was failed by the *resource* at bus  $b$  and the *pre-dispatch calculation engine* shall assign *resource* to subset  $BIT_t^{ORG}$  and add  $OR10SLMP$  to  $LMPIT_{t,b}$ .

## 14.6 Revised Financial Dispatch Data Parameter Determination

- 14.6.1 A *resource* that fails the Price Impact Test in a time-step ( $t$ ) shall have its *financial dispatch data parameters* revised as follows:
- 14.6.1.1 If the *resource* has failed a Price Impact Test for *energy* and is in  $BIT_t^{NCA}$ ,  $BIT_t^{DCA}$ ,  $BIT_t^{BCA}$ ,  $BIT_t^{GMP}$ , the *financial dispatch data parameters* in  $PARAME_{t,b}$  shall be used to determine the *financial dispatch data*

*parameters* that shall be replaced with the *resource's* applicable *reference level value*.

- 14.6.1.2 If the *resource* has failed a Price Impact Test for *operating reserve* and is in  $BIT_t^{ORL}$  or  $BIT_t^{ORG}$ , the *financial dispatch data parameters* in  $PARAMOR_{t,b}$  shall be used to determine the *financial dispatch data parameters* that shall be replaced with the *resource's* applicable *reference level value*.
- 14.6.1.3 If a *non-quick-start resource* has failed a Price Impact Test in any time-step, the *commitment cost parameters* (*start-up offer*, *speed-no-load offer*, or *energy offer* associated with the *minimum loading point*) that failed the corresponding Conduct Test shall be replaced with the *resource's* applicable *reference level value* for that time-step. For any time-steps prior, any *commitment cost parameters* for that *resource* that failed the Conduct Test shall be replaced with the *resource's* applicable *reference level value* in those time-steps. This is expressed as:
  - 14.6.1.3.1 For each time-step  $t \in TS$  and all  $b \in B^{NQS} \cap (BIT_t^{NCA} \cup BIT_t^{DCA} \cup BIT_t^{BCA} \cup BIT_t^{GMP})$ , for hours prior to and including the hour that failed the Price Impact Test,  $T \in \{1, \dots, T\}$ , if  $b \in BCT_T^{NCA} \cup BCT_T^{DCA} \cup BCT_T^{BCA} \cup BCT_T^{GMP}$  and  $PARAME_{T,b}$  contains any of the *commitment cost parameters*  $SUOffer$ ,  $SNLOffer$ , or  $EnergyToMLP_k$ , replace these parameters with *reference level values*.
- 14.6.1.4 Section 14.6.1.3 shall apply to the tests for local market power and global market power for *operating reserve*, except  $PARAMOR_{T,b}$  shall be checked in place of  $PARAME_{T,b}$ .
- 14.6.1.5 If a *resource* is in a *narrow constrained area* or a *dynamic constrained area* and has failed a Price Impact Test, each *resource* in the same *narrow constrained area* or *dynamic constrained area* that also failed the corresponding Conduct Test shall have its *offer data* replaced with its applicable *reference level value* for that hour. For each time-step  $t \in TS$ :
  - 14.6.1.5.1 if  $BIT_t^{NCA}$  includes one or more *resources* in a *narrow constrained area*,  $n$ , each *resource*  $b \in BCT_t^{NCA}$  for *narrow constrained area*,  $n$ , shall have the parameters in  $PARAME_{t,b}$  replaced with its *reference level values*; and



- 14.6.1.5.2 if  $BIT_t^{DCA}$  includes one or more *resources* in a *dynamic constrained area*,  $d$ , each *resource*  $b \in BCT_t^{DCA}$  for *dynamic constrained area*,  $d$ , shall have the parameters in  $PARAM_{t,b}$  replaced with its *reference level values*.
- 14.6.1.6 If a *non-quick-start resource* in a *narrow constrained area* or a *dynamic constrained area* has failed a Price Impact Test, each *non-quick-start resource* in the *narrow constrained area* or *dynamic constrained area* that also failed the corresponding Conduct Test shall have its commitment cost parameters replaced with its applicable *reference level value* for that time-step. For any time-steps prior, if a *non-quick-start resource* in that *narrow constrained area* or *dynamic constrained area* has a commitment cost parameter that failed the Conduct Test, that commitment cost parameter shall be replaced with the *resource's* applicable *reference level value* in those time-steps. This is expressed as:
- 14.6.1.6.1 For all time-steps up to the time-step in which a *resource* failed the Price Impact Test for a *narrow constrained area*, for all  $b \in BCT_t^{NCA}$ , if  $PARAM_{t,b}$  contains any of the *commitment cost parameters*  $SUOffer$ ,  $SNLOffer$ , or  $EnergyToMLP_k$ , replace these parameters with *reference level values*.
- 14.6.1.6.2 For all time-steps up to the time-step in which a *resource* failed the Price Impact Test for a *dynamic constrained area*, for all  $b \in BCT_t^{DCA}$ , if  $PARAM_{t,b}$  contains any of the *commitment cost parameters*  $SUOffer$ ,  $SNLOffer$ , or  $EnergyToMLP_k$ , replace these parameters with *reference level values*.
- 14.6.1.7 If a *resource* fails the local market power for *operating reserve* Price Impact Test, all *resources* in the same *operating reserve* region with a non-zero *operating reserve* minimum requirement that failed the corresponding Conduct Test for at least one parameter shall have the parameter that failed the Conduct Test replaced with the *resource's* applicable *reference level value* for that hour. This is expressed as:
- 14.6.1.7.1 For each time-step  $t \in TS$ , if  $BIT_t^{ORL}$  includes one or more *resource* in *operating reserve* region,  $r$ , all *resources*,  $b \in BIT_t^{ORL}$  for *operating reserve* region  $r$ , shall have the parameters in  $PARAMOR_{t,b}$  replaced with *reference level values*.

14.6.1.8 If a *non-quick-start resource* fails the local market power for *operating reserve* Price Impact Test in any time-step, the *commitment cost parameters* for all *non-quick-start resources* in the same *operating reserve* region with a non-zero *operating reserve* minimum requirement that failed the corresponding Conduct Test shall be replaced with the *resource's* applicable *reference level value* for that time-step. For any time-steps prior, any *commitment cost parameters* of *non-quick-start resources* that failed the Conduct Test shall be replaced with the *resource's* applicable *reference level value* in those time-steps. This is expressed as:

14.6.1.8.1 For all time-steps up to the time-step in which a *resource* failed the Price Impact Test for  $r$ , for all  $b \in BCT_t^{ORL}$ , if  $PARAM_{t,b}$  contains any of the *commitment cost parameters*  $SUOffer$ ,  $SNLOffer$ , or  $EnergyToMLP_{kr}$ , replace these parameters with *reference level values*.

## 14.7 Outputs

14.7 The *pre-dispatch calculation engine* shall prepare the following outputs, subject to section 14.7.2, for each time-step  $t \in TS$ :

14.7.1.1 The set of *resources* that failed the Price Impact Test for all time-steps in the pre-dispatch look ahead period, by condition, in accordance to sections 14.4 and 14.5. Those *resources* shall be added to the accumulated set of *resources* from previous *pre-dispatch calculation engine* runs which failed the Price Impact Test in the current time-step  $t \in TS$ ;

14.7.1.2 The *locational marginal prices* for *energy* and *operating reserve* that failed the Price Impact Test for each *resource* at bus  $b$  in accordance to sections 14.4 and 14.5;

14.7.1.3 A revised set of *offer* data to be used by the next *pre-dispatch calculation engine* run and next real-time hour. The revised set of offer data will be for the *resources* that failed the Price Impact Test:

14.7.1.3.1 in current *pre-dispatch calculation engine* run replacing *offer* data that failed the Conduct Test with the applicable *reference level values*, in accordance with section 14.6; and

14.7.1.3.2 in previous *pre-dispatch calculation engine* runs with *financial dispatch data parameters* that were decided

to be mitigated in previous *pre-dispatch calculation engine* runs replaced with *reference level values*.

- 14.7.2 The *pre-dispatch calculation engine* shall not replace *financial dispatch data parameters* from a *resource* with that *resource's* applicable *reference level value* if the *financial dispatch data parameters* is less than the *reference level value*.

## 15 Pseudo-Unit Modelling

### 15.1 Pseudo-Unit Model Parameters

- 15.1.1 The *pre-dispatch calculation engine* shall use the following registration and daily *dispatch data* to determine the underlying relationship between a *pseudo-unit* and the associated physical *resources* for a *combined cycle plant* with  $K$  combustion turbine *resources* and one steam turbine *resource*:
- 15.1.1.1  $CMCR_k$  designates the registered *maximum continuous rating* of combustion turbine *resource*  $k \in \{1, \dots, K\}$  in MW;
  - 15.1.1.2  $CMLP_k$  designates the *minimum loading point* of combustion turbine *resource*  $k \in \{1, \dots, K\}$  in MW;
  - 15.1.1.3  $SMCR$  designates the registered *maximum continuous rating* of the steam turbine *resource* in MW;
  - 15.1.1.4  $SMLP$  designates the *minimum loading point* of the steam turbine *resource* in MW for a 1x1 configuration;
  - 15.1.1.5  $SDF$  designates the amount of duct firing capacity available on the steam turbine *resource* in MW;
  - 15.1.1.6  $STPortion_k$  designates the percentage of the steam turbine *resource* capacity attributed to *pseudo-unit*  $k \in \{1, \dots, K\}$ ; and
  - 15.1.1.7  $CSCM_k \in \{0, 1\}$  designates whether *pseudo-unit*  $k \in \{1, \dots, K\}$  is flagged to operate in *single cycle mode*, subject to section 15.5.
- 15.1.2 The *pre-dispatch calculation engine* shall calculate the following model parameters for each *pseudo-unit*  $k \in \{1, \dots, K\}$ :
- 15.1.2.1  $MMCR_k$  designates the maximum continuous rating of *pseudo-unit*  $k$  and is calculated as follows:

$$CMCR_k + SMCR \cdot STPortion_k \cdot (1 - CSCM_k)$$

- 15.1.2.2  $MMLP_k$  designates the *minimum loading point* of *pseudo-unit k* and is calculated as follows:

$$CMLP_k + SMLP \cdot (1 - CSCM_k)$$

- 15.1.2.3  $MDF_k$  designates the duct firing capacity of *pseudo-unit k* and is calculated as follows:

$$SDF \cdot STPortion_k \cdot (1 - CSCM_k)$$

- 15.1.2.4  $MDR_k$  designates the *dispatchable* capacity of *pseudo-unit k* and is calculated as follows:

$$MMCR_k - MMLP_k - MDF_k$$

- 15.1.3 The *pre-dispatch calculation engine* shall define three operating regions of *pseudo-unit k*  $k \in \{1, \dots, K\}$ , as follows:

- 15.1.3.1 The *minimum loading point* region shall be the capacity between 0 and  $MMLP_k$ ;

- 15.1.3.2 The *dispatchable* region shall be the capacity between  $MMLP_k$  and  $MMLP_k + MDR_k$ ;

- 15.1.3.3 The duct firing region shall be the capacity between  $MMLP_k + MDR_k$  and  $MMCR_k$ .

- 15.1.4 The *pre-dispatch calculation engine* shall calculate the associated combustion turbine *resource* and steam turbine *resource* shares for the three operating regions of *pseudo-unit k*  $k \in \{1, \dots, K\}$ , as follows:

- 15.1.4.1 For the *minimum loading point* region:

- 15.1.4.1.1 Steam turbine *resource* share:

$$STShareMLP_k = \frac{SMLP \cdot (1 - CSCM_k)}{MMLP_k},$$

- 15.1.4.1.2 Combustion turbine *resource* share:

$$CTShareMLP_k = \frac{CMLP_k}{MMLP_k}; \text{ and}$$

- 15.1.4.2 For the *dispatchable* region:

- 15.1.4.2.1 Steam turbine *resource* share:

$$STShareDR_k = \frac{(1-CSCM_k)(SMCR \cdot STPortion_k - SMLP - SDF \cdot STPortion_k)}{MDR_k};$$

and

15.1.4.2.2 Combustion turbine *resource* share:

$$CTShareDR_k = \frac{CMCR_k - CMLP_k}{MDR_k}; \text{ and}$$

15.1.4.3 For the duct firing region:

15.1.4.3.1 Steam turbine resource share shall be equal to 1; and

15.1.4.3.2 Combustion turbine *resource* share shall be equal to 0.

## 15.2 Application of Physical Resource Deratings to the Pseudo-Unit Model

15.2.1 The *pre-dispatch calculation engine* shall apply deratings submitted by *market participants* to the applicable *dispatchable* capacity and duct firing capacity parameters for a *pseudo-unit*, where:

15.2.1.1  $CTCap_{t,k}$  designates the capacity of combustion turbine *resource*  $k \in \{1, \dots, K\}$  in time-step  $t$  as determined by submitted deratings;

15.2.1.2  $STCap_t$  designates the capacity of the steam turbine *resource* in time-step  $t$  as determined by submitted deratings; and

15.2.1.3  $TotalQ_{t,k}$  designates the total quantity of *energy* for *pseudo-unit*  $k \in \{1, \dots, K\}$  in time-step  $t$ .

15.2.2 The *pre-dispatch calculation engine* shall solve for the following operating region parameters for each *pseudo-unit*  $k \in \{1, \dots, K\}$ :

15.2.2.1  $MLP_{t,k}$ , which designates the *minimum loading point* of *pseudo-unit*  $k$  in time-step  $t$ ;

15.2.2.2  $DR_{t,k}$ , which designates the *dispatchable* region capacity of *pseudo-unit*  $k$  in time-step  $t$ ; and

15.2.2.3  $DF_{t,k}$ , which designates the duct firing region capacity of *pseudo-unit*  $k$  in time-step  $t$ .

15.2.3 Pre-Processing of De-rates

15.2.3.1 The *pre-dispatch calculation engine* shall perform the following pre-processing steps to determine the available operating regions for a

*pseudo-unit* based on the combustion turbine *resource's* and steam turbine *resource's* share and the application of the *pseudo-unit* deratings. For *pseudo-unit*  $k \in \{1, \dots, K\}$  for time-step  $t \in TS$ :

15.2.3.1.1 Step 1: Calculate the amount of *offered energy* attributed to each combustion turbine *resource* ( $CTAmt_{t,k}$ ) and steam turbine *resource* portion ( $STAmt_{t,k}$ ):

If  $TotalQ_{t,k} < MMLP_k$  then:

Calculate  $CTAmt_{t,k} = 0$ ; and

Calculate  $STAmt_{t,k} = 0$ .

Otherwise:

$CTAmtMLP = MMLP_k \cdot CTShareMLP_k$ ; and

$STAmtMLP = MMLP_k \cdot STShareMLP_k$ .

If  $TotalQ_{t,k} > MMLP_k + MDR_k$ , then:

$CTAmtDR = MDR_k \cdot CTShareDR_k$ ;

$STAmtDR = MDR_k \cdot STShareDR_k$ ; and

$STAmtDF = (1 - CSCM_k) \cdot (TotalQ_{t,k} - MMLP_k - MDR_k)$ .

Otherwise:

$CTAmtDR = (TotalQ_{t,k} - MMLP_k) \cdot CTShareDR_k$ ;

$STAmtDR = (TotalQ_{t,k} - MMLP_k) \cdot STShareDR_k$ ;

$STAmtDF = 0$ ;

$CTAmt_{t,k} = CTAmtMLP + CTAmtDR$ ; and

$STAmt_{t,k} = STAmtMLP + STAmtDR + STAmtDF$ .

15.2.3.1.2 Step 2: Allocate the steam turbine *resource's* capacity to each *pseudo-unit*:

$$PRSTCap_{t,k} = \left( \frac{STAmt_{t,k}}{\sum_{w \in \{1, \dots, K\}} STAmt_{t,w}} \right) \cdot STCap_t$$

15.2.3.1.3 Step 3: Determine if the *pseudo-unit* is available:

If  $CTAmt_{t,k} < CMLP_k$ , then the *pseudo-unit* is unavailable.

If  $STAmt_{t,k} < SMLP \cdot (1 - CSCM_k)$ , then the *pseudo-unit* is unavailable.

If  $CTCap_{t,k} < CMLP_k$ , then the *pseudo-unit* is unavailable.

If  $PRSTCap_{t,k} < SMLP \cdot (1 - CSCM_k)$ , then the *pseudo-unit* is unavailable.

15.2.3.1.4 Step 4: Initialize the operating region parameters for time-step  $t \in TS$  to the model parameter values:

Set  $MLP_{t,k} = MMLP_k$ .

Set  $DR_{t,k} = MDR_k$ .

Set  $DF_{t,k} = MDF_k$ .

15.2.3.1.5 Step 5: Apply the derating on the combustion turbine *resource* to the *dispatchable* region:

Calculate  $P$  so that  $CMLP_k + P \cdot CTShareDR_k \cdot MDR_k = CTCap_{t,k}$ ; and

Set  $DR_{t,k} = \min(DR_{t,k}, P \cdot MDR_k)$ .

15.2.3.1.6 Step 6: Apply the derating on the steam turbine *resource* to the duct firing and *dispatchable* regions for *pseudo-units* not operating in *single-cycle mode*:

Calculate  $R$  so that  $SMLP + R \cdot STShareDR_k \cdot MDR_k = PRSTCap_{t,k}$ .

If  $R \leq 1$ , update  $DF_{t,k} = 0$ , and  $DR_{t,k} = \min(DR_{t,k}, R \cdot MDR_k)$ .

If  $R > 1$ , update  $DF_{t,k} = \min(DF_{t,k}, PRSTCap_{t,k} - SMLP - STShareDR_k \cdot MDR_k)$ .

## 15.2.4 Available Energy Laminations

15.2.4.1 The *pre-dispatch calculation engine* shall determine the *offer* quantity laminations that may be scheduled for *energy* and *operating reserve* in each operating region for time-step  $t \in TS$  for each *pseudo-unit*  $k \in \{1, \dots, K\}$ , subject to section 15.2.4.2, where:

15.2.4.1.1  $QMLP_{t,k}$  designates the total quantity that may be scheduled in the *minimum loading point* region;

15.2.4.1.2  $QDR_{t,k}$  designates the total quantity that may be scheduled in the *dispatchable* region; and

15.2.4.1.3  $QDF_{t,k}$  designates the total quantity that may be scheduled in the duct firing region.

15.2.4.2 The available *offered* quantity laminations shall be subject to the following conditions:

$$0 \leq QMLP_{t,k} \leq MLP_{t,k};$$

$$0 \leq QDR_{t,k} \leq DR_{t,k};$$

$$0 \leq QDF_{t,k} \leq DF_{t,k};$$

if  $QMLP_{t,k} < MLP_{t,k}$ , then the *pseudo-unit* is unavailable and  $QDR_{t,k} = QDF_{t,k} = 0$ ; and

if  $QDR_{t,k} < DR_{t,k}$ , then  $QDF_{t,k} = 0$ .

### 15.3 Convert Physical Resource Constraints to Pseudo-Unit Constraints

15.3.1 The *pre-dispatch calculation engine* shall convert physical *resource* constraints to *pseudo-unit* constraints, where:

15.3.1.1  $PSUMin_{t,k}^q$  designates the minimum limitation on *pseudo-unit*  $k$  determined by translating constraint  $q$ . When constraint  $q$  does not provide a minimum limitation on *pseudo-unit*  $k$ , then  $PSUMin_{t,k}^q$  shall be set equal to 0;

15.3.1.2  $PSUMax_{t,k}^q$  designates the maximum limitation on *pseudo-unit*  $k$  determined by translating constraint  $q$ . When constraint  $q$  does not provide a maximum limitation on *pseudo-unit*  $k$ , then  $PSUMax_{t,k}^q$  shall be set equal to  $MLP_{t,k} + DR_{t,k} + DF_{t,k}$ ;

15.3.1.3  $CTCmt_{t,k} \in \{0,1\}$  designates whether combustion turbine *resource*  $k \in \{1,..K\}$  is considered committed in time-step  $t \in TS$ .

15.3.2 The *pre-dispatch calculation engine* shall calculate the minimum and maximum limitations, subject to section 15.3.3.1, as follows:

15.3.2.1 Minimum limitation:  $MinDG_{t,k} = \max_{q \in \{1,..Q\}} PSUMin_{t,k}^q$

15.3.2.2 Maximum limitation:  $MaxDG_{t,k} = \min_{q \in \{1,..Q\}} PSUMax_{t,k}^q$



where Q designates the number of constraints impacting a *combined cycle plant* that have been provided to the *pre-dispatch calculation engine*.

### 15.3.3 Pseudo-Unit Minimum and Maximum Constraints

15.3.3.1 *Pseudo-unit* minimum and maximum constraints shall be calculated as follows:

15.3.3.1.1  $PSUMin_{t,k} = PMin$ , where  $PMin$  shall be a minimum constraint provided on *pseudo-unit*  $k \in \{1,..,K\}$  for time-step  $t \in TS$ ; and

15.3.3.1.2  $PSUMax_{t,k} = PMax$ ,  $PMax$  shall be a maximum constraint provided on *pseudo-unit*  $k \in \{1,..,K\}$  for time-step  $t \in TS$ .

### 15.3.4 Combustion Turbine Resource Minimum and Maximum Constraints

15.3.4.1 If the *pseudo-unit* is not flagged to operate in *single cycle mode*, then the combustion turbine *resource's* minimum constraint shall be converted to a *pseudo-unit* constraint as follows:

If  $CTMin < MLP_{t,k} \cdot CTShareMLP_k$ , then set

$STMinMLP = CTMin \cdot \left( \frac{STShareMLP_k}{CTShareMLP_k} \right)$ ; and

$STMinDR = 0$ .

Otherwise, if  $CTMin \geq MLP_{t,k} \cdot CTShareMLP_k$ , then set

$STMinMLP = MLP_{t,k} \cdot STShareMLP_k$ ; and

$STMinDR = (CTMin - MLP_{t,k} \cdot CTShareMLP_k) \cdot \left( \frac{STShareDR_k}{CTShareDR_k} \right)$ .

Therefore:

$PSUMin_{t,k} = CTMin + STMinMLP + STMinDR$ .

15.3.4.2 If a *pseudo-unit* is flagged to operate in *single cycle mode*, then the combustion turbine *resource's* minimum constraint shall be converted to a *pseudo-unit* constraint as follows:

$PSUMin_{t,k} = CTMin$ .

- 15.3.4.3 If the *pseudo-unit* is not flagged to operate in *single cycle mode*, then the combustion turbine *resource's* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

If  $CTMax < MLP_{t,k} \cdot CTShareMLP_k$ , then the *pseudo-unit* is unavailable (i. e.  $PSUMax_{t,k} = 0$ ).

Otherwise, calculate the effect of the constraint on the steam turbine *resource* within the *minimum loading point* and *dispatchable* regions:

$$STMaxMLP = MLP_{t,k} \cdot STShareMLP_k$$

$$STMaxDR = (CTMax - MLP_{t,k} \cdot CTShareMLP_k) \cdot \left( \frac{STShareDR_k}{CTShareDR_k} \right)$$

$$PSUMax_{t,k} = CTMax + STMaxMLP + STMaxDR$$

- 15.3.4.4 If a *pseudo-unit* is flagged to operate in *single cycle mode*, then the combustion turbine *resource's* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

$$PSUMax_{t,k} = CTMax.$$

## 15.3.5 Steam Turbine Resource Minimum and Maximum Constraints

- 15.3.5.1 The *pre-dispatch calculation engine* shall convert a steam turbine *resource's* minimum constraint to a *pseudo-unit* constraints as follows:

- 15.3.5.1.1 Step 1: Identify  $A \subseteq \{1, \dots, K\}$ , which designates the set of *pseudo-units* to which the constraint may be allocated where *pseudo-unit*  $k \in \{1, \dots, K\}$  is placed in set  $A$  if and only if  $CSCM_k = 0$  and  $CTCmd_{t,k} = 1$ . If the set  $A$  is empty, then no further steps are required, otherwise proceed to Step 2.

- 15.3.5.1.2 Step 2: Determine the steam turbine *resource's* portion of the capacity of *pseudo-unit*  $k \in A$ :

$$STCap_k = QMLP_{t,k} \cdot STShareMLP_k + QDR_{t,k} \cdot STShareDR_k + QDF_{t,k}$$

- 15.3.5.1.3 Step 3: Allocate the  $STMin$  constraint to each *pseudo-unit*  $k \in A$ , where  $STMin$  constraint shall be allocated equally to each *pseudo-unit*  $k \in A$  and  $STPMin_k$  is limited by  $STCap_k$ .

- 15.3.5.1.4 Step 4: The steam turbine *resource* portion minimum constraint shall be converted to a *pseudo-unit* constraint, where for each *pseudo-unit*  $k \in A$ :

If  $STPMin_k < MLP_{t,k} \cdot STShareMLP_k$ , then set

$$CTMinMLP_k = STPMin_k \cdot \left( \frac{CTShareMLP_k}{STShareMLP_k} \right); \text{ and}$$

$$CTMinDR_k = 0.$$

Otherwise, if  $STPMin_k \geq MLP_{t,k} \cdot STShareMLP_k$ , then set

$$CTMinMLP_k = MLP_{t,k} \cdot CTShareMLP_k; \text{ and}$$

$$CTMinDR_k = (STPMin_k - MLP_{t,k} \cdot STShareMLP_k) \cdot \left( \frac{CTShareDR_k}{STShareDR_k} \right).$$

Therefore:

$$PSUMin_{t,k} = STPMin_k + CTMinMLP_k + CTMinDR_k.$$

- 15.3.5.2 If *pseudo-units* with sufficient steam turbine *resource* capacity are not committed, then the *pre-dispatch calculation engine* shall not convert the entire quantity of the steam turbine *resource's* minimum constraint to *pseudo-unit* constraints.

- 15.3.5.3 The steam turbine *resource's* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

$$PRSTMax_{t,k} = \left( \frac{STAmt_{t,k}}{\sum_{w \in \{1, \dots, K\}} STAmt_{t,w}} \right) \cdot STMax.$$

- 15.3.5.3.1 If the converted steam turbine *resource* maximum constraint limits the steam turbine *resource* portion to below its *minimum loading point*, then

$$PSUMax_{t,k} = 0.$$

- 15.3.5.3.2 Otherwise, calculate R so that  $SMLP + R \cdot STShareDR_k \cdot MDR_k = PRSTMax_{t,k}$ :

If  $R \leq 1$ , set  $PSUMax_{t,k} = MLP_{t,k} + \min(DR_{t,k}, R \cdot MDR_k)$ .

If  $R > 1$ , set  $PSUMax_{t,k} = MLP_{t,k} + DR_{t,k} + PRSTMax_{t,k} - SMLP - STShareDR_k \cdot MDR_k$ .

- 15.3.5.4 If the steam turbine *resource's* minimum and maximum constraints are equal but do not convert to equal *pseudo-unit* minimum and maximum constraints, then the steam turbine *resource* minimum constraint conversion in section 15.3.5.1 shall be used to determine equal *pseudo-unit* minimum and maximum constraints.

## 15.4 Steam Turbine Resource Forced Outages

- 15.4.1 If the steam turbine *resource* experiences a *forced outage*, the *pre-dispatch calculation engine* shall evaluate the corresponding *pseudo-units* as *resources* being offered in *single cycle mode*.

## 15.5 Single-Cycle Mode Flag Across Two Dispatch Days

- 15.5.1 If the pre-dispatch look-ahead period spans two *dispatch days* and the *single cycle mode* flag across the two *dispatch days* differs, then the *pre-dispatch calculation engine* shall apply the following:
- 15.5.1.1 If there are no future minimum constraints for the *pseudo-unit* before the end of the first *dispatch day* and if the *IESO's energy* management system indicates that the combustion turbine *resource* associated with the *pseudo-unit* is not online, then the *pre-dispatch calculation engine* shall use the *single cycle mode* flag of the second *dispatch day* for the entire pre-dispatch look-ahead period.
  - 15.5.1.2 If there are no minimum *reliability* or commitment constraints on the *pseudo-unit* which cross into the next *dispatch day* and either there is a future minimum *reliability* or commitment constraint on the *pseudo-unit* that ends before the end of the first *dispatch day* or if the *IESO's energy* management system indicates that the combustion turbine *resource* associated with the *pseudo-unit* is online, then the *pre-dispatch calculation engine* shall:
    - 15.5.1.2.1 use the *single cycle mode* flag of the first *dispatch day* for the pre-dispatch look-ahead period in the first *dispatch day* and use the *single cycle mode* flag of the second *dispatch day* for the pre-dispatch look-ahead period in the second *dispatch day*; and
    - 15.5.1.2.2 schedule the *pseudo-unit* to 0 MW in the first hour of the second *dispatch day*.

- 15.5.1.3 If there is a minimum *reliability* or commitment constraint on the *pseudo-unit* that crosses into the next *dispatch day*, then the *pre-dispatch calculation engine* shall:
- 15.5.1.3.1 use the *single cycle mode* flag of the first *dispatch day* for the pre-dispatch look-ahead period in the first *dispatch day* and the beginning hours of the second *dispatch day* to meet such constraint;
  - 15.5.1.3.2 use the *single cycle mode* flag of the second *dispatch day* for pre-dispatch look-ahead period in the second *dispatch day* after such constraint for the *pseudo-unit* has completed; and
  - 15.5.1.3.3 schedule the *pseudo-unit* to 0 MW in the first hour for which no *reliability* or commitment constraint applies in the second *dispatch day*.

## 15.6 Conversion of Pseudo-Unit Schedules to Physical Resource Schedules

- 15.6.1 For a *combined cycle plant* with  $K$  combustion turbine *resources* and one steam turbine *resource*, the *pre-dispatch calculation engine* shall compute the following *energy* and *operating reserve* schedules for time-step  $t \in TS$ :
- 15.6.1.1  $CTE_{t,k}$ , which designates the *energy* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
  - 15.6.1.2  $STPE_{t,k}$ , which designates the *energy* schedule for the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
  - 15.6.1.3  $STE_t$ , which designates the *energy* schedule for the steam turbine *resource*;
  - 15.6.1.4  $CT10S_{t,k}$ , which designates the synchronized *ten-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
  - 15.6.1.5  $STP10S_{t,k}$ , which designates the synchronized *ten-minute operating reserve* schedule for the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
  - 15.6.1.6  $ST10S_t$ , which designates the synchronized *ten-minute operating reserve* schedule for the steam turbine *resource*;

- 15.6.1.7  $CT10N_{t,k}$ , which designates the non-synchronized *ten-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1,...,K\}$ ;
  - 15.6.1.8  $STP10N_{t,k}$ , which designates the non-synchronized *ten-minute operating reserve* schedule for the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1,...,K\}$ ;
  - 15.6.1.9  $ST10N_t$ , which designates the non-synchronized *ten-minute operating reserve* schedule for the steam turbine *resource*;
  - 15.6.1.10  $CT30R_{t,k}$ , which designates the *thirty-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1,...,K\}$ ;
  - 15.6.1.11  $STP30R_{t,k}$ , which designates the *thirty-minute operating reserve* schedule for the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1,...,K\}$ ; and
  - 15.6.1.12  $ST30R_t$ , which designates the *thirty-minute operating reserve* schedule for the steam turbine *resource*.
- 15.6.2 The *pre-dispatch calculation engine* shall determine the following *energy* and *operating reserve* schedules for *pseudo-unit*  $k \in \{1,...,K\}$  in time-step  $t \in TS$ :
- 15.6.2.1  $SE_{t,k}$ , which designates the total amount of *energy* scheduled and  $SE_{t,k} = SEMLP_{t,k} + SEDR_{t,k} + SEDF_{t,k}$  where:
    - 15.6.2.1.1  $SEMLP_{t,k}$  designates the portion of the schedule corresponding to the *minimum loading point* region, where  $0 \leq SEMLP_{t,k} \leq QMLP_{t,k}$ ;
    - 15.6.2.1.2  $SEDR_{t,k}$  designates the portion of the schedule corresponding to the *dispatchable* region, where  $0 \leq SEDR_{t,k} \leq QDR_{t,k}$  and  $SEDR_{t,k} > 0$  only if  $SEMLP_{t,k} = QMLP_{t,k}$ ;
    - 15.6.2.1.3  $SEDF_{t,k}$  designates the portion of the schedule corresponding to the *duct firing* region, where  $0 \leq SEDF_{t,k} \leq QDF_{t,k}$  and  $SEDF_{t,k} > 0$  only if  $SEDR_{t,k} = QDR_{t,k}$ ;
  - 15.6.2.2  $S10S_{t,k}$ , which designates the total amount of synchronized *ten-minute operating reserve* scheduled;

15.6.2.3  $S10N_{t,k}$ , which designates the total amount of non-synchronized *ten-minute operating reserve* scheduled. If the *pseudo-unit* cannot provide *operating reserve* from its duct firing region, then  $0 \leq SE_{t,k} + S10S_{t,k} + S10N_{t,k} \leq QMLP_{t,k} + QDR_{t,k}$ ; and

15.6.2.4  $S30R_{t,k}$ , which designates the total amount of *thirty-minute operating reserve* scheduled, where  $0 \leq SE_{t,k} + S10S_{t,k} + S10N_{t,k} + S30R_{t,k} \leq QMLP_{t,k} + QDR_{t,k} + QDF_{t,k}$

15.6.3 The *pre-dispatch calculation engine* shall convert *pseudo-unit* schedules to physical generation *resource* schedules for *energy* and *operating reserve*, as follows:

15.6.3.1 If  $SE_{h,k} \geq MLP_{h,k}$ , then:

$$CTE_{t,k} = SEMLP_{t,k} \cdot CTShareMLP_k + SEDR_{h,k} \cdot CTShareDR_k;$$

$$STPE_{t,k} = SEMLP_{t,k} \cdot STShareMLP_k + SEDR_{t,k} \cdot STShareDR_k + SEDF_{t,k};$$

$$RoomDR_{t,k} = QDR_{t,k} - SEDR_{t,k};$$

$$10SDR_{t,k} = \min(RoomDR_{t,k}, S10S_{t,k});$$

$$10NDR_{t,k} = \min(RoomDR_{t,k} - 10SDR_{t,k}, S10N_{t,k});$$

$$30RDR_{t,k} = \min(RoomDR_{t,k} - 10SDR_{t,k} - 10NDR_{t,k}, S30R_{t,k});$$

$$CT10S_{t,k} = 10SDR_{t,k} \cdot CTShareDR_k;$$

$$STP10S_{t,k} = 10SDR_{t,k} \cdot STShareDR_k + (S10S_{t,k} - 10SDR_{t,k});$$

$$CT10N_{t,k} = 10NDR_{t,k} \cdot CTShareDR_k;$$

$$STP10N_{t,k} = 10NDR_{t,k} \cdot STShareDR_k + (S10N_{t,k} - 10NDR_{t,k});$$

$$CT30R_{t,k} = 30RDR_{t,k} \cdot CTShareDR_k; \text{ and}$$

$$STP30R_{t,k} = 30RDR_{t,k} \cdot STShareDR_k + (S30R_{t,k} - 30RDR_{t,k})$$

15.6.3.2 If  $SE_{t,k} < MLP_{t,k}$  and is ramping to *minimum loading point*, then the conversion shall be determined by the *ramp up energy to minimum loading point*.

15.6.3.3 The steam turbine *resources* portion schedules from section 15.6.3.1 shall be summed to obtain the steam turbine *resource* schedule as follows:

$$STE_t = \sum_{k=1, \dots, K} STPE_{t,k};$$

$$ST10S_t = \sum_{k=1,\dots,K} STP10S_{t,k};$$

$$ST10N_t = \sum_{k=1,\dots,K} STP10N_{t,k}; \text{ and}$$

$$ST30R_t = \sum_{k=1,\dots,K} STP30R_{t,k}.$$

## 16 Pricing Formulas

### 16.1 Purpose

- 16.1.1 The *pre-dispatch calculation engine* shall calculate *locational marginal prices* using shadow prices, constraint sensitivities and marginal loss factors.

### 16.2 Sets, Indices and Parameters

- 16.2.1 The sets, indices and parameters used to calculate *locational marginal prices* are described in section 4. In addition, the following shadow prices from Pass 1 shall be used:

- 16.2.1.1  $SPEmT_{t,c,f}^1$ , which designates the Pass 1 shadow price for the post-contingency transmission constraint for *facility*  $f \in F$  in contingency  $c \in C$  in time-step  $t$ ;
- 16.2.1.2  $SPExtT_{t,z}^1$ , which designates the Pass 1 shadow price for the import or export limit constraint  $z \in Z_{Sch}$  in time-step  $t$ ;
- 16.2.1.3  $SPL_t^1$ , which designates the Pass 1 shadow price for the *energy* balance constraint in time-step  $t$ ;
- 16.2.1.4  $SPNIUExtBwdT_t^1$ , which designates the Pass 1 shadow price for the net interchange scheduling limit constraint limiting increases in net imports between time-step  $(t-1)$  and time-step  $t$ ;
- 16.2.1.5  $SPNIDExtBwdT_t^1$ , which designates the Pass 1 shadow price for the net interchange scheduling limit constraint limiting decreases in net imports between time-step  $(t-1)$  and time-step  $t$ ;
- 16.2.1.6  $SPNIUExtFwdT_t^1$ , which designates the Pass 1 shadow price for the net interchange scheduling limit constraint limiting increases in net imports between time-step  $t$  and time-step  $(t+1)$ ;



- 16.2.1.7  $SPNIDExtFwdT_t^1$ , which designates the Pass 1 shadow price for the net interchange scheduling limit constraint limiting decreases in net imports between time-step  $t$  and time-step  $(t + 1)$ ;
- 16.2.1.8  $SPNormT_{t,f}^1$ , which designates the Pass 1 shadow price for the pre-contingency transmission constraint for *facility*  $f \in F$  in time-step  $t$ ;
- 16.2.1.9  $SP10S_t^1$ , which designates the Pass 1 shadow price for the total synchronized *ten-minute operating reserve* requirement constraint in time-step  $t$ ;
- 16.2.1.10  $SP10R_t^1$ , which designates the Pass 1 shadow price for the total *ten-minute operating reserve* requirement constraint in time-step  $t$ ;
- 16.2.1.11  $SP30R_t^1$ , which designates the Pass 1 shadow price for the total *thirty-minute operating reserve* requirement constraint in time-step  $t$ ;
- 16.2.1.12  $SPREGMin10R_{r,t}^1$ , which designates the Pass 1 shadow price for the minimum *ten-minute operating reserve* constraint for region  $r \in ORREG$  in time-step  $t$ ;
- 16.2.1.13  $SPREGMin30R_{r,t}^1$ , which designates the Pass 1 shadow price for the minimum *thirty-minute operating reserve* constraint for region  $r \in ORREG$  in time-step  $t$ ;
- 16.2.1.14  $SPREGMax10R_{r,t}^1$ , which designates the Pass 1 shadow price for the maximum *ten-minute operating reserve* constraint for region  $r \in ORREG$  in time-step  $t$ ; and
- 16.2.1.15  $SPREGMax30R_{r,t}^1$ , which designates the Pass 1 shadow price for the maximum *thirty-minute operating reserve* constraint for region  $r \in ORREG$  in time-step  $t$ .

## 16.3 Locational Marginal Prices for Energy

### 16.3.1 Energy Locational Marginal Prices for Delivery Points

- 16.3.1.1 The *pre-dispatch calculation engine* shall calculate a *locational marginal price* and components for *energy* for Pass 1 and each time-step  $t \in TS$  for every bus  $b \in L$  where a *non-dispatchable generation resource* or *dispatchable generation resource*, a *dispatchable load*, an

hourly demand response resource, or a non-dispatchable load is sited and:

- 16.3.1.1.1  $LMP_{t,b}^1$  designates the Pass 1 time-step  $t$  locational marginal price for energy;
- 16.3.1.1.2  $PRef_t^1$  designates the Pass 1 time-step  $t$  locational marginal price for energy at the reference bus;
- 16.3.1.1.3  $PLoss_{t,b}^1$  designates the Pass 1 time-step  $t$  loss component; and
- 16.3.1.1.4  $PCong_{t,b}^1$  designates the Pass 1 time-step  $t$  congestion component.

- 16.3.1.2 The pre-dispatch calculation engine shall calculate an initial locational marginal price for energy, a locational marginal price for energy at the reference bus, a loss component and a congestion component for Pass 1 at bus  $b \in L$  in time-step  $t \in TS$ , as follows:

$$InitLMP_{t,b}^1 = InitPRef_t^1 + InitPLoss_{t,b}^1 + InitPCong_{t,b}^1$$

where:

$$InitPRef_t^1 = SPL_t^1;$$

$$InitPLoss_{t,b}^1 = MglLoss_{t,b}^1 \cdot SPL_t^1;$$

and

$$InitPCong_{t,b}^1 = \sum_{f \in F_t} PreConSF_{t,f,b} \cdot SPNormT_{t,f}^1 + \sum_{c \in C} \sum_{f \in F_{t,c}} SF_{t,c,f,b} \cdot SPEmT_{t,c,f}^1.$$

- 16.3.1.3 If the initial locational marginal price for energy at the reference bus ( $InitPRef_t^1$ ) is not within the settlement bounds ( $EngyPrcFlr$ ,  $EngyPrcCeil$ ), then the pre-dispatch calculation engine shall modify the locational marginal price for energy at the reference bus as follows:

$$\text{If } InitPRef_t^1 > EngyPrcCeil, \text{ set } PRef_t^1 = EngyPrcCeil$$

$$\text{If } InitPRef_t^1 < EngyPrcFlr, \text{ set } PRef_t^1 = EngyPrcFlr$$

$$\text{Otherwise, set } PRef_t^1 = InitPRef_t^1$$

- 16.3.1.4 If the initial locational marginal price for energy ( $InitLMP_{t,b}^1$ ) is not within the settlement bounds ( $EngyPrcFlr$ ,  $EngyPrcCeil$ ), then the pre-

*dispatch calculation engine* shall modify the *locational marginal price* for *energy* as follows:

If  $InitLMP_{t,b}^1 > EngyPrcCeil$ , set  $LMP_{t,b}^1 = EngyPrcCeil$

If  $InitLMP_{t,b}^1 < EngyPrcFlr$ , set  $LMP_{t,b}^1 = EngyPrcFlr$

Otherwise, set  $LMP_{t,b}^1 = InitLMP_{t,b}^1$

- 16.3.1.5 The *pre-dispatch calculation engine* shall modify the loss component as follows:

If  $PRef_t^1 \neq InitPRef_t^1$ , set  $PLoss_{t,b}^1 = MglLoss_{t,b}^1 \cdot PRef_t^1$

Otherwise, set  $PLoss_{t,b}^1 = InitPLoss_{t,b}^1$

- 16.3.1.6 The *pre-dispatch calculation engine* shall modify the congestion component as follows:

If  $LMP_{t,b}^1 - PRef_t^1 - PLoss_{t,b}^1$  and  $InitPCong_{t,b}^1$  have the same mathematical sign, then set  $PCong_{t,b}^1 = LMP_{t,b}^1 - PRef_t^1 - PLoss_{t,b}^1$

Otherwise, set  $PCong_{t,b}^1 = 0$  and set  $PLoss_{t,b}^1 = LMP_{t,b}^1 - PRef_t^1$

## 16.3.2 Energy Locational Marginal Prices for Intertie Metering Points

- 16.3.2.1 The *pre-dispatch calculation engine* shall calculate a *locational marginal price* and components for *energy* for Pass 1 and each time-step  $t \in TS$  for *intertie zone* bus  $d \in D$ , where:

16.3.2.1.1  $ExtLMP_{t,d}^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for *energy*;

16.3.2.1.2  $IntLMP_{t,d}^1$  designates the Pass 1 time-step  $t$  *intertie border price* for *energy*;

16.3.2.1.3  $ICP_{t,d}^1$  designates the Pass 1 time-step  $t$  *intertie congestion price*;

16.3.2.1.4  $PRef_t^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for *energy* at the *reference bus*;

16.3.2.1.5  $PLoss_{t,d}^1$  designates the Pass 1 time-step  $t$  loss component;

16.3.2.1.6  $PIntCong_{t,d}^1$  designates the Pass 1 time-step  $t$  internal congestion component for *energy*;

- 16.3.2.1.7  $PExtCong_{t,d}^1$  designates the Pass 1 time-step  $t$  external congestion component for the *intertie congestion price*; and
- 16.3.2.1.8  $PNISL_{t,d}^1$  designates the Pass 1 time-step  $t$  net interchange scheduling limit congestion component for the *intertie congestion price*.

16.3.2.2 The *pre-dispatch calculation engine* shall calculate an initial *locational marginal price for energy*, a *locational marginal price for energy* for the *reference bus*, a loss components and a congestion components for *energy* for Pass 1 at *intertie zone* bus  $d \in D_a$  in *intertie zone*  $a \in A$  in time-step  $t$ , subject to sections 16.3.2.8 and 16.3.2.9, as follows:

$$InitExtLMP_{t,d}^1 = InitIntLMP_{t,d}^1 + InitICP_{t,d}^1$$

where:

$$InitPRef_t^1 = SPL_t^1;$$

$$InitPLoss_{t,d}^1 = MglLoss_{t,d}^1 \cdot SPL_t^1;$$

$$InitPIntCong_{t,d}^1$$

$$\triangle = \sum_{f \in F_t} PreConSF_{t,f,d} \cdot$$

$$SPNormT_{t,f}^1 + \sum_{c \in C} \sum_{f \in F_{t,c}} SF_{t,c,f,d} \cdot SPEmT_{t,c,f}^1;$$

$$InitIntLMP_{t,d}^1 = InitPRef_t^1 + InitPLoss_{t,d}^1 + InitPIntCong_{t,d}^1;$$

$$InitPExtCong_{t,d}^1 = \sum_{z \in Z_{sch}} EnCoeff_{a,z} \cdot SPEmT_{t,z}^1;$$

and

$$InitPNISL_{t,d}^1 = SPNIUExtBwdT_t^1 - SPNIUExtFwdT_t^1 - SPNIDExtBwdT_t^1 + SPNIDExtFwdT_t^1;$$

$$InitICP_{t,d}^1 = InitPExtCong_{t,d}^1 + InitPNISL_{t,d}^1$$

16.3.2.3 If the initial *locational marginal price for energy* ( $InitExtLMP_{t,d}^1$ ) is not within the *settlement bounds* ( $EngyPrcFlr$ ,  $EngyPrcCeil$ ), then the *pre-dispatch calculation engine* shall modify the *intertie border price for energy*, and its components, as follows:

- 16.3.2.3.1 The initial *locational marginal price* for the *reference bus* ( $InitPRef_t^1$ ) shall be modified as per section 16.3.1.3;

- 16.3.2.3.2 The initial *intertie border price* ( $InitIntLMP_{t,d}^1$ ) shall be modified as per section 16.3.1.4, where  $InitLMP_{t,b}^1 = InitIntLMP_{t,d}^1$ ;
- 16.3.2.3.3 The initial loss component ( $InitPLoss_{t,d}^1$ ) shall be modified as per section 16.3.1.5; and
- 16.3.2.3.4 The initial internal congestion component ( $InitPIntCong_{t,d}^1$ ) shall be modified as per section 16.3.1.6, where  $InitPCong_{t,b}^1 = InitPIntCong_{t,d}^1$ .
- 16.3.2.4 If the initial *locational marginal price for energy* ( $InitExtLMP_{t,d}^1$ ) is not within the *settlement bounds* ( $EngyPrcFlr$ ,  $EngyPrcCeil$ ), then the *pre-dispatch calculation engine* shall modify the *locational marginal price for energy*, as follows:
- If  $InitExtLMP_{t,d}^1 > EngyPrcCeil$ , set  $ExtLMP_{t,d}^1 = EngyPrcCeil$
- If  $InitExtLMP_{t,d}^1 < EngyPrcFlr$ , set  $ExtLMP_{t,d}^1 = EngyPrcFlr$
- Otherwise, set  $ExtLMP_{t,d}^1 = InitExtLMP_{t,d}^1$
- 16.3.2.5 If the modified *locational marginal price for energy* ( $ExtLMP_{t,d}^1$ ) is equal to the *intertie border price for energy* ( $IntLMP_{t,d}^1$ ), then the *pre-dispatch calculation engine* shall modify the external congestion component for the *intertie congestion price* and net interchange scheduling limit congestion component for the *intertie congestion price*, as follows:
- If  $ExtLMP_{t,d}^1 = IntLMP_{t,d}^1$ , set  $PExtCong_{t,d}^1 = 0$  and  $PNISL_{t,d}^1 = 0$
- 16.3.2.6 If the modified *locational marginal price for energy* ( $ExtLMP_{t,d}^1$ ) is not equal to the *intertie border price for energy* ( $IntLMP_{t,d}^1$ ), then the *pre-dispatch calculation engine* shall modify the external congestion component for the *intertie congestion price* and net interchange scheduling limit congestion component for the *intertie congestion price*, as follows:
- If  $ExtLMP_{t,d}^1 \neq IntLMP_{t,d}^1$ , set

$$PNISL_{t,d}^1 = (ExtLMP_{t,d}^1 - IntLMP_{t,d}^1) \cdot \left( \frac{InitPNISL_{h,d}^1}{InitPNISL_{t,d}^1 + InitPExtCong_{t,d}^1} \right).$$

If  $PNISL_{t,d}^1 > NISLPen$ , set  $PNISL_{t,d}^1 = NISLPen$

If  $PNISL_{t,d}^1 < (-1) \cdot NISLPen$ , set  $PNISL_{t,d}^1 = (-1) \cdot NISLPen$

Then  $PExtCong_{t,d}^1 = ExtLMP_{t,d}^1 - IntLMP_{t,d}^1 - PNISL_{t,d}^1$

- 16.3.2.7 The *pre-dispatch calculation engine* shall calculate the *intertie* congestion price as follows:

$$ICP_{t,d}^1 = PExtCong_{t,d}^1 + PNISL_{t,d}^1$$

- 16.3.2.8 The *locational marginal price* for *energy* calculated by the *pre-dispatch calculation engine* shall be the same for all *boundary entity resource* buses at the same *intertie zone*. *Intertie* transactions associated with the same *boundary entity resource* bus, but specified as occurring at different *intertie zones*, subject to phase shifter operation, shall be modelled as flowing across independent paths. Pricing of these transactions shall utilize shadow prices associated with the internal transmission constraints, *intertie* limits and transmission losses applicable to the path associated to the relevant *intertie zone*.

- 16.3.2.9 When an *intertie zone* is out-of-service, the *intertie* limits for that *intertie zone* will be set to zero and all import and export *boundary entity resources* for that *intertie zone* will receive a zero schedule and the *locational marginal price* for *energy* shall be set to the *intertie border price* for *energy*.

### 16.3.3 Zonal Prices for Energy

- 16.3.3.1 The *pre-dispatch calculation engine* shall calculate the zonal price for *energy* and its components for Pass 1 and each time-step  $t$  for each *virtual transaction zone*  $m \in M$ , as follows:

$$VZonalP_{t,m}^1 = PRef_t^1 + VZonalP_{Loss,t,m}^1 + VZonalP_{Cong,t,m}^1$$

where

$$VZonalP_{Loss,t,m}^1 = \sum_{b \in L_m^{VIRT}} WF_{t,m,b}^{VIRT} \cdot P_{Loss,t,b}^1$$

and

$$VZonalPCong_{t,m}^1 = \sum_{b \in L_m^{VIRT}} WF_{t,m,b}^{VIRT} \cdot PCong_{t,b}^1$$

- 16.3.3.2 The *pre-dispatch calculation engine* shall calculate the zonal price for *energy* and its components for Pass 1 and each time-step  $t$  for each *non-dispatchable load zone*  $y \in Y$ , as follows:

$$ZonalP_{t,y}^1 = PRef_t^1 + ZonalP_{t,y}^{Loss1} + ZonalPCong_{t,y}^1$$

where:

$$ZonalP_{t,y}^{Loss1} = \sum_{b \in L_y^{NDL}} WF_{t,y,b}^{NDL} \cdot P_{t,b}^{Loss1}$$

and

$$ZonalPCong_{t,y}^1 = \sum_{b \in L_y^{NDL}} WF_{t,y,b}^{NDL} \cdot PCong_{t,b}^1$$

- 16.3.3.3 The *Ontario zonal price* is calculated per section 16.3.3.2 where the *non-dispatchable load zone* is comprised of all *non-dispatchable loads* within Ontario.

#### 16.3.4 Pseudo-Unit Pricing

- 16.3.4.1 The *pre-dispatch calculation engine* shall calculate a *locational marginal price* and components for *energy* for Pass 1 and each time-step  $t$  for every *pseudo-unit*  $k \in \{1, \dots, K\}$ , where:

16.3.4.1.1  $CTMglLoss_{t,k}^1$  designates the marginal loss factor for the combustion turbine *resource* identified by *pseudo-unit*  $k$  for time-step  $t$  in Pass 1;

16.3.4.1.2  $STMglLoss_{t,k}^D$  designates the marginal loss factor for the steam turbine *resource* identified by *pseudo-unit*  $k$  for time-step  $t$  in Pass 1;

16.3.4.1.3  $CTPreConSF_{t,f,k}$  designates the pre-contingency sensitivity factor for the combustion turbine *resource* identified by *pseudo-unit*  $k$  on *facility*  $f$  during time-step  $t$  under pre-contingency conditions;

16.3.4.1.4  $STPreConSF_{t,f,k}$  designates the pre-contingency sensitivity factor for the steam turbine *resource*

identified by *pseudo-unit k* on *facility f* during time-step *t* under pre-contingency conditions;

16.3.4.1.5  $CTSF_{t,c,f,k}$  designates the post-contingency sensitivity factor for the combustion turbine *resource* identified by *pseudo-unit k* on *facility f* during time-step *t* under post-contingency conditions for contingency *c*; and

16.3.4.1.6  $STSF_{t,c,f,k}$  designates the post-contingency sensitivity factor for the steam turbine *resource* identified by *pseudo-unit k* on *facility f* during time-step *t* under post-contingency conditions for contingency *c*.

16.3.4.2 The *pre-dispatch calculation engine* shall calculate an initial *locational marginal price for energy*, a *locational marginal price for energy* at the *reference bus*, a loss component and a congestion component for Pass 1 and each time-step *t* for every *pseudo-unit k*  $k \in \{1,..,K\}$ , as follows:

$$InitLMP_{t,k}^1 = InitPRef_t^1 + InitPLoss_{t,k}^1 + InitPCong_{t,k}^1$$

where:

$$InitPRef_t^1 = SPL_t^1;$$

$$InitPLoss_{t,k}^1 = MglLoss_{t,k}^1 \cdot SPL_t^1;$$

and

$$InitPCong_{t,k}^1 = \sum_{f \in F_t} PreConSF_{t,f,k} \cdot SPNormT_{t,f}^1 + \sum_{c \in C} \sum_{f \in F_{t,c}} SF_{t,c,f,k} \cdot SPEmT_{t,c,f}^1$$

16.3.4.3 If *pseudo-unit k*  $k \in \{1,..,K\}$  is scheduled within its *minimum loading point range* or not scheduled at all, its marginal loss and sensitivity factors shall be:

$$MglLoss_{t,k}^1 = CTShareMLP_k \cdot CTMglLoss_{t,k}^1 + STShareMLP_k \cdot STMglLoss_{t,k}^1$$

$$PreConSF_{t,f,k} = CTShareMLP_k \cdot CTPreConSF_{t,f,k} + STShareMLP_k \cdot STPreConSF_{t,f,k}$$

$$SF_{t,c,f,k} = CTShareMLP_k \cdot CTSF_{t,c,f,k} + STShareMLP_k \cdot STSF_{t,c,f,k}$$



- 16.3.4.4 If *pseudo-unit*  $k \in \{1,..,K\}$  is scheduled within its *dispatchable* region, its marginal loss and sensitivity factors shall be:

$$MglLoss_{t,k}^1 = CTShareDR_k \cdot CTMglLoss_{t,k}^1 + STShareDR_k \cdot STMglLoss_{t,k}^1$$

$$PreConSF_{t,f,k} = CTShareDR_k \cdot CTPreConSF_{t,f,k} + STShareDR_k \cdot STPreConSF_{t,f,k}$$

$$SF_{t,c,f,k} = CTShareDR_k \cdot CTSF_{t,c,f,k} + STShareDR_k \cdot STSF_{t,c,f,k}$$

- 16.3.4.5 If *pseudo-unit*  $k \in \{1,..,K\}$  is scheduled within its duct firing region, its marginal loss and sensitivity factors shall be:

$$MglLoss_{t,k}^1 = STMglLoss_{t,k}^1$$

$$PreConSF_{t,f,k} = STPreConSF_{t,f,k}$$

$$SF_{t,c,f,k} = STSF_{t,c,f,k}$$

## 16.4 Locational Marginal Prices for Operating Reserve

### 16.4.1 Operating Reserve Locational Marginal Prices for Delivery Points

- 16.4.1.1 The *pre-dispatch calculation engine* shall calculate a *locational marginal price* and components for *operating reserve* for Pass 1 and each time-step  $t$  for a *delivery point* associated with the *dispatchable generation resource* and *dispatchable load* at bus  $b \in B$ , where:

- 16.4.1.1.1  $L30RP_{t,b}^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for *thirty-minute operating reserve*;

- 16.4.1.1.2  $P30RRef_t^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for *thirty-minute operating reserve* at the *reference bus*;

- 16.4.1.1.3  $P30RCong_{t,b}^1$  designates the Pass 1 time-step  $t$  congestion component for *thirty-minute operating reserve*;

- 16.4.1.1.4  $L10NP_{t,b}^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for non-synchronized *ten-minute operating reserve*;

- 16.4.1.1.5  $P10NRef_t^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for non-synchronized *ten-minute operating reserve* at the *reference bus*;
- 16.4.1.1.6  $P10NCong_{t,b}^1$  designates the Pass 1 time-step  $t$  congestion component for non-synchronized *ten-minute operating reserve*;
- 16.4.1.1.7  $L10SP_{t,b}^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for synchronized *ten-minute operating reserve*;
- 16.4.1.1.8  $P10SRef_t^1$  designates the Pass 1 time-step  $t$  *locational marginal prices* for synchronized *ten-minute operating reserve* at the *reference bus*;
- 16.4.1.1.9  $P10SCong_{t,b}^1$  designates the Pass 1 time-step  $t$  congestion component for synchronized *ten-minute operating reserve*; and
- 16.4.1.1.10  $ORREG_b \subseteq ORREG$  as the subset of  $ORREG$  consisting of regions that include bus  $b$ .

16.4.1.2 The *pre-dispatch calculation engine* shall calculate an initial *locational marginal price*, a *locational marginal price* at the *reference bus*, and congestion components for Pass 1 for a *delivery point* associated with the *dispatchable generation resource* and *dispatchable load* at bus  $b \in B$  in time-step  $t \in TS$ , for each class of *operating reserve*, as follows:

$$InitL30RP_{t,b}^1 = InitP30RRef_t^1 + InitP30RCong_{t,b}^1$$

where

$$InitP30RRef_t^1 = SP30R_t^1$$

and

$$\begin{aligned} InitP30RCong_{t,b}^1 &= \sum_{r \in ORREG_b} SPREGMin30R_{t,r}^1 \\ &+ \sum_{r \in ORREG_b} SPREGMax30R_{t,r}^1 \end{aligned}$$

$$InitL10NP_{t,b}^1 = InitP10NRef_t^1 + InitP10NCong_{t,b}^1$$

where

$$InitP10NRef_t^1 = SP10R_t^1 + SP30R_t^1$$

and

$$\begin{aligned} InitP10NCong_{t,b}^1 &= \sum_{r \in ORREG_b} (SPREGMin10R_{r,t}^1 \\ &\quad + SPREGMin30R_{r,t}^1) \\ &\quad + \sum_{r \in ORREG_b} (SPREGMax10R_{r,t}^1 \\ &\quad + SPREGMax30R_{r,t}^1) \end{aligned}$$

$$InitL10SP_{t,b}^1 = InitP10SRef_t^1 + InitP10SCong_{t,b}^1$$

where

$$InitP10SRef_t^1 = SP10S_t^1 + SP10R_t^1 + SP30R_t^1$$

and

$$\begin{aligned} InitP10SCong_{t,b}^1 &= \sum_{r \in ORREG_b} (SPREGMin10R_{r,t}^1 \\ &\quad + SPREGMin30R_{r,t}^1) \\ &\quad + \sum_{r \in ORREG_b} (SPREGMax10R_{r,t}^1 \\ &\quad + SPREGMax30R_{r,t}^1) \end{aligned}$$

16.4.1.3 If the initial *locational marginal price* at the *reference bus* ( $InitP30RRef_t^1$ ,  $InitP10NRef_t^1$ , or  $InitP10SRef_t^1$ ) is not within the *settlement bounds* ( $ORPrCflr$ ,  $ORPrCceil$ ), then the *pre-dispatch calculation engine* shall modify the *locational marginal price* at the *reference bus* for each class of *operating reserve* as follows:

If  $InitP30RRef_t^1 > ORPrCceil$ , set  $P30RRef_t^1 = ORPrCceil$ ;

If  $InitP30RRef_t^1 < ORPrCflr$ , set  $P30RRef_t^1 = ORPrCflr$ ;

Otherwise, set  $P30RRef_t^1 = InitP30RRef_t^1$ .

If  $InitP10NRef_t^1 > ORPrCceil$ , set  $P10NRef_t^1 = ORPrCceil$

If  $InitP10NRef_t^1 < ORPrcFlr$ , set  $P10NRef_t^1 = ORPrcFlr$

Otherwise, set  $P10NRef_t^1 = InitP10NRef_t^1$

If  $InitP10SRef_t^1, ORPrcFlr > ORPrcCeil$ , set  $10SRef_t^1 = ORPrcCeil$

If  $InitP10SRef_t^1, ORPrcFlr < ORPrcFlr$ , set  $10SRef_t^1 = ORPrcFlr$

Otherwise, set  $10SRef_t^1 = InitP10SRef_t^1$

- 16.4.1.4 If the initial *locational marginal price* ( $InitL30RP_{t,b}^1$ ,  $InitL10NP_{t,b}^1$ , or  $InitL10SP_{t,b}^1$ ) is not within the *settlement* bounds ( $ORPrcFlr$ ,  $ORPrcCeil$ ), then the *pre-dispatch calculation engine* shall modify the *locational marginal price* for each class of *operating reserve* as follows:

If  $InitL30RP_{t,b}^1 > ORPrcCeil$ , set  $L30RP_{t,b}^1 = ORPrcCeil$ ;

If  $InitL30RP_{t,b}^1 < ORPrcFlr$ , set  $L30RP_{t,b}^1 = ORPrcFlr$ ;

Otherwise, set  $L30RP_{t,b}^1 = InitL30RP_{t,b}^1$ .

If  $InitL10NP_{t,b}^1 > ORPrcCeil$ , set  $L10NP_{t,b}^1 = ORPrcCeil$ ;

If  $InitL10NP_{t,b}^1 < ORPrcFlr$ , set  $L10NP_{t,b}^1 = ORPrcFlr$ ;

Otherwise, set  $L10NP_{t,b}^1 = InitL10NP_{t,b}^1$ .

If  $InitL10SP_{t,b}^1 > ORPrcCeil$ , set  $L10SP_{t,b}^1 = ORPrcCeil$ ;

If  $InitL10SP_{t,b}^1 < ORPrcFlr$ , set  $L10SP_{t,b}^1 = ORPrcFlr$ ;

Otherwise, set  $L10SP_{t,b}^1 = InitL10SP_{t,b}^1$ .

- 16.4.1.5 If the initial *locational marginal price* ( $InitL30RP_{t,b}^1$ ,  $InitL10NP_{t,b}^1$ , or  $InitL10SP_{t,b}^1$ ) is not within the *settlement* bounds ( $ORPrcFlr$ ,  $ORPrcCeil$ ), then the *pre-dispatch calculation engine* shall modify the congestion component for each class of *operating reserve* as follows:

Set  $P30RCong_{t,b}^1 = L30RP_{t,b}^1 - P30RRef_t^1$ ;

Set  $P10NCong_{t,b}^1 = L10NP_{t,b}^1 - P10NRef_t^1$ ; and

Set  $P10SCong_{t,b}^1 = L10SP_{t,b}^1 - P10SRef_t^1$ .

- 16.4.1.6 Operating Reserve Locational Marginal Prices for Intertie Metering Points

- 16.4.1.7 The *pre-dispatch calculation engine* shall calculate a *locational marginal price* and components for *operating reserve* for Pass 1 and each time-step  $t \in TS$  for *intertie zone bus*  $d \in D$ , where:
- 16.4.1.7.1  $ExtL30RP_{t,d}^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for *thirty-minute operating reserve*;
  - 16.4.1.7.2  $P30RRef_t^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for *thirty-minute operating reserve* at the *reference bus*;
  - 16.4.1.7.3  $P30RIntCong_{t,d}^1$  designates the Pass 1 time-step  $t$  internal congestion component for *thirty-minute operating reserve*;
  - 16.4.1.7.4  $P30RExtCong_{t,d}^1$  designates the Pass 1 time-step  $t$  *intertie congestion component* *thirty-minute operating reserve*;
  - 16.4.1.7.5  $ExtL10NP_{t,d}^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for non-synchronized *ten-minute operating reserve*;
  - 16.4.1.7.6  $P10NRef_t^1$  designates the Pass 1 time-step  $t$  *locational marginal price* for non-synchronized *ten-minute operating reserve* at the *reference bus*;
  - 16.4.1.7.7  $P10NIntCong_{t,d}^1$  designates the Pass 1 time-step  $t$  internal congestion component for non-synchronized *ten-minute operating reserve*;
  - 16.4.1.7.8  $P10NExtCong_{t,d}^1$  designates the Pass 1 time-step  $t$  external congestion component for non-synchronized *ten-minute operating reserve*; and
  - 16.4.1.7.9  $ORREG_d \subseteq ORREG$  as the subset of  $ORREG$  consisting of regions that include bus  $d$ .
- 16.4.1.8 The *pre-dispatch calculation engine* shall calculate initial *locational marginal price*, *locational marginal price* at the *reference bus*, internal congestion component and external congestion component for Pass 1 at *intertie zone bus*  $d \in D_a$  in *intertie zone*  $a \in A$  in time-step  $t \in TS$ ,

for each class of *operating reserve*, subject to sections 16.4.1.11 and 16.4.1.12, as follows:

$$InitExtL30RP_{t,d}^1 = InitP30RRef_t^1 + InitP30RIntCong_{t,d}^1 + InitP30RExtCong_{t,d}^1$$

where:

$$InitP30RRef_t^1 = SP30R_t^1;$$

$$InitP30RIntCong_{t,d}^1 = \sum_{r \in ORREG_d} SPREGMin30R_{t,r}^1 + \sum_{r \in ORREG_d} SPREGMax30R_{t,r}^1;$$

and

$$InitP30RExtCong_{t,d}^1 = \sum_{z \in Z_{Sch}} 0.5 \cdot (EnCoeff_{a,z} + 1) \cdot SPExtT_{t,z}^1.$$

$$InitExtL10NP_{t,d}^1 = InitP10NRef_t^1 + InitP10NIntCong_{t,d}^1 + InitP10NExtCong_{t,d}^1$$

where:

$$InitP10NRef_t^1 = SP10R_t^1 + SP30R_t^1;$$

$$InitP10NIntCong_{t,d}^1 = \sum_{r \in ORREG_d} (SPREGMin10R_{r,t}^1 + SPREGMin30R_{r,t}^1) + \sum_{r \in ORREG_d} (SPREGMax10R_{r,t}^1 + SPREGMax30R_{r,t}^1);$$

and

$$InitP10NExtCong_{t,d}^1 = \sum_{z \in Z_{Sch}} 0.5 \cdot (EnCoeff_{a,z} + 1) \cdot SPExtT_{t,z}^1$$

16.4.1.9 If the initial *locational marginal price* ( $InitExtL30RP_{t,b}^1$ ) is not within the *settlement bounds* ( $ORPrCFI, ORPrCEil$ ), then the *pre-dispatch calculation engine* shall modify the *locational marginal price*, the *locational marginal price* at the *reference bus*, and the external congestion component for *thirty-minute operating reserve* as follows:

$$IntL30R = InitP30RRef_t^1 + InitP30RIntCong_{t,d}^1;$$

If  $InitP30RRef_t^1 > ORPrCEil$ , set  $P30RRef_t^1 = ORPrCEil$ ;

If  $InitP30RRef_t^1 < ORPrCFI$ , set  $P30RRef_t^1 = ORPrCFI$ ;

Otherwise, set  $P30RRef_t^1 = InitP30RRef_t^1$ ;

Set  $P30RIntCong_{t,d}^1 = ExtL30RP_{t,b}^1 - P30RRef_t^1$ ;

If  $InitExtL30RP_{t,b}^1 > ORPrcCeil$ , set  $ExtL30RP_{t,b}^1 = ORPrcCeil$ ;

If  $InitExtL30RP_{t,b}^1 < ORPrcFlr$ , set  $ExtL30RP_{t,b}^1 = ORPrcFlr$ ;

Otherwise,  $ExtL30RP_{t,b}^1 = InitExtL30RP_{t,b}^1$ ; and

Set  $P30RExtCong_{t,d}^1 = ExtL30RP_{t,b}^1 - P30RRef_t^1 - P30RIntCong_{t,d}^1$

- 16.4.1.10 If the initial *locational marginal price* ( $InitExtL10NP_{t,b}^1$ ) is not within the *settlement bounds* ( $ORPrcFlr$ ,  $ORPrcCeil$ ), then the *pre-dispatch calculation engine* shall modify the initial *locational marginal price*, *locational marginal price* at the *reference bus*, and the external congestion component for *ten-minute operating reserve* as follows:

$IntL10N = InitP10NRef_t^1 + InitP10NIntCong_{t,d}^1$ ;

If  $InitP10NRef_t^1 > ORPrcCeil$ , set  $P10NRef_t^1 = ORPrcCeil$ ;

If  $InitP10NRef_t^1 < ORPrcFlr$ , set  $P10NRef_t^1 = ORPrcFlr$ ;

Otherwise,  $P10NRef_t^1 = InitP10NRef_t^1$ ; and

Set  $P10NIntCong_{t,d}^1 = L10NP_{t,b}^1 - P10NRef_t^1$ ;

If  $InitExtL10NP_{t,b}^1 > ORPrcCeil$ , set  $ExtL10NP_{t,b}^1 = ORPrcCeil$ ;

If  $InitExtL10NP_{t,b}^1 < ORPrcFlr$ , set  $ExtL10NP_{t,b}^1 = ORPrcFlr$ ;

Otherwise,  $ExtL30RP_{t,b}^1 = InitExtL10NP_{t,b}^1$ ; and

Set  $P10NExtCong_{t,d}^1 = ExtL10NP_{t,b}^1 - P10NRef_t^1 - P10NIntCong_{t,d}^1$

- 16.4.1.11 The *locational marginal price* calculated by the *pre-dispatch calculation engine* shall be the same for all *boundary entity resource* buses at the same *intertie zone*. Reserve imports associated with the same *boundary entity resource* bus, but specified as occurring at a different *intertie zone*, subject to phase shifter operation, shall be modelled as flowing across independent paths. Pricing of these reserve imports shall utilize shadow prices associated with *intertie* limits and regional minimum and maximum *operating reserve* requirements applicable to the path associated to the relevant *intertie zone*.

- 16.4.1.12 When an *intertie zone* is out-of-service, the *intertie* limits for that *intertie zone* will be set to zero and all *boundary entity resources* for

that *intertie zone* will receive a zero schedule for *energy* and *operating reserve* and the *intertie operating reserve* prices shall be set equal to the *locational marginal price* for the *reference bus* for that class of *operating reserve* plus the applicable shadow prices associated with regional minimum and maximum *operating reserve* requirements.

## 16.5 Pricing for Islanded Nodes

16.5.1 For *non-quick start resources* that are not connected to the *main island*, the *pre-dispatch calculation engine* may use the following reconnection logic where enabled by the *IESO* in the order set out below to calculate the *locational marginal prices* for *energy*:

16.5.1.1 Determine the connection paths over open switches that connect the *non-quick start resource* to the *main island*;

16.5.1.2 Determine the priority rating for each connection path identified based on a weighted sum of the base voltage over all open switches used by the reconnection path and the MW ratings of the newly connected branches; and

16.5.1.3 Select the reconnection path with the highest priority rating, breaking ties arbitrarily.

16.5.2 For all (i) *resources* other than those specified in section 16.5.1 not connected to the *main island*; (ii) *non-quick start resources* where a price was not able to be determined in accordance with section 16.5.1; the *pre-dispatch calculation engine* shall use the following logic in the order set out below to calculate *locational marginal prices* for *energy*, using a node-level and *facility*-level substitution list determined by the *IESO*:

16.5.2.1 Use the *locational marginal price* for *energy* at a node in the node-level substitution list where defined and enabled by the *IESO*, provided such node is connected to the *main island*;

16.5.2.2 If no such nodes are identified, use the average *locational marginal price* for *energy* of all nodes at the same voltage level within the same *facility* that are connected to the *main island*;

16.5.2.3 If no such nodes are identified, use the average *locational marginal price* for *energy* of all nodes within the same *facility* that are connected to the *main island*;



- 16.5.2.4 If no such nodes are identified, use the average *locational marginal price* for *energy* of all nodes from another *facility* that is connected to the *main island*, as determined by the *facility*-level substitution list where defined and enabled by the *IESO*; and
- 16.5.2.5 If a price is unable to be determined in accordance with sections 16.5.2.2 through 16.5.2.4, use the *locational marginal price* for *energy* for the *reference bus*.

**Note: The existing Appendix 7.6- Local Market Power has been deleted in its entirety and replaced with the new Appendix 7.6- The Real-Time Calculation Engine Process**

## **Appendix 7.6 – The Real-Time Calculation Engine Process**

### **1.1 Purpose**

- 1.1.1 This appendix describes the process used by the *real-time calculation engine* to determine schedules and prices for the *real-time market* and real-time look-ahead period.

## **2 Real-Time Calculation Engine**

### **2.1 Real-Time Look-Ahead Period**

- 2.1.1 The real-time look-ahead period is the time horizon of the multi-interval optimization that includes the *dispatch interval* and the subsequent ten five-minute intervals.

### **2.2 Real-Time Calculation Engine Pass**

- 2.2.1 The *real-time calculation engine* shall execute one pass, Pass 1, the Real-Time Scheduling and Pricing Pass in accordance with section 7, to produce *real-time schedules* and *locational marginal prices*.

## **3 Information Used by the Real-Time Calculation Engine**

- 3.1.1 The *real-time calculation engine* shall use the information in section 3A.1 of Chapter 7.

## 4 Sets, Indices and Parameters Used by the Real-Time Calculation Engine

### 4.1 Fundamental Sets and Indices

- 4.1.1  $A$  designates the set of all *intertie zones*;
- 4.1.2  $B$  designates the set of buses identifying all *dispatchable* and *non-dispatchable resources* within Ontario;
- 4.1.3  $B^{DG} \subseteq B$  designates the set of buses identifying *dispatchable generation resources*;
- 4.1.4  $B^{DL} \subseteq B$  designates the set of buses identifying *dispatchable loads*;
- 4.1.5  $B^{HDR} \subseteq B$  designates the set of buses identifying *hourly demand response resources*;
- 4.1.6  $B^{HE} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable hydroelectric generation resources*;
- 4.1.7  $B^{NDG} \subseteq B$  designates the set of buses identifying *non-dispatchable generation resources*;
- 4.1.8  $B^{NoBid} \subseteq B$  designates the set of buses identifying *dispatchable loads* with no *bid* for *energy*;
- 4.1.9  $B^{NoOffer} \subseteq B$  designates the set of buses identifying *generation resources* with no *offer* for *energy*;
- 4.1.10  $B^{NO10DF} \subseteq B^{PSU}$  designates the subset of buses identifying *pseudo-units* that cannot provide *ten-minute operating reserve* from the duct firing region;
- 4.1.11  $B^{NQS} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable non-quick start resources*;
- 4.1.12  $B^{PSU} \subseteq B^{NQS}$  designates the subset of buses identifying *pseudo-units*;
- 4.1.13  $B_r^{REG} \subseteq B$  designates the set of internal buses in *operating reserve* region  $r \in ORREG$ ;
- 4.1.14  $B_p^{ST} \subseteq B^{PSU}$  designates the subset of buses identifying *pseudo-units* with a share of steam turbine *resource*  $p \in PST$ ;

- 4.1.15  $B^{VG} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable variable generation resources*;
- 4.1.16  $C$  designates the set of contingencies that shall be considered in the *security assessment function*;
- 4.1.17  $D$  designates the set of buses outside Ontario, corresponding to imports and exports at *intertie zones*;
- 4.1.18  $D_r^{REG} \subseteq D$  designates the set of *intertie zone* buses identifying *boundary entity resources* in *operating reserve* region  $r \in ORREG$ ;
- 4.1.19  $D_a \subseteq D$  designates the set of all buses identifying *boundary entity resources* in *intertie zone*  $a \in A$ ;
- 4.1.20  $DI \subseteq D$  designates the subset of  $k$  *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers*;
- 4.1.21  $DI_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers* in *intertie zone*  $a \in A$ ;
- 4.1.22  $DX \subseteq D$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids*;
- 4.1.23  $DX_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids* in *intertie zone*  $a \in A$ ;
- 4.1.24  $F$  designates the set of *facilities* and groups of *facilities* for which transmission constraints may be identified;
- 4.1.25  $F_i \subseteq F$  designates the set of *facilities* whose pre-contingency limit was violated in interval  $i$  as determined by a preceding *security assessment function* iteration;
- 4.1.26  $F_{i,c} \subseteq F$  designates the set of *facilities* whose post-contingency limit for contingency  $c$  is violated in interval  $i$  as determined by a preceding *security assessment function* iteration;
- 4.1.27  $I = \{1, \dots, n_I\}$  designates the set of all intervals, where  $n_I$  designates the number of five-minute intervals considered within the real-time look-ahead period;
- 4.1.28  $J_{i,b}^E$  designates the set of *bid* laminations for *energy* at  $b \in B^{DL}$  for interval  $i \in I$ ;
- 4.1.29  $J_{i,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B^{DL}$  for interval  $i \in I$ ;

- 4.1.30  $f_{i,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B^{DL}$  for interval  $i \in I$ ;
- 4.1.31  $f_{i,b}^{30R}$  designates the set of *offer* laminations for *thirty-minute operating reserve* at bus  $b \in B^{DL}$  for interval  $i \in I$ ;
- 4.1.32  $K_{i,b}^{DF} \subseteq K_{i,b}^E$  designates the set of *offer* laminations for *energy* corresponding to the duct firing region of a *pseudo-unit* at bus  $b \in B^{PSU}$  in interval  $i \in I$ ;
- 4.1.33  $K_{i,b}^{DR} \subseteq K_{i,b}^E$  designates the set of *offer* laminations for *energy* corresponding to the dispatchable region of a *pseudo-unit* at bus  $b \in B^{PSU}$  in interval  $i \in I$ ;
- 4.1.34  $K_{i,b}^E$  designates the set of *offer* laminations for *energy* at  $b \in B^{NDG} \cup B^{DG}$  for interval  $i \in I$ ;
- 4.1.35  $K_{i,b}^{MLP} \subseteq K_{i,b}^E$  designates the set of *offer* laminations for *energy* corresponding to the *minimum loading point* region of a *pseudo-unit* at bus  $b \in B^{PSU}$  in interval  $i \in I$ ;
- 4.1.36  $K_{i,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B^{DG}$  for interval  $i \in I$ ;
- 4.1.37  $K_{i,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B^{DG}$  for interval  $i \in I$ ;
- 4.1.38  $K_{i,b}^{30R}$  designates the set of *offer* laminations for *thirty-minute operating reserve* at bus  $b \in B^{DG}$  for interval  $i \in I$ ;
- 4.1.39  $L$  designates the set of buses where the *locational marginal prices* represent prices for *delivery points* associated with *non-dispatchable generation resources* and *dispatchable generation resources, dispatchable loads, hourly demand response resources, price responsive loads* and *non-dispatchable loads*;
- 4.1.40  $L_m^{VIRT} \subseteq L$  designates the buses contributing to the *virtual zonal price* for *virtual transaction zone*  $m \in M$ ;
- 4.1.41  $L_y^{NDL} \subseteq L$  designates the buses contributing to the zonal price for *non-dispatchable load zone*  $y \in Y$ ;
- 4.1.42  $M$  designates the set of *virtual transaction zones*;
- 4.1.43  $PST$  designates the set of steam turbine *resources offered* as part of a *pseudo-unit*;

4.1.44  $Y$  designates the *non-dispatchable load* zones in Ontario.

## 4.2 Market Participant Data Parameters

4.2.1 With respect to a *non-dispatchable generation resource* identified by bus  $b \in B^{NDG}$ :

4.2.1.1  $FNDG_{i,b}$  designates the fixed quantity of *energy* scheduled for interval  $i \in I$ ;

4.2.1.2  $PNDG_{i,b,k}$  designates the price for the maximum incremental quantity of *energy* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^E$ ; and

4.2.1.3  $QNDG_{i,b,k}$  designates the maximum incremental quantity of *energy* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^E$ .

4.2.2 With respect to a *dispatchable generation resource* identified by bus  $b \in B^{DG}$ :

4.2.2.1  $DRRDG_{i,b,w}$  for  $w \in \{1, \dots, NumRRDG_{i,b}\}$  designates the ramp rate in MW per minute at which the *resource* can decrease the amount of *energy* it supplies in interval  $i \in I$  while operating in the range between  $RmpRngMaxDG_{i,b,w-1}$  and  $RmpRngMaxDG_{i,b,w}$ ;

4.2.2.2  $NumRRDG_{i,b}$  designates the number of ramp rates provided for interval  $i \in I$ ;

4.2.2.3  $ORRDG_b$  designates the maximum *operating reserve* ramp rate in MW per minute;

4.2.2.4  $PDG_{i,b,k}$  designates the price for the maximum incremental quantity of *energy* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^E$ ;

4.2.2.5  $P10SDG_{i,b,k}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10S}$ ;

4.2.2.6  $P10NDG_{i,b,k}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10N}$ ;

- 4.2.2.7  $P30RDG_{i,b,k}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{30R}$ ;
- 4.2.2.8  $QDG_{i,b,k}$  designates the maximum incremental quantity of *energy* above the *minimum loading point* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^E$ ;
- 4.2.2.9  $Q10SDG_{i,b,k}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10S}$ ;
- 4.2.2.10  $Q10NDG_{i,b,k}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10N}$ ;
- 4.2.2.11  $Q30RDG_{i,b,k}$  designates the maximum incremental quantity of *thirty-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{30R}$ ;
- 4.2.2.12  $RLP30R_{i,b}$  designates the *reserve loading point* for *thirty-minute operating reserve* in interval  $i \in I$ ;
- 4.2.2.13  $RLP10S_{i,b}$  designates the *reserve loading point* for synchronized *ten-minute operating reserve* in interval  $i \in I$ ;
- 4.2.2.14  $RmpRngMaxDG_{i,b,w}$  for  $w \in \{1, \dots, NumRRDG_{i,b}\}$  designates the  $w^{th}$  ramp rate break point for interval  $i \in I$ ;
- 4.2.2.15  $URRDG_{i,b,w}$  for  $w \in \{1, \dots, NumRRDG_{i,b}\}$  designates the ramp rate in MW per minute at which the *resource* can increase the amount of *energy* it supplies in interval  $i \in I$  while operating in the range between  $RmpRngMaxDG_{i,b,w-1}$  and  $RmpRngMaxDG_{i,b,w}$  where  $RmpRngMaxDG_{i,b,0}$  shall be equal to zero.
- 4.2.3 With respect to a *dispatchable non-quick start resource* identified by bus  $b \in B^{NQS}$ :
- 4.2.3.1  $MinQDG_b$  designates the *minimum loading point* indicating the minimum output at which the *resource* must be scheduled except for times when the *resource* is starting up or shutting down.

- 4.2.4 With respect to a *dispatchable* hydroelectric *generation resource* identified by bus  $b \in B^{HE}$ :
- 4.2.4.1  $(ForL_{i,b,w}, ForU_{i,b,w})$  for  $w \in \{1, \dots, NFor_{i,b}\}$  designate the lower and upper limits of the *forbidden regions* in interval  $i \in I$  and indicate that the *resource* cannot be scheduled between  $ForL_{i,b,w}$  and  $ForU_{i,b,w}$  for all  $w \in \{1, \dots, NFor_{i,b}\}$ .
- 4.2.5 With respect to a *pseudo-unit* identified by bus  $b \in B^{PSU}$ :
- 4.2.5.1  $STShareMLP_b$  designates the steam turbine *resource's* share of the *minimum loading point* region; and
- 4.2.5.2  $STShareDR_b$  designates the steam turbine *resource's* share of the *dispatchable* region.
- 4.2.6 With respect to a *generation resource* with no *offer* for *energy* identified by bus  $b \in B^{NoOffer}$ :
- 4.2.6.1  $FNOG_{i,b}$  designates the fixed quantity of *energy* scheduled for injection for interval  $i \in I$  determined by the *IESO's energy* management system.
- 4.2.7 With respect to a *dispatchable load* identified by bus  $b \in B^{DL}$ :
- 4.2.7.1  $DRRDL_{i,b,w}$  for  $w \in \{1, \dots, NumRRDL_{i,b}\}$  designates the ramp rate in MW per minute at which the *dispatchable load* can decrease its amount of *energy* consumption in interval  $i \in I$  while operating in the range between  $RmpRngMaxDL_{i,b,w-1}$  and  $RmpRngMaxDL_{i,b,w}$ ;
- 4.2.7.2  $NumRRDL_{i,b}$  designates the number of ramp rates provided for interval  $i \in I$ ;
- 4.2.7.3  $ORRDL_b$  designates the *operating reserve* ramp rate in MW per minute for reductions in load consumption;
- 4.2.7.4  $PDL_{i,b,j}$  designates the price for the maximum incremental quantity of *energy* in interval  $i \in I$  in association with *bid* lamination  $j \in J_{i,b}^E$ ;
- 4.2.7.5  $P10NDL_{i,b,j}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10N}$ ;



- 4.2.7.6  $P10SDL_{i,b,j}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10S}$ ;
- 4.2.7.7  $P30RDL_{i,b,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{30R}$ ;
- 4.2.7.8  $QDL_{i,b,j}$  designates the maximum incremental quantity of *energy* that may be scheduled in interval  $i \in I$  in association with *bid* lamination  $j \in J_{i,b}^E$ ;
- 4.2.7.9  $QDLFIRM_{i,b}$  designates the quantity of *energy* that is *bid* at the *maximum market clearing price* in interval  $i \in I$ ;
- 4.2.7.10  $Q10NDL_{i,b,j}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10N}$ ;
- 4.2.7.11  $Q10SDL_{i,b,j}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10S}$ ;
- 4.2.7.12  $Q30RDL_{i,b,j}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{30R}$ ;
- 4.2.7.13  $RmpRngMaxDL_{i,b,w}$  for  $w \in \{1, \dots, NumRRDL_{i,b}\}$  designates the  $w^{th}$  ramp rate break point for interval  $i \in I$ ;
- 4.2.7.14  $URRDL_{i,b,w}$  for  $w \in \{1, \dots, NumRRDL_{i,b}\}$  designates the ramp rate in MW per minute at which the *dispatchable load* can increase its amount of *energy* consumption in interval  $i \in I$  while operating in the range between  $RmpRngMaxDL_{i,b,w-1}$  and  $RmpRngMaxDL_{i,b,w}$  where  $RmpRngMaxDL_{i,b,0}$  shall be equal to zero.
- 4.2.8 With respect to an *hourly demand response resource* identified by bus  $b \in B^{HDR}$ :
- 4.2.8.1  $FHDR_{i,b}$  designates the fixed schedule of *energy* consumption for interval  $i \in I$  determined by the activation of the *hourly demand response resource*.

- 4.2.9 With respect to a *dispatchable load* with no *bid* for *energy* at bus  $b \in B^{NoBid}$ :
- 4.2.9.1  $FNBL_{i,b}$  designates the fixed quantity of *energy* scheduled for consumption for interval  $i \in I$  determined by the *IESO's energy* management system.
- 4.2.10 With respect to a *boundary entity resource* import at *intertie zone* bus  $d \in DI$ , where the *locational marginal price* represents the price for the *intertie metering point* and its fixed schedules are the most recent *interchange schedules*:
- 4.2.10.1  $FIGPrC_{i,d}$  designates the fixed quantity of *energy* scheduled to import for interval  $i \in I$  and used for calculating *locational marginal prices*;
- 4.2.10.2  $FIGSch_{i,d}$  designates the fixed quantity of *energy* scheduled to import for interval  $i \in I$  and used for determining schedules;
- 4.2.10.3  $F10NIGPrC_{i,d}$  designates the fixed quantity of non-synchronized *ten-minute operating reserve* scheduled for interval  $i \in I$  and used for calculating *locational market prices*;
- 4.2.10.4  $F10NIGSch_{i,d}$  designates the fixed quantity of non-synchronized *ten-minute operating reserve* scheduled for in interval  $i \in I$  and used for determining schedules;
- 4.2.10.5  $F30RIGPrC_{i,d}$  designates the fixed quantity of *thirty-minute operating reserve* scheduled for interval  $i \in I$  and used for calculating *locational marginal prices*; and
- 4.2.10.6  $F30RIGSch_{i,d}$  designates the fixed quantity of *thirty-minute operating reserve* scheduled for interval  $i \in I$  and used for determining schedules.
- 4.2.11 With respect to a *boundary entity resource* export at *intertie zone* bus  $d \in DX$ , where the *locational marginal price* represents the price for the *intertie metering point* and its fixed schedules are the most recent *interchange schedules*:
- 4.2.11.1  $FXLPrC_{i,d}$  designates the fixed quantity of *energy* scheduled to export for interval  $i \in I$  and used for calculating *locational marginal prices*;
- 4.2.11.2  $FXLSch_{i,d}$  designates the fixed quantity of *energy* scheduled to export for interval  $i \in I$  and used for determining schedules;
- 4.2.11.3  $F10NXLPrC_{i,d}$  designates the fixed quantity of non-synchronized *ten-minute operating reserve* scheduled for interval  $i \in I$  and used for calculating *locational marginal prices*;

- 4.2.11.4  $F10NXLSch_{i,d}$  designates the fixed quantity of non-synchronized *ten-minute operating reserve* scheduled for interval  $i \in I$  and used for determining schedules;
- 4.2.11.5  $F30RXLPrc_{i,d}$  designates the fixed quantity of *thirty-minute operating reserve* scheduled for interval  $i \in I$  and used for calculating *locational marginal prices*; and
- 4.2.11.6  $F30RXLSch_{i,d}$  designates the fixed quantity of *thirty-minute operating reserve* scheduled for interval  $i \in I$  and used for determining schedules.

## 4.3 IESO Data Parameters

### 4.3.1 Variable Generation Forecast

- 4.3.1.1  $FG_{i,b}$  designates the *IESO's centralized variable generation* forecast for a *variable generation resource* identified by bus  $b \in B^{VG}$  for interval  $i \in I$ .

### 4.3.2 Variable Generation Tie-Breaking

- 4.3.2.1  $NumVG_i$  designates the number of *variable generation resources* in the daily *dispatch* order for interval  $i \in I$ ; and
- 4.3.2.2  $TBM_{i,b} \in \{1, \dots, NumVG_i\}$  designates the tie-breaking modifier for the *variable generation resource* at bus  $b \in B^{VG}$  for interval  $i \in I$ .

### 4.3.3 Operating Reserve Requirements

- 4.3.3.1  $ORREG$  designates the set of regions for which regional *operating reserve* limits have been defined;
- 4.3.3.2  $REGMin10R_{i,r}$  designates the minimum requirement for total *ten-minute operating reserve* in region  $r \in ORREG$  in interval  $i \in I$ ;
- 4.3.3.3  $REGMin30R_{i,r}$  designates the minimum requirement for *thirty-minute operating reserve* in region  $r \in ORREG$  in interval  $i \in I$ ;
- 4.3.3.4  $REGMax10R_{i,r}$  designates the maximum amount of total *ten-minute operating reserve* that may be scheduled in region  $r \in ORREG$  in interval  $i \in I$ ;

- 4.3.3.5  $REGMax30R_{i,r}$  designates the maximum amount of *thirty-minute operating reserve* that may be scheduled in region  $r \in ORREG$  in interval  $i \in I$ ;
- 4.3.3.6  $TOT10S_i$  designates the synchronized *ten-minute operating reserve* requirement;
- 4.3.3.7  $TOT10R_i$  designates the total *ten-minute operating reserve* requirement; and
- 4.3.3.8  $TOT30R_i$  designates the *thirty-minute operating reserve* requirement.

#### 4.3.4 Resource Minimums and Maximums

- 4.3.4.1 Where applicable the minimum or maximum output of a *dispatchable generation resource* and minimum or maximum consumption of a *dispatchable load* may be limited due to *reliability* constraints, applicable *contracted ancillary services*, *day-ahead operational commitments*, *pre-dispatch operational commitments*, *outages*, *derates*, *operating reserve* activation, and other constraints, such that:
  - 4.3.4.1.1  $MaxDF_{i,b}$  designates the maximum output limit in interval  $i$  for the duct firing region of a *pseudo-unit* at bus  $b \in B^{PSU}$ ;
  - 4.3.4.1.2  $MaxDG_{i,b}$  designates the most restrictive maximum output limit for the *dispatchable generation resource* in interval  $i$  at bus  $b \in B^{DG}$ ;
  - 4.3.4.1.3  $MaxDL_{i,b}$  designates the most restrictive maximum consumption limit for the *dispatchable load* in interval  $i$  at bus  $b \in B^{DL}$ ;
  - 4.3.4.1.4  $MaxDR_{i,b}$  designates the maximum output limit in interval  $i$  for the *dispatchable* region of a *pseudo-unit* at bus  $b \in B^{PSU}$ ;
  - 4.3.4.1.5  $MinDG_{i,b}$  designates the most restrictive minimum output limit for the *dispatchable generation resource* in interval  $i$  at bus  $b \in B^{DG}$ ; and
  - 4.3.4.1.6  $MinDL_{i,b}$  designates the most restrictive minimum consumption limit for the *dispatchable load* in interval  $i$  at bus  $b \in B^{DL}$ .

#### 4.3.5 Control Action Adjustments for Pricing

- 4.3.5.1  $CAAdj_i$  designates the *demand* adjustment required to calculate *locational marginal prices* appropriately when voltage reduction or load shedding has been implemented.

#### 4.3.6 Constraint Violation Penalties for interval $i \in I$ :

- 4.3.6.1  $(PLdViolSch_{i,w}, QLdViolSch_{i,w})$  for  $w \in \{1, \dots, N_{LdViol_i}\}$  designate the price-quantity segments of the penalty curve for under *generation* used by the Real-Time Scheduling algorithm in section 8;
- 4.3.6.2  $(PLdViolPrc_{i,w}, QLdViolPrc_{i,w})$  for  $w \in \{1, \dots, N_{LdViol_i}\}$  designate the price-quantity segments of the penalty curve for under *generation* used by the Real-Time Pricing algorithm in section 9;
- 4.3.6.3  $(PGenViolSch_{i,w}, QGenViolSch_{i,w})$  for  $w \in \{1, \dots, N_{GenViol_i}\}$  designate the price-quantity segments of the penalty curve for over *generation* used by the Real-Time Scheduling algorithm in section 8;
- 4.3.6.4  $(PGenViolPrc_{i,w}, QGenViolPrc_{i,w})$  for  $w \in \{1, \dots, N_{GenViol_i}\}$  designate the price-quantity segments of the penalty curve for over *generation* used by the Real-Time Pricing algorithm in section 9;
- 4.3.6.5  $(P10SViolSch_{i,w}, Q10SViolSch_{i,w})$  for  $w \in \{1, \dots, N_{10SViol_i}\}$  designate the price-quantity segments of the penalty curve for the synchronized *ten-minute operating reserve* requirement used by the Real-Time Scheduling algorithm in section 8;
- 4.3.6.6  $(P10SViolPrc_{i,w}, Q10SViolPrc_{i,w})$  for  $w \in \{1, \dots, N_{10SViol_i}\}$  designate the price-quantity segments of the penalty curve for the synchronized *ten-minute operating reserve* requirement used by the Real-Time Pricing algorithm in section 9;
- 4.3.6.7  $(P10RViolSch_{i,w}, Q10RViolSch_{i,w})$  for  $w \in \{1, \dots, N_{10RViol_i}\}$  designate the price-quantity segments of the penalty curve for the total *ten-minute operating reserve* requirement used by the Real-Time Scheduling algorithm in section 8;
- 4.3.6.8  $(P10RViolPrc_{i,w}, Q10RViolPrc_{i,w})$  for  $w \in \{1, \dots, N_{10RViol_i}\}$  designate the price-quantity segments of the penalty curve for the total *ten-minute operating reserve* requirement used by the Real-Time Pricing algorithm in section 9;

- 4.3.6.9 ( $P30RViolSch_{i,w}, Q30RViolSch_{i,w}$ ) for  $w \in \{1, \dots, N_{30RViol_i}\}$  designate the price-quantity segments of the penalty curve for the total *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement used by the Real-Time Scheduling algorithm in section 8;
- 4.3.6.10 ( $P30RViolPrc_{i,w}, Q30RViolPrc_{i,w}$ ) for  $w \in \{1, \dots, N_{30RViol_i}\}$  designate the price-quantity segments of the penalty curve for the total *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement used by the Real-Time Pricing algorithm in section 9;
- 4.3.6.11 ( $PREG10RViolSch_{i,w}, QREG10RViolSch_{i,w}$ ) for  $w \in \{1, \dots, N_{REG10RViol_i}\}$  designate the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* minimum requirements used by the Real-Time Scheduling algorithm in section 8;
- 4.3.6.12 ( $PREG10RViolPrc_{i,w}, QREG10RViolPrc_{i,w}$ ) for  $w \in \{1, \dots, N_{REG10RViol_i}\}$  designate the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* minimum requirements used by the Real-Time Pricing algorithm in section 9;
- 4.3.6.13 ( $PREG30RViolSch_{i,w}, QREG30RViolSch_{i,w}$ ) for  $w \in \{1, \dots, N_{REG30RViol_i}\}$  designate the price-quantity segments of the penalty curve for area *thirty-minute operating reserve* minimum requirements used by the Real-Time Scheduling algorithm in section 8;
- 4.3.6.14 ( $PREG30RViolPrc_{i,w}, QREG30RViolPrc_{i,w}$ ) for  $w \in \{1, \dots, N_{REG30RViol_i}\}$  designate the price-quantity segments of the penalty curve for area *thirty-minute operating reserve* minimum requirements used by the Real-Time Pricing algorithm in section 9;
- 4.3.6.15 ( $PXREG10RViolSch_{i,w}, QXREG10RViolSch_{i,w}$ ) for  $w \in \{1, \dots, N_{XREG10RViol_i}\}$  designate the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* maximum restrictions used by the Real-Time Scheduling algorithm in section 8;
- 4.3.6.16 ( $PXREG10RViolPrc_{i,w}, QXREG10RViolPrc_{i,w}$ ) for  $w \in \{1, \dots, N_{XREG10RViol_i}\}$  designate the price-quantity segments of the penalty curve for area total *ten-minute operating reserve* maximum restrictions used by the Real-Time Pricing algorithm in section 9;
- 4.3.6.17 ( $PXREG30RViolSch_{i,w}, QXREG30RViolSch_{i,w}$ ) for  $w \in \{1, \dots, N_{XREG30RViol_i}\}$  designate the price-quantity segments of the penalty curve for area

total *thirty-minute operating reserve* maximum restrictions used by the Real-Time Scheduling algorithm in section 8;

4.3.6.18 ( $PXREG30RViolPrc_{i,w}$ ,  $QXREG30RViolPrc_{i,w}$ ) for  $w \in \{1, \dots, N_{XREG30RViol_i}\}$  designate the price-quantity segments of the penalty curve for area total *thirty-minute operating reserve* maximum restrictions used by the Real-Time Pricing algorithm in section 9;

4.3.6.19 ( $PPreITLViolSch_{f,i,w}$ ,  $QPreITLViolSch_{f,i,w}$ ) for  $w \in \{1, \dots, N_{PreITLViol_{f,i}}\}$  designate the price-quantity segments of the penalty curve for exceeding the pre-contingency limit of the transmission constraint for *facility*  $f \in F$  used by the Real-Time Scheduling algorithm in section 8;

4.3.6.20 ( $PPreITLViolPrc_{f,i,w}$ ,  $QPreITLViolPrc_{f,i,w}$ ) for  $w \in \{1, \dots, N_{PreITLViol_{f,i}}\}$  designate the price-quantity segments of the penalty curve for exceeding the pre-contingency limit of the transmission constraint for *facility*  $f \in F$  used by the Real-Time Pricing algorithm in section 9;

4.3.6.21 ( $PITLViolSch_{c,f,i,w}$ ,  $QITLViolSch_{c,f,i,w}$ ) for  $w \in \{1, \dots, N_{ITLViol_{c,f,i}}\}$  designate the price-quantity segments of the penalty curve for exceeding the contingency  $c \in C$  post-contingency limit of the transmission constraint for *facility*  $f \in F$  used by the Real-Time Scheduling algorithm in section 8;

4.3.6.22 ( $PITLViolPrc_{c,f,i,w}$ ,  $QITLViolPrc_{c,f,i,w}$ ) for  $w \in \{1, \dots, N_{ITLViol_{c,f,i}}\}$  designate the price-quantity segments of the penalty curve for exceeding the contingency  $c \in C$  post-contingency limit of the transmission constraint for *facility*  $f \in F$  used by the Real-Time Pricing algorithm in section 9; and

4.3.6.23 *NISLPen* designates the net interchange scheduling limit constraint violation penalty price for *locational marginal pricing*.

#### 4.3.7 Price Bounds

4.3.7.1 *EngyPrcCeil* designates and is equal to the *maximum market clearing price* for *energy*;

4.3.7.2 *EngyPrcFlr* designates and is equal to the *settlement floor price* for *energy*;

4.3.7.3 *ORPrcCeil* designates and is equal to the *maximum operating reserve price* for all classes of *operating reserve*; and

4.3.7.4  $ORPrCFlr$  designates the minimum price for all classes of *operating reserve* and is equal to \$0/MW.

#### 4.3.8 Weighting Factors for Zonal Prices

4.3.8.1  $WF_{i,m,b}^{VIRT}$  designates the weighting factor for bus  $b \in L_m^{VIRT}$  used to calculate the price for *virtual transaction zone*  $m \in M$  for interval  $i \in I$  and shall be equal to the weighting factor used in the *day-ahead market* for the applicable hour;

4.3.8.2  $WF_{i,y,b}^{NDL}$  designates the weighting factor for bus  $b \in L_y^{NDL}$  used to calculate the price for *non-dispatchable load zone*  $y \in Y$  for interval  $i \in I$  and shall be obtained by renormalizing the load distribution factors so that the sum of weighting factors for a *non-dispatchable load zone* and for a given interval is one.

### 4.4 Other Data Parameters

#### 4.4.1 Non-Dispatchable Demand Forecast

4.4.1.1  $FL_i$  designates the five-minute province-wide *non-dispatchable demand* forecast for interval  $i \in I$  calculated by the *security assessment* function.

#### 4.4.2 Internal Transmission Constraints

4.4.2.1  $PreConSF_{i,f,b}$  designates the pre-contingency sensitivity factor for bus  $b \in B \cup D$  indicating the fraction of *energy* injected at bus  $b$  which flows on *facility*  $f$  during interval  $i$  under pre-contingency conditions;

4.4.2.2  $AdjNormMaxFlow_{i,f}$  designates the limit corresponding to the maximum flow allowed on *facility*  $f$  in interval  $i$  under pre-contingency conditions;

4.4.2.3  $SF_{i,c,f,b}$  designates the post-contingency sensitivity factor for bus  $b \in B \cup D$  indicating the fraction of *energy* injected at bus  $b$  which flows on *facility*  $f$  during interval  $i$  under post-contingency conditions for contingency  $c$ ; and

4.4.2.4  $AdjEmMaxFlow_{i,c,f}$  designates the limit corresponding to the maximum flow allowed on *facility*  $f$  in interval  $i$  under post-contingency conditions for contingency  $c$ .



#### 4.4.3 Transmission Losses

4.4.3.1 *LossAdj<sub>i</sub>* designates any adjustment needed for interval  $i \in I$  to correct for any discrepancy between Ontario total system losses calculated using a base case power flow from the *security* assessment function and linearized losses that would be calculated using the marginal loss factors; and

4.4.3.2 *MglLoss<sub>i,b</sub>* designates the marginal loss factor and represents the marginal impact on transmission losses resulting from transmitting *energy* from the *reference bus* to serve an increment of additional load at *resource* bus  $b \in B \cup D$  in interval  $i \in I$ .

## 5 Initialization

### 5.1 Purpose

5.1.1 The initialization processes set out in this section shall occur prior to the execution of the *real-time calculation engine* described in section 2.2.1 above.

### 5.2 Reference Bus

5.2.1 The *IESO* shall use Richview Transformer Station as the *real-time calculation engine's* default *reference bus* for the calculation of *locational marginal prices*.

5.2.2 If the default *reference bus* is out of service, another in-service bus shall be selected.

### 5.3 Islanding Conditions

5.3.1 In the event of a network split, the *real-time calculation engine* shall:

5.3.1.1 only evaluate *resources* that are within the *main island*;

5.3.1.2 use only forecasts of *demand* forecast areas in the *main island*; and

5.3.1.3 use a bus within the *main island* in place of the *reference bus* if the *reference bus* does not fall within the *main island*.

## 5.4 Variable Generation Tie-Breaking

- 5.4.1 For each interval  $i \in I$ , each *variable generation resource* bus  $b \in B^{VG}$  and each *offer* lamination  $k \in K_{i,b}^E$ , the *offer price*  $PDG_{i,b,k}$  shall be updated to  $PDG_{i,b,k} - \left( \frac{TBM_{i,b}}{NumVG_i} \right) \rho$ , where  $\rho$  is a small nominal value of order  $10^{-4}$ .

## 5.5 Pseudo-Unit Constraints

- 5.5.1 Constraints for *pseudo-units* corresponding to the minimum and maximum constraints on physical *resources* shall be determined in accordance with section 10.

## 5.6 Initial Scheduling Assumptions

### 5.6.1 Initial Schedules

- 5.6.1.1 Initial *energy* schedules shall be based on the values determined by the *IESO's energy* management system and the schedules from the previous *real-time calculation engine* run, where:
- 5.6.1.1.1  $RTDLTel_{-1,b}$  designates the *energy* management system MW value for the *dispatchable load* at bus  $b \in B^{DL}$ ;
  - 5.6.1.1.2  $SDLSch_{0,b}^{Prev}$  designates the schedule determined for the *dispatchable load* at bus  $b \in B^{DL}$  by the Real-Time Scheduling algorithm in section 8, of the previous *real-time calculation engine* run;
  - 5.6.1.1.3  $RTDGTel_{-1,b}$  designates the *energy* management system MW value for the *dispatchable generation resource* at bus  $b \in B^{DG}$ ;
  - 5.6.1.1.4  $SDGSch_{0,b}^{Prev}$  designates the schedule determined for the *dispatchable generation resource* at bus  $b \in B^{DG}$  by the Real-Time Scheduling algorithm in section 8, of the previous *real-time calculation engine* run;
  - 5.6.1.1.5  $SDLPrC_{0,b}^{Prev}$  designates the schedule determined for the *dispatchable load* at bus  $b \in B^{DL}$  by the Real-Time Pricing algorithm in section 9, of the previous *real-time calculation engine* run; and

- 5.6.1.1.6  $SDGPr_{0,b}^{prev}$  designates the schedule determined for the *dispatchable generation resource* at bus  $b \in B^{DG}$  by the Real-Time Pricing algorithm in section 9, of the previous *real-time calculation engine* run.
- 5.6.1.2 For the *dispatchable load* at bus  $b$ , the initial schedule,  $SDLInitSch_{0,b}$ , for the Real-Time Scheduling algorithm in section 8, shall be determined as follows:
- 5.6.1.2.1 Step 1: Calculate  $TelUp_{0,b}$  using the submitted up ramp rates and break points to determine the maximum consumption level the *dispatchable load* can achieve in five minutes from  $RTDLTel_{-1,b}$ ;
- 5.6.1.2.2 Step 2: Calculate  $TelDown_{0,b}$  using the submitted down ramp rates and break points to determine the minimum consumption level the *dispatchable load* can achieve in five minutes from  $RTDLTel_{-1,b}$ ; and
- 5.6.1.2.3 Step 3: If the schedule from the previous *real-time calculation engine* run is achievable by ramping from the  $RTDLTel_{-1,b}$ , then set the initial schedule to the schedule from the previous *real-time calculation engine* run. Otherwise, set the initial schedule to the nearest boundary:
- If  $TelDown_{0,b} \leq SDLSch_{0,b}^{prev} \leq TelUp_{0,b}$ , then set  $SDLInitSch_{0,b} = SDLSch_{0,b}^{prev}$
- If  $SDLSch_{0,b}^{prev} < TelDown_{0,b}$ , then set  $SDLInitSch_{0,b} = TelDown_{0,b}$
- Otherwise, set  $SDLInitSch_{0,b} = TelUp_{0,b}$ .
- 5.6.1.3 For the *dispatchable generation resource* at bus  $b$ , the initial schedule,  $SDGInitSch_{0,b}$ , for the Real-Time Scheduling algorithm in section 8, shall be determined as follows:
- 5.6.1.3.1 Step 1: Calculate  $TelUp_{0,b}$  using the submitted up ramp rates and break points to determine the maximum production level the *resource* can achieve in five minutes from  $RTDGTel_{-1,b}$ ;

5.6.1.3.2 Step 2: Calculate  $TelDown_{0,b}$  using the submitted down ramp rates and break points to determine the minimum production level the *resource* can achieve in five minutes from  $RTDGTel_{-1,b}$ ; and

5.6.1.3.3 Step 3: If the schedule from the previous *real-time calculation engine* run is achievable by ramping from the  $RTDGTel_{-1,b}$ , then set the initial schedule to the schedule from the previous *real-time calculation engine* run. Otherwise, set the initial schedule to the nearest boundary:

If  $TelDown_{0,b} \leq SDGSch_{0,b}^{Prev} \leq TelUp_{0,b}$  then set  $SDGInitSch_{0,b} = SDGSch_{0,b}^{Prev}$   
 If  $SDGSch_{0,b}^{Prev} < TelDown_{0,b}$  then set  $SDGInitSch_{0,b} = TelDown_{0,b}$   
 Otherwise, set  $SDGInitSch_{0,b} = TelUp_{0,b}$ .

5.6.1.4 For the *dispatchable load* at bus  $b$ , the initial schedule,  $SDLInitPrc_{0,b}$ , for the Real-Time Pricing algorithm in section 9, shall be determined as follows:

If  $SDLSch_{0,b}^{Prev} \leq SDLPrC_{0,b}^{Prev} \leq SDLInitSch_{0,b}$  or  $SDLInitSch_{0,b} \leq SDLPrC_{0,b}^{Prev} \leq SDLSch_{0,b}^{Prev}$ , then set  $SDLInitPrc_{0,b} = SDLInitSch_{0,b}$ ;  
 Otherwise set  $SDLInitPrc_{0,b} = SDLPrC_{0,b}^{Prev}$ .

5.6.1.5 For the *dispatchable generation* at bus  $b$ , the initial schedule  $SDGInitPrc_{0,b}$ , for the Real-Time Pricing algorithm in section 9, designates the initial schedule for the *dispatchable generation resource* at bus  $b$  and is determined as follows:

If  $SDGSch_{0,b}^{Prev} \leq SDGPrC_{0,b}^{Prev} \leq SDGInitSch_{0,b}$  or  $SDGInitSch_{0,b} \leq SDGPrC_{0,b}^{Prev} \leq SDGSch_{0,b}^{Prev}$  then set  $SDGInitPrc_{0,b} = SDGInitSch_{0,b}$ ;  
 Otherwise set  $SDGInitPrc_{0,b} = SDGPrC_{0,b}^{Prev}$ .

5.6.2 Start-up and Shutdown for Non-Quick Start Resources

5.6.2.1 The start-up and shutdown for *non-quick start resources* at bus  $b \in B^{NQS}$  and interval  $i \in I$  shall be based on the following parameters that

are determined based on observed *resource* operation as well as confirmed start-up and shutdown times:

- 5.6.2.1.1  $AtZero_{i,b} \in \{0,1\}$ , which designates that the *resource* is scheduled to be offline;
- 5.6.2.1.2  $SU_{i,b} \in \{0,1\}$ , which designates that the *resource* must be scheduled on its start-up trajectory. This input may indicate an upcoming confirmed start-up or that the *resource* has started ramping up already;
- 5.6.2.1.3  $AtMLP_{i,b} \in \{0,1\}$ , which designates that the *resource* is scheduled to operate at or above its *minimum loading point* due to a minimum generation constraint or the *resource* shutdown has yet to be confirmed by the *IESO*;
- 5.6.2.1.4  $EvalSD_{i,b} \in \{0,1\}$ , which designates that the *resource* has been de-committed by the *pre-dispatch calculation engine*, such de-commitment has been confirmed by the *IESO*, and the *resource* can be evaluated for *energy* schedules below its *minimum loading point* but can still be scheduled at or above its *minimum loading point*; and
- 5.6.2.1.5  $SD_{i,b} \in \{0,1\}$ , which designates that the *resource* must be scheduled on its shutdown trajectory. This input may indicate an upcoming mandatory shutdown or that the *resource* has already started ramping down.

5.6.2.2 For all parameters in section 5.6.2.1:

$$AtZero_{i,b} + SU_{i,b} + AtMLP_{i,b} + EvalSD_{i,b} + SD_{i,b} = 1$$

## 6 Security Assessment Function in the Real-Time Calculation Engine

### 6.1 Interaction between the Security Assessment Function and Optimization Functions

- 6.1.1 The scheduling and pricing algorithms of the *real-time calculation engine* pass shall perform multiple iterations of the optimization functions and the *security* assessment function to check for violations of monitored thermal limits and operating *security limits* using the schedules produced by the optimization functions.
- 6.1.2 As multiple iterations are performed, the transmission constraints produced by the *security* assessment function shall be used by the optimization functions.
- 6.1.3 The *security* assessment function shall use the physical *resource* representation of *combined cycle plant* that are registered as *pseudo-units*.

### 6.2 Inputs into the Security Assessment Function

- 6.2.1 The *security* assessment function shall use the following inputs:
  - 6.2.1.1 the *IESO demand* forecasts; and
  - 6.2.1.2 applicable *IESO-controlled grid* information pursuant to section 3A.1 of Chapter 7.
- 6.2.2 The *security* assessment function shall also use the following outputs of the optimization functions:
  - 6.2.2.1 the schedules for *dispatchable loads* and *hourly demand response resources*;
  - 6.2.2.2 the schedules for *non-dispatchable generation resources* and *dispatchable generation resources*; and
  - 6.2.2.3 the schedules for *boundary entity resources* at each *intertie zone*.

#### Security Assessment Function Processing

- 6.3.1 The *security* assessment function shall determine the province-wide non-*dispatchable demand* forecast quantity,  $FL_i$ , using *demand* forecasts for *demand* forecast areas, the *IESO's energy* management system MW quantities and the

scheduled quantities from the previous *real-time calculation engine* run as follows:

- 6.3.1.1 sum the *IESO* five-minute *demand* forecasts for *demand* forecast areas;
  - 6.3.1.2 subtract the expected consumption of all physical *hourly demand response resources*;
  - 6.3.1.3 subtract the expected consumption of all virtual *hourly demand response resources*; and
  - 6.3.1.4 subtract the expected consumption of all *dispatchable loads*.
- 6.3.2 The *security* assessment function shall perform the following calculations and analyses:
- 6.3.2.1 A base case solution function shall prepare a power flow solution for each interval in the real-time look-ahead period. The base case solution function shall select the power system model state applicable to the forecast of conditions for the interval and input schedules.
  - 6.3.2.2 The base case solution function shall use an AC power flow analysis. If the AC power flow analysis fails to converge, the base case solution function shall use a non-linear DC power flow analysis. If the non-linear DC power flow analysis fails to converge, the base case solution function shall use a linear DC power flow analysis.
  - 6.3.2.3 If the AC or non-linear DC power flow analysis converges, continuous thermal limits for all monitored equipment and operating *security limits* shall be monitored to check for pre-contingency limit violations.
  - 6.3.2.4 Violated pre-contingency limits shall be linearized using pre-contingency sensitivity factors and incorporated as constraints for use by the optimization functions.
  - 6.3.2.5 If the linear DC power flow analysis is used, the pre-contingency *security* assessment may develop linear constraints to facilitate the convergence of the AC or non-linear DC power flow analysis in the subsequent iterations.
  - 6.3.2.6 A linear power flow analysis shall be used to simulate contingencies, calculate post-contingency flows and check all monitored equipment for limited-time thermal limit violations.

- 6.3.2.7 Violated post-contingency limits shall be linearized using post-contingency sensitivity factors and incorporated as constraints for use by the optimization functions.
- 6.3.2.8 The base case solution shall be used to calculate Ontario *transmission system* losses, marginal loss factors and loss adjustment for each interval. The impact of losses on branches between the *resource* bus and the *resource connection point* to the *IESO-controlled grid* and losses on branches outside Ontario shall be excluded when determining marginal loss factors.
- 6.3.2.9 The *real-time calculation engine* shall use a set of fixed marginal loss factors for each *dispatch hour*. The same set of fixed marginal loss factors shall apply to all five-minute intervals that fall in the *dispatch hour*. The set of fixed marginal loss factors for each *dispatch hour* shall be determined based on the marginal loss factors calculated in the previous hour by the Real-Time Scheduling algorithm in section 8 of the *real-time calculation engine*.
- 6.3.2.10 The marginal loss factors for the advisory intervals that fall in the hour following the *dispatch hour* shall be determined based on the fixed marginal loss factors for the *dispatch hour* described in section 6.3.2.9 and the marginal loss factors calculated by the Real-Time Scheduling algorithm in section 8 of the previous *real-time calculation engine* run.
- 6.3.2.11 The Real-Time Scheduling and Real-Time Pricing algorithms in sections 8 and 9, respectively, shall use the same set of marginal loss factors.

## 6.3 Outputs from the Security Assessment Function

- 6.4.1 The outputs of the *security* assessment function used in the optimization functions include the following:
  - 6.4.1.1 a set of linearized constraints for all violated pre-contingency and post-contingency limits for each interval. The sensitivities and limits associated with the constraints shall be those provided by the most recent *security* assessment function iteration;
  - 6.4.1.2 pre-contingency and post-contingency sensitivity factors for each interval;
  - 6.4.1.3 the marginal loss factors as described in sections 6.3.2.8 – 6.3.2.11; and



6.4.1.4 loss adjustment quantity for each interval.

## 7 Pass 1: Real-Time Scheduling and Pricing

7.1.1 Pass 1 shall use *market participant* and *IESO* inputs and *resource* and system constraints to determine a set of *resource* schedules and *locational marginal prices*. Pass 1 shall consist of the following algorithms:

- the Real-Time Scheduling algorithm described in section 8;
- the Real-Time Pricing algorithm described in section 9;

## 8 Real-Time Scheduling

### 8.1 Purpose

8.1.1 The Real-Time Scheduling algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade using *dispatch data* submitted by *registered market participants* or where applicable, the *reference level values* for *financial dispatch data parameters* mitigated in previous *pre-dispatch calculation engine* runs in accordance with Appendix 7.5A, section 14.7, to meet the *IESO's* province-wide non-*dispatchable demand* forecast and *IESO*-specified *operating reserve* requirements for each interval of the real-time look-ahead period.

### 8.2 Information, Sets, Indices and Parameters

8.2.1 Information, sets, indices and parameters used by Real-Time Scheduling algorithm are described in sections 3 and 4.

### 8.3 Variables and Objective Function

8.3.1 The Real-Time Scheduling algorithm shall solve for the following variables:

8.3.1.1  $SDL_{i,b,j}$  which designates the amount of *energy* that a *dispatchable load* scheduled at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with lamination  $j \in J_{i,b}^E$ ;

8.3.1.2  $S10SDL_{i,b,j}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with lamination  $j \in J_{i,b}^{10S}$ ;

- 8.3.1.3  $S10NDL_{i,b,j}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with lamination  $j \in J_{i,b}^{10N}$ ;
- 8.3.1.4  $S30RDL_{i,b,j}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with lamination  $j \in J_{i,b}^{30R}$ ;
- 8.3.1.5  $SNDG_{i,b,k}$  which designates the amount of *energy* that a *non-dispatchable generation resource* scheduled at bus  $b \in B^{NDG}$  in interval  $i \in I$  in association with lamination  $k \in K_{i,b}^E$ ;
- 8.3.1.6  $SDG_{i,b,k}$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with lamination  $k \in K_{i,b}^E$ ;
- 8.3.1.7  $S10SDG_{i,b,k}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with lamination  $k \in K_{i,b}^{10S}$ ;
- 8.3.1.8  $S10NDG_{i,b,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with lamination  $k \in K_{i,b}^{10N}$ ;
- 8.3.1.9  $S30RDG_{i,b,k}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with lamination  $k \in K_{i,b}^{30R}$ ;
- 8.3.1.10  $SCT_{i,b}$  which designates the schedule of the combustion turbine *resource* associated with the *pseudo-unit* at bus  $b \in B^{PSU}$  in interval  $i \in I$ ;
- 8.3.1.11  $SST_{i,p}$  which designates the schedule of steam turbine *resource*  $p \in PST$  in interval  $i \in I$ ;
- 8.3.1.12  $TB_i$  which designates any adjustment to the objective function to facilitate pro-rata tie-breaking in interval  $i \in I$ , as described in section 8.3.2.1; and

8.3.1.13  $ViolCost_i$ , which designates the cost incurred in order to avoid having the schedules violate constraints for interval  $i \in I$ , as described in section 8.3.2.3.

8.3.2 The objective function for the Real-Time Scheduling algorithm shall maximize gains from trade by maximizing the following expression:

$$\sum_{i=1..n_I} (ObjDL_i - ObjNDG_i - ObjDG_i - TB_i - ViolCost_i)$$

where:

$$ObjDL_i = \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^E} SDL_{i,b,j} \cdot PDL_{i,b,j} - \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \cdot P10SDL_{i,b,j} - \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \cdot P10NDL_{i,b,j} - \sum_{j \in J_{i,b}^{30R}} S30RDL_{i,b,j} \cdot P30RDL_{i,b,j} \right);$$

$$ObjNDG_i = \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{i,b}^E} SNDG_{i,b,k} \cdot PNDG_{i,b,k} \right);$$

and

$$ObjDG_i = \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^E} SDG_{i,b,k} \cdot PDG_{i,b,k} + \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \cdot P10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \cdot P10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k} \cdot P30RDG_{i,b,k} \right).$$

8.3.2.1 The tie-breaking term ( $TB_i$ ) shall sum a term for each *bid* or *offer* lamination. For each lamination, this term shall be the product of a small penalty cost and the quantity of the lamination scheduled. The penalty cost shall be calculated by multiplying a base penalty cost of  $TB_{Pen}$  by the amount of the lamination scheduled and then dividing by the maximum amount that could have been scheduled. That is:

$$TB_i = TBDL_i + TBNDG_i + TBDG_i$$

where:

$$TBDL_i = \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^E} \left( \frac{(SDL_{i,b,j})^2 \cdot TBPen}{QDL_{i,b,j}} \right) + \sum_{j \in J_{i,b}^{10S}} \left( \frac{(S10SDL_{i,b,j})^2 \cdot TBPen}{Q10SDL_{i,b,j}} \right) + \sum_{j \in J_{i,b}^{10N}} \left( \frac{(S10NDL_{i,b,j})^2 \cdot TBPen}{Q10NDL_{i,b,j}} \right) + \sum_{j \in J_{i,b}^{30R}} \left( \frac{(S30RDL_{i,b,j})^2 \cdot TBPen}{Q30RDL_{i,b,j}} \right) \right);$$

$$TBNDG_i = \sum_{b \in B^{NDG}} \left( \sum_{k \in K_{i,b}^E} \left( \frac{(SNDG_{i,b,k})^2 \cdot TBPen}{QNDG_{i,b,k}} \right) \right);$$

and

$$TBDG_i = \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^E} \left( \frac{(SDG_{i,b,k})^2 \cdot TBPen}{QDG_{i,b,k}} \right) + \sum_{k \in K_{i,b}^{10S}} \left( \frac{(S10SDG_{i,b,k})^2 \cdot TBPen}{Q10SDG_{i,b,k}} \right) + \sum_{k \in K_{i,b}^{10N}} \left( \frac{(S10NDG_{i,b,k})^2 \cdot TBPen}{Q10NDG_{i,b,k}} \right) + \sum_{k \in K_{i,b}^{30R}} \left( \frac{(S30RDG_{i,b,k})^2 \cdot TBPen}{Q30RDG_{i,b,k}} \right) \right).$$

8.3.2.1 *ViolCost<sub>i</sub>* shall be calculated for interval  $i \in I$  using the following variables:

8.3.2.2.1 *SLdViol<sub>i,w</sub>* which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{LdViol_i}\}$  of the penalty curve for the *energy* balance constraint allowing under-generation;

8.3.2.2.2 *SGenViol<sub>i,w</sub>* which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{GenViol_i}\}$  of the penalty curve for the *energy* balance constraint allowing over-generation;

8.3.2.2.3 *S10SViol<sub>i,w</sub>* which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{10SViol_i}\}$  of the penalty curve for the synchronized *ten-minute operating reserve* requirement;

8.3.2.2.4 *S10RViol<sub>i,w</sub>* which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{10RViol_i}\}$  of the penalty

curve for the total *ten-minute operating reserve* requirement;

- 8.3.2.2.5  $S30RViol_{i,w}$ , which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{30RViol_i}\}$  of the penalty curve for the *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement;
- 8.3.2.2.6  $SREG10RViol_{r,i,w}$ , which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{REG10RViol_i}\}$  of the penalty curve for violating the area total *ten-minute operating reserve* minimum requirement in region  $r \in ORREG$ ;
- 8.3.2.2.7  $SREG30RViol_{r,i,w}$ , which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{REG30RViol_i}\}$  of the penalty curve for violating the area *thirty-minute operating reserve* minimum requirement in region  $r \in ORREG$ ;
- 8.3.2.2.8  $SXREG10RViol_{r,i,w}$ , which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{XREG10RViol_i}\}$  of the penalty curve for violating the area total *ten-minute operating reserve* maximum restriction in region  $r \in ORREG$ ;
- 8.3.2.2.9  $SXREG30RViol_{r,i,w}$ , which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{XREG30RViol_i}\}$  of the penalty curve for violating the area *thirty-minute operating reserve* maximum restriction in region  $r \in ORREG$ ;
- 8.3.2.2.10  $SPreITLViol_{f,i,w}$ , which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{PreITLViol_{f,i}}\}$  of the penalty curve for violating the pre-contingency transmission limit for *facility*  $f \in F_i$  and
- 8.3.2.2.11  $SITLViol_{c,f,i,w}$ , which designates the violation variable affiliated with segment  $w \in \{1, \dots, N_{ITLViol_{c,f,i}}\}$  of the penalty curve for violating the post-contingency transmission limit for *facility*  $f \in F$  and contingency  $c \in C$ .

8.3.2.2  $ViolCost_i$  shall be calculated as follows:

$$\begin{aligned}
 ViolCost_i = & \sum_{w=1..N_{LdViol_i}} SLdViol_{i,w} \cdot PLdViolSch_{i,w} \\
 & - \sum_{w=1..N_{GenViol_i}} SGenViol_{i,w} \cdot PGenViolSch_{i,w} \\
 & + \sum_{w=1..N_{10SViol_i}} S10SViol_{i,w} \cdot P10SViolSch_{i,w} \\
 & + \sum_{w=1..N_{10RViol_i}} S10RViol_{i,w} \cdot P10RViolSch_{i,w} \\
 & + \sum_{w=1..N_{30RViol_i}} S30RViol_{i,w} \cdot P30RViolSch_{i,w} \\
 & + \sum_{r \in ORREG} \left( \sum_{w=1..N_{REG10RViol_i}} SREG10RViol_{r,i,w} \cdot PREG10RViolSch_{i,w} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{w=1..N_{REG30RViol_i}} SREG30RViol_{r,i,w} \cdot PREG30RViolSch_{i,w} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{w=1..N_{XREG10RViol_i}} SXREG10RViol_{r,i,w} \cdot PXREG10RViolSch_{i,w} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{w=1..N_{XREG30RViol_i}} SXREG30RViol_{r,i,w} \cdot PXREG30RViolSch_{i,w} \right) \\
 & + \sum_{f \in F_i} \left( \sum_{w=1..N_{PreITLViol_{f,i}}} SPreITLViol_{f,i,w} \cdot PPreITLViolSch_{f,i,w} \right) \\
 & + \sum_{c \in C} \sum_{f \in F_{i,c}} \left( \sum_{w=1..N_{ITLViol_{c,f,i}}} SITLViol_{c,f,i,w} \cdot PITLViolSch_{c,f,i,w} \right).
 \end{aligned}$$

## 8.4 Constraints

8.4.1 The Real-Time Scheduling algorithm optimization function shall apply the constraints described in sections 8.5 – 8.7.

## 8.5 Dispatch Data Constraints Applying to Individual Intervals

### 8.5.1 Scheduling Variable Bounds

8.5.1.1 No schedule shall be negative, nor shall any schedule exceed the quantity *offered* for *energy* and *operating reserve* respectively. Therefore:

$$\begin{aligned}
 0 \leq SDL_{i,b,j} &\leq QDL_{i,b,j} && \text{for all } b \in B^{DL}, j \in J_{i,b}^E; \\
 0 \leq S10SDL_{i,b,j} &\leq Q10SDL_{i,b,j} && \text{for all } b \in B^{DL}, j \in J_{i,b}^{10S}; \\
 0 \leq S10NDL_{i,b,j} &\leq Q10NDL_{i,b,j} && \text{for all } b \in B^{DL}, j \in J_{i,b}^{10N}; \\
 0 \leq S30RDL_{i,b,j} &\leq Q30RDL_{i,b,j} && \text{for all } b \in B^{DL}, j \in J_{i,b}^{30R}; \\
 0 \leq SNDG_{i,b,k} &\leq QNDG_{i,b,k} && \text{for all } b \in B^{NDG}, k \in K_{i,b}^E; \\
 0 \leq SDG_{i,b,k} &\leq QDG_{i,b,k} && \text{for all } b \in B^{DG}, k \in K_{i,b}^E; \\
 0 \leq S10SDG_{i,b,k} &\leq Q10SDG_{i,b,k} && \text{for all } b \in B^{DG}, k \in K_{i,b}^{10S}; \\
 0 \leq S10NDG_{i,b,k} &\leq Q10NDG_{i,b,k} && \text{for all } b \in B^{DG}, k \in K_{i,b}^{10N}; \text{ and} \\
 0 \leq S30RDG_{i,b,k} &\leq Q30RDG_{i,b,k} && \text{for all } b \in B^{DG}, k \in K_{i,b}^{30R} \\
 &&& \text{for all intervals } i \in I.
 \end{aligned}$$

8.5.1.2 A *non-quick start resource* cannot provide *energy* when it is scheduled to be offline. Therefore, for all intervals  $i \in I$ , *non-quick start resource* buses  $b \in B^{NQS}$ , and *offer* laminations  $k \in K_{i,b}^E$ :

$$0 \leq SDG_{i,b,k} \leq (1 - AtZero_{i,b}) \cdot QDG_{i,b,k}.$$

8.5.1.3 A *non-quick start resource* cannot provide *operating reserve* unless it is scheduled at or above its *minimum loading point*. Therefore, for all intervals  $i \in I$  and *non-quick start resource* buses  $b \in B^{NQS}$ :

$$\begin{aligned}
 0 \leq S10SDG_{i,b,k} &\leq (AtMLP_{i,b} + EvalSD_{i,b}) \cdot Q10SDG_{i,b,k} && \text{for all } k \in K_{i,b}^{10S}; \\
 0 \leq S10NDG_{i,b,k} &\leq (AtMLP_{i,b} + EvalSD_{i,b}) \cdot Q10NDG_{i,b,k} && \text{for all } k \in K_{i,b}^{10N}; \text{ and} \\
 0 \leq S30RDG_{i,b,k} &\leq (AtMLP_{i,b} + EvalSD_{i,b}) \cdot Q30RDG_{i,b,k} && \text{for all } k \in K_{i,b}^{30R}.
 \end{aligned}$$



## 8.5.2 Resource Initial Conditions

- 8.5.2.1 The initial schedule for a *dispatchable load* at bus  $b \in B^{DL}$  shall be fixed to the *resource* initial schedules. For all *dispatchable load* buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{0,b}^B} SDL_{0,b,j} = SDLInitSch_{0,b}$$

- 8.5.2.2 The initial schedule for a *dispatchable generation resource* at bus  $b \in B^{DG}$  shall be fixed to the *resource* initial schedules. For all *dispatchable generation resource* buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{0,b}^B} SDG_{0,b,k} = SDGInitSch_{0,b}$$

## 8.5.3 Resource Minimums and Maximums for Energy

- 8.5.3.1 A constraint shall limit schedules for *dispatchable loads* within their minimum and maximum consumption for an interval. For all intervals  $i \in I$  and all buses  $b \in B^{DL}$ :

$$MinDL_{i,b} \leq \sum_{j \in J_{i,b}^B} SDL_{i,b,j} \leq MaxDL_{i,b}.$$

- 8.5.3.2 The non-*dispatchable* portion of a *dispatchable load* shall always be scheduled. For all intervals  $i \in I$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^B} SDL_{i,b,j} \geq QDLFIRM_{i,b}.$$

- 8.5.3.3 The *non-dispatchable generation resources* shall be scheduled to the fixed quantity determined by their observed output. For all intervals  $i \in I$  and all buses  $b \in B^{NDG}$ :

$$\sum_{k \in K_{i,b}^B} SNDG_{i,b,k} = FNDG_{i,b}.$$

- 8.5.3.4 A constraint shall limit schedules for *dispatchable generation resources* within their minimum and maximum output for an interval.

For a *dispatchable variable generation resource*, the maximum schedule shall be limited by its forecast. That is:

8.5.3.4.1 For all intervals  $i \in I$  and all buses  $b \in B^{DG}$ ,

$$AdjMaxDG_{i,b} = \begin{cases} \min(MaxDG_{i,b}, FG_{i,b}) & \text{if } b \in B^{VG} \\ MaxDG_{i,b} & \text{otherwise} \end{cases}$$

and

$$AdjMinDG_{i,b} = \min(MinDG_{i,b}, AdjMaxDG_{i,b}).$$

8.5.3.4.2 For all intervals  $i \in I$  and all buses  $b \in B^{DG}$ :

$$AdjMinDG_{i,b} \leq \sum_{k \in K_{i,b}^E} SDG_{i,b,k} \leq AdjMaxDG_{i,b}.$$

8.5.3.5 A constraint shall limit the schedule for a *non-quick start resource* at or above its *minimum loading point* when such *resource* is committed or when the *resource* shutdown is yet to be confirmed by the *IESO*. For all *non-quick start resource* buses  $b \in B^{NQS}$  and intervals  $i \in I$ :

$$\sum_{k \in K_{i,b}^E} SDG_{i,b,k} \geq AtMLP_{i,b} \cdot MinQDG_b.$$

#### 8.5.4 Operating Reserve Requirements

8.5.4.1 The total synchronized *ten-minute operating reserve*, non-synchronized *ten-minute operating reserve* and *thirty-minute operating reserve* scheduled from a *dispatchable load* shall not exceed:

8.5.4.1.1 the *dispatchable load's* ramp capability over 30 minutes;

8.5.4.1.2 the total scheduled consumption less the non-*dispatchable* portion; and

8.5.4.1.3 the remaining portion of its capacity that is *dispatchable* after considering minimum load consumption constraints.

8.5.4.2 These restrictions shall be enforced by the following constraints for all intervals  $i \in I$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} S30RDL_{i,b,j} \leq 30 \cdot ORRDL_b;$$

$$\sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} S30RDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} SDL_{i,b,j} - QDLFIRM_{i,b};$$

and

$$\sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} S30RDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} SDL_{i,b,j} - MinDL_{i,b}.$$

8.5.4.3 The amount of both synchronized and non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide shall not exceed the amount by which the *dispatchable load* can decrease its consumption over 10 minutes, as limited by its *operating reserve* ramp rate. This restriction shall be enforced by the following constraint for all intervals  $i \in I$  and all buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \leq 10 \cdot ORRDL_b.$$

8.5.4.4 The total *operating reserve* scheduled from a *dispatchable generation resource* shall not exceed the *resource's* ramp capability over 30 minutes, its remaining capacity, and its unscheduled capacity. These restrictions shall be enforced by the following constraints for all intervals  $i \in I$  and all buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k} \leq 30 \cdot ORRDG_b;$$

$$\sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k}$$

$$\leq \sum_{k \in K_{i,b}^E} (QDG_{i,b,k} - SDG_{i,b,k});$$

and

$$\sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k}$$

$$\leq AdjMaxDG_{i,b} - \sum_{k \in K_{i,b}^E} SDG_{i,b,k}.$$

- 8.5.4.5 The amount of both synchronized and non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall not exceed the amount by which the *resource* can increase its output over 10 minutes, as limited by its *operating reserve ramp rate*. This restriction shall be enforced by the following constraint for all intervals  $i \in I$  and all buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \leq 10 \cdot ORRDG_b.$$

- 8.5.4.6 The amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall be limited by its *reserve loading point* for synchronized *ten-minute operating reserve*. This restriction shall be enforced by the following

constraint for all intervals  $i \in I$  and all buses  $b \in B^{DG}$  with  $RLP10S_{i,b} > 0$ :

$$\begin{aligned} \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} &\leq \left( \sum_{k \in K_{i,b}^E} SDG_{i,b,k} \right) \cdot \left( \frac{1}{RLP10S_{i,b}} \right) \\ &\cdot \left( \min \left\{ 10 \cdot ORRDG_b, \sum_{k \in K_{i,b}^{10S}} Q10SDG_{i,b,k} \right\} \right). \end{aligned}$$

- 8.5.4.7 The amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall be limited by its *reserve loading point* for *thirty-minute operating reserve*. This restriction shall be enforced by the following constraint for all intervals  $i \in I$  and all buses  $b \in B^{DG}$  with  $RLP30R_{i,b} > 0$ :

$$\begin{aligned} \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k} &\leq \left( \sum_{k \in K_{i,b}^E} SDG_{i,b,k} \right) \cdot \left( \frac{1}{RLP30R_{i,b}} \right) \\ &\cdot \left( \min \left\{ 30 \cdot ORRDG_b, \sum_{k \in K_{i,b}^{30R}} Q30RDG_{i,b,k} \right\} \right). \end{aligned}$$

## 8.5.5 Pseudo-Units

- 8.5.5.1 A constraint shall be required to calculate physical *generation resource* schedules from *pseudo-unit* schedules using the steam turbine *resource's* shares in the operating regions of the *pseudo-unit*

determined in section 10. For all intervals  $i \in I$  and *pseudo-unit* buses  $b \in B^{PSU}$ :

$$SSTMod_{i,p} = \sum_{b \in B_p^{ST}} \left( STShareMLP_b \cdot \left( \sum_{k \in K_{i,b}^{MLP}} SDG_{i,b,k} \right) + STShareDR_b \cdot \left( \sum_{k \in K_{i,b}^{DR}} SDG_{i,b,k} \right) + \sum_{k \in K_{i,b}^{DF}} SDG_{i,b,k} \right)$$

$$SCTMod_{i,b} = (1 - STShareMLP_b) \cdot \left( \sum_{k \in K_{i,b}^{MLP}} SDG_{i,b,k} \right) + (1 - STShareDR_b) \cdot \left( \sum_{k \in K_{i,b}^{DR}} SDG_{i,b,k} \right),$$

8.5.5.1.1 and for all intervals  $i \in I$  and steam turbine *resources*  $p \in PST$ :

8.5.5.2 Maximum constraints shall be enforced on the operating region to which they apply for both *energy* and *operating reserve* schedules. For all intervals  $i \in I$  and *pseudo-unit* buses  $b \in B^{PSU}$ :

$$\sum_{k \in K_{i,b}^{DR}} SDG_{i,b,k} \leq MaxDR_{i,b},$$

$$\sum_{k \in K_{i,b}^{DF}} SDG_{i,b,k} \leq MaxDF_{i,b},$$

and

$$\sum_{k \in K_{i,b}^{DR}} SDG_{i,b,k} + \sum_{k \in K_{i,b}^{DF}} SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k} \leq MaxDR_{i,b} + MaxDF_{i,b}.$$

8.5.5.3 For a *pseudo-unit* that cannot provide *ten-minute operating reserve* from its duct firing region, constraints shall limit the *pseudo-unit* from being scheduled to provide *ten-minute operating reserve* whenever the *pseudo-unit* is scheduled for *energy* in its duct firing region.

8.5.5.4 For the purposes of the *energy* balance constraint in section 8.7.1 and the transmission constraints in section 8.7.3, the combustion turbine *resource's* schedule for the *pseudo-unit* at bus  $b \in B^{PSU}$  in interval  $i \in I$ ,  $SCT_{i,b}$  shall be equal to:

8.5.5.4.1  $SCTMod_{i,b}$  if the *pseudo-unit* is scheduled at or above *minimum loading point*;

8.5.5.4.2 the portion of  $UpTraj_{i,b}$  or  $DnTraj_{i,b}$  defined in the section 8.6.2 that was allocated to the combustion turbine *resource* in accordance with section 10.6 if the *resource* is ramping to or ramping from its *minimum loading point*; or

8.5.5.4.3 0 otherwise.

8.5.5.5 For the purposes of the *energy* balance constraint in section 8.7.1 and the transmission constraints in section 8.7.3, the steam turbine *resource's* schedule for  $p \in PST$ ,  $SST_{i,p}$  shall be equal to  $SSTMod_{i,p}$  where  $SST_{i,p}$  will be corrected to account for the contribution from *pseudo-units*  $b \in B_p^{ST}$  ramping to or ramping from *minimum loading point* as determined by the allocation of  $UpTraj_{i,b}$  or  $DnTraj_{i,b}$  in accordance with section 10.6.

## 8.5.6 Dispatchable Hydroelectric Generation Resources

8.5.6.1 A *dispatchable hydroelectric generation resource* shall be scheduled within its *forbidden region* if the *resource* is being ramped through the *forbidden region* at its maximum *offered* ramp capability.

## 8.6 Dispatch Data Inter-Interval/Multi-Interval Constraints

### 8.6.1 Energy Ramping

8.6.1.1 For *dispatchable loads*, the ramping constraint in section 8.6.1.4 uses  $URRDL_b$  to represent a ramp up rate selected from  $URRDL_{i,b,w}$  and uses  $DRRDL_b$  to represent a ramp down rate selected from  $DRRDL_{i,b,w}$ .

8.6.1.2 For *dispatchable generation resources*, the ramping constraint in section 8.6.1.5 uses  $URRDG_b$  to represent a ramp up rate selected from  $URRDG_{i,b,w}$  and uses  $DRRDG_b$  to represent a ramp down rate selected from  $DRRDG_{i,b,w}$ .

- 8.6.1.3 The *real-time calculation engine* shall respect the ramping restrictions determined by the up to five *offered* MW quantity, ramp up rate and ramp down rate value sets.
- 8.6.1.4 In the case of *dispatchable loads*, *energy* schedules cannot vary by more than an interval's ramping capability for that *resource*. This constraint shall be enforced by the following for all intervals  $i \in I$  and buses  $b \in B^{DL}$ :

$$\begin{aligned} \sum_{j \in J_{i-1,b}^E} SDL_{i-1,b,j} - 5 \cdot DRRDL_b &\leq \sum_{j \in J_{i,b}^E} SDL_{i,b,j} \\ &\leq \sum_{j \in J_{i-1,b}^E} SDL_{i-1,b,j} + 5 \cdot URRDL_b. \end{aligned}$$

- 8.6.1.5 *Energy* schedules for a *dispatchable generation resource* cannot vary by more than an interval's ramping capability for that *resource*. This constraint shall be enforced by the following for all intervals  $i \in I$  and buses  $b \in B^{DG}$ :

$$\begin{aligned} \sum_{k \in K_{i-1,b}^E} SDG_{i-1,b,k} - 5 \cdot DRRDG_b &\leq \sum_{k \in K_{i,b}^E} SDG_{i,b,k} \\ &\leq \sum_{k \in K_{i-1,b}^E} SDG_{i-1,b,k} + 5 \cdot URRDG_b. \end{aligned}$$

#### 8.6.1 Non-Quick Start Resource Start-up and Shutdown

8.6.2.1 For all intervals in the real-time look-ahead period in which a *non-quick start resource* is scheduled to start-up, such *resource* shall be scheduled on a fixed ramp-up trajectory as determined by its *offered* ramp rates. The ramp-up trajectory ( $UpTraj_{i,b}$ ) for interval  $i \in I$  such that  $SU_{i,b}=1$  is determined as follows:

- 8.6.2.1.1 If  $i = 1$ , then  $UpTraj_{i,b}$  shall be determined from the *resource* initial schedule and the *offered* ramp up capability;
- 8.6.2.1.2 If  $i > 1$  and  $SU_{i-1,b} = 0$ , then  $UpTraj_{i,b}$  shall be determined from the *offered* ramp up capability from 0; and



8.6.2.1.3 For all intervals  $i \in I$  such that  $SU_{i,b}=1$ :

$$\sum_{k \in K_{i,b}^E} SDG_{i,b,k} = UpTraj_{i,b}.$$

8.6.2.2 For all intervals in the real-time look-ahead period in which a *non-quick start resource* is scheduled to shutdown, such *resource* shall be scheduled on a fixed ramp-down trajectory as determined by its *offered* ramp rates. The ramp-down trajectory ( $DnTraj_{i,b}$ ) for interval  $i \in I$  such that  $SD_{i,b} = 1$  is determined as follows:

8.6.2.2.1 If  $i = 1$ , then  $DnTraj_{i,b}$  shall be determined from the *resource* initial schedule and the *offered* ramp down capability;

8.6.2.2.2 If  $i > 1$  and  $SD_{i-1,b} = 0$ , then  $DnTraj_{i,b}$  shall be  $MinQDG_{b,i}$  and

8.6.2.2.3 If  $i > 1$  and  $SD_{i-1,b} = 1$ , then  $DnTraj_{i,b}$  shall be determined from the *offered* ramp down capability from  $DnTraj_{i-1,b}$ .

8.6.2.2.4 For all intervals  $i \in I$  such that  $SD_{i,b} = 1$ :

$$\sum_{k \in K_{i,b}^E} SDG_{i,b,k} = DnTraj_{i,b}.$$

### 8.6.3 Operating Reserve Ramping

8.6.3.1 Constraints shall be applied to recognize that interval to interval changes to a *dispatchable load's* schedule for *energy* may modify the

amount of *operating reserve* that the *resource* can provide. For all intervals  $i \in I$  and all buses  $b \in B^{DL}$ :

$$\begin{aligned} \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} S30RDL_{i,b,j} \\ \leq - \sum_{j \in J_{i-1,b}^E} SDL_{i-1,b,j} + \sum_{j \in J_{i,b}^E} SDL_{i,b,j} + 30 \cdot ORRD L_b \end{aligned}$$

and

$$\begin{aligned} \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \\ \leq - \sum_{j \in J_{i-1,b}^E} SDL_{i-1,b,j} + \sum_{j \in J_{i,b}^E} SDL_{i,b,j} + 10 \cdot ORRD L_b. \end{aligned}$$

8.6.3.2 Constraints shall be applied to recognize that interval to interval changes in a *dispatchable generation resource's* schedule for *energy* may modify the amount of *operating reserve* that the *resource* can provide. For all intervals  $i \in I$  and all buses  $b \in B^{DG}$ :

$$\begin{aligned} \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k} \\ \leq \sum_{k \in K_{i-1,b}^E} SDG_{i-1,b,k} - \sum_{k \in K_{i,b}^E} SDG_{i,b,k} + 30 \cdot ORRD G_b \end{aligned}$$

and

$$\begin{aligned} \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \\ \leq \sum_{k \in K_{i-1,b}^E} SDG_{i-1,b,k} - \sum_{k \in K_{i,b}^E} SDG_{i,b,k} + 10 \cdot ORRD G_b. \end{aligned}$$

## 8.7 Constraints for Reliability Requirements

### 8.7.1 Energy Balance

- 8.7.1.1 The total amount of *energy* withdrawals scheduled at load bus  $b \in B$  in interval  $i \in I$ ,  $With_{i,b}$  shall be:

$$With_{i,b} = \begin{cases} \sum_{j \in J_{i,b}^E} SDL_{i,b,j} & \text{if } b \in B^{DL} \\ FHDR_{i,b} & \text{if } b \in B^{HDR} \\ FNBL_{i,b} & \text{if } b \in B^{NoBid} \end{cases}$$

- 8.7.1.2 The total amount of export *energy* scheduled at *intertie zone* bus  $d \in DX$  in interval  $i \in I$ ,  $With_{i,d}$ , as the fixed exports from Ontario to the *intertie zone* export bus shall be:

$$With_{i,d} = FXLSch_{i,d}.$$

- 8.7.1.3 The total amount of injections scheduled at internal bus  $b \in B$ , in interval  $i \in I$ ,  $Inj_{i,b}$  shall be:

$$Inj_{i,b} = \begin{cases} \sum_{k \in K_{i,b}^E} SNDG_{i,b,k} & \text{if } b \in B^{NDG} \\ \sum_{k \in K_{i,b}^E} SDG_{i,b,k} & \text{if } b \in B^{DG} \\ FNOG_{i,b} & \text{if } b \in B^{NoOffer} \end{cases}$$

- 8.7.1.4 The total amount of import *energy* scheduled at *intertie zone* bus  $d \in DI$  in interval  $i \in I$ ,  $Inj_{i,d}$ , as the imports into Ontario from that *intertie zone* bus shall be:

$$Inj_{i,d} = FIGSch_{i,d}.$$

- 8.7.1.5 Injections and withdrawals at each bus shall be multiplied by one plus the marginal loss factor to reflect the losses or reduction in losses that result when injections or withdrawals occur at locations other than the *reference bus*. These loss-adjusted injections and withdrawals must then be equal to each other after taking into account the adjustment for any discrepancy between total and marginal losses. Load or generation reduction associated with the demand constraint violation shall be subtracted from the total load or generation for the *real-time calculation engine* to produce a solution.

For interval  $i \in I$ , the *energy* balance shall be:

$$\begin{aligned}
 FL_i + & \sum_{b \in B^{DL} \cup B^{HDR} \cup B^{NoBid}} (1 + MglLoss_{i,b}) \cdot With_{i,b} \\
 & + \sum_{d \in DX} (1 + MglLoss_{i,d}) \cdot With_{i,d} - \sum_{w=1..N_{LdViol_i}} SLdViol_{i,w} \\
 = & \sum_{b \in B^{NDG} \cup B^{DG} \cup B^{NoOffer}} (1 + MglLoss_{i,b}) \cdot Inj_{i,b} \\
 & + \sum_{d \in DI} (1 + MglLoss_{i,d}) \cdot Inj_{i,d} - \sum_{w=1..N_{GenViol_i}} SGenViol_{i,w} \\
 & + LossAdj_i.
 \end{aligned}$$

## 8.7.2 Operating Reserve Requirements

- 8.7.2.1 *Operating reserve* shall be scheduled to meet system-wide requirements for synchronized *ten-minute operating reserve*, total *ten-minute operating reserve*, and *thirty-minute operating reserve* while respecting all applicable regional minimum requirements and regional maximum restrictions for *operating reserve*.
- 8.7.2.2 Constraint violation penalty curves shall be used to impose a penalty cost for not meeting the *IESO's* system-wide *operating reserve* requirements, not meeting a regional minimum requirement, or not adhering to a regional maximum restriction. Full *operating reserve* requirements shall be scheduled unless the cost of doing so would be higher than the applicable penalty cost. For each interval  $i \in I$ :

$$\begin{aligned}
 \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \right) \\
 + \sum_{w=1..N_{10SViol_i}} S10SViol_{i,w} \geq TOT10S_i;
 \end{aligned}$$

$$\begin{aligned}
& \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \right) \\
& + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \right) \\
& + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \right) + \sum_{d \in DX} F10NXLSch_{i,d} \\
& + \sum_{d \in DI} F10NIGSch_{i,d} + \sum_{w=1..N_{10RViol_i}} S10RViol_{i,w} \\
& \geq TOT10R_i;
\end{aligned}$$

and

$$\begin{aligned}
& \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \right) + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \right) \\
& + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \right) \\
& + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \right) + \sum_{d \in DX} F10NXLSch_{i,d} \\
& + \sum_{d \in DI} F10NIGSch_{i,d} + \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^{30R}} S30RDL_{i,b,j} \right) \\
& + \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k} \right) + \sum_{d \in DX} F30RXLSch_{i,d} \\
& + \sum_{d \in DI} F30RIGSch_{i,d} + \sum_{w=1..N_{30RViol_i}} S30RViol_{i,w} \\
& \geq TOT30R_i.
\end{aligned}$$

8.7.2.3 The following constraints shall be applied for each interval  $i \in I$  and each region  $r \in ORREG$ :

$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} F10NXLSch_{i,d} + \sum_{d \in D_r^{REG} \cap DI} F10NIGSch_{i,d} \\
& + \sum_{w=1..N_{REG10RViol_i}} SREG10RViol_{r,i,w} \geq REGMin10R_{i,r}; \\
\\
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} F10NXLSch_{i,d} + \sum_{d \in D_r^{REG} \cap DI} F10NIGSch_{i,d} \\
& - \sum_{w=1..N_{XREG10RViol_i}} SXREG10RViol_{r,i,w} \leq REGMax10R_{i,r}; \\
\\
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} F10NXLSch_{i,d} + \sum_{d \in D_r^{REG} \cap DI} F10NIGSch_{i,d} \\
& - \sum_{w=1..N_{XREG10RViol_i}} SXREG10RViol_{r,i,w} \leq REGMax10R_{i,r};
\end{aligned}$$

$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} F10NXLSch_{i,d} + \sum_{d \in D_r^{REG} \cap DI} F10NIGSch_{i,d} \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{30R}} S30RDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} F30RXLSch_{i,d} + \sum_{d \in D_r^{REG} \cap DI} F30RIGSch_{i,d} \\
& + \sum_{w=1..N_{REG30RViol_i}} SREG30RViol_{r,i,w} \geq REGMin30R_{i,r};
\end{aligned}$$

and

$$\begin{aligned}
& \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10S}} S10SDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10S}} S10SDG_{i,b,k} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{10N}} S10NDL_{i,b,j} \right) + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{10N}} S10NDG_{i,b,k} \right) \\
& + \sum_{d \in D_r^{REG} \cap DX} F10NXLSch_{i,d} + \sum_{d \in D_r^{REG} \cap DI} F10NIGSch_{i,d} \\
& + \sum_{b \in B_r^{REG} \cap B^{DL}} \left( \sum_{j \in J_{i,b}^{30R}} S30RDL_{i,b,j} \right) \\
& + \sum_{b \in B_r^{REG} \cap B^{DG}} \left( \sum_{k \in K_{i,b}^{30R}} S30RDG_{i,b,k} \right) + \sum_{d \in D_r^{REG} \cap DX} F30RXLSch_{i,d} \\
& + \sum_{d \in D_r^{REG} \cap DI} F30RIGSch_{i,d} \\
& - \sum_{w=1..N_{XREG30RViol_i}} SXREG30RViol_{r,i,w} \\
& \leq REGMax30R_{i,r}.
\end{aligned}$$

### 8.7.3 IESO Internal Transmission Limits

8.7.3.1 A set of *energy* schedules shall be produced that do not violate any *security* limits in the pre-contingency state and the post-contingency state subject to the remainder of this section 8.7.3. The total amount

of *energy* scheduled to be injected and withdrawn at each bus used by the *energy* balance constraint in section 8.7.1.5, shall be used to produce these schedules.

- 8.7.3.2 Pre-contingency,  $SPreITLViol_{f,i,w}$  and post-contingency,  $SITLViol_{c,f,i,w}$  transmission limit violation variables shall allow the *real-time calculation engine* to find a solution.
- 8.7.3.3 For all intervals  $i \in I$  and *facilities*  $f \in F_i$ , the linearized constraints for violated pre-contingency limits obtained from the *security* assesment function shall take the form:

$$\begin{aligned} & \sum_{b \in B^{NDG} \cup B^{DG} \cup B^{NoOffer}} PreConSF_{i,f,b} \cdot Inj_{i,b} \\ & - \sum_{b \in B^{DL} \cup B^{HDR} \cup B^{NoBid}} PreConSF_{i,f,b} \cdot With_{i,b} \\ & + \sum_{d \in DI} PreConSF_{i,f,d} \cdot Inj_{i,d} - \sum_{d \in DX} PreConSF_{i,f,d} \\ & \cdot With_{i,d} - \sum_{w=1..N_{PreITLViol_{f,i}}} SPreITLViol_{f,i,w} \\ & \leq AdjNormMaxFlow_{i,f}. \end{aligned}$$

- 8.7.3.4 For all intervals  $i \in I$ , contingencies  $c \in C$ , and *facilities*  $f \in F_{i,c}$ , the linearized constraints for violated post-contingency limits obtained from the *security* assesment function shall take the form:

$$\begin{aligned} & \sum_{b \in B^{NDG} \cup B^{DG} \cup B^{NoOffer}} SF_{i,c,f,b} \cdot Inj_{i,b} \\ & - \sum_{b \in B^{DL} \cup B^{HDR} \cup B^{NoBid}} SF_{i,c,f,b} \cdot With_{i,b} + \sum_{d \in DI} SF_{i,c,f,d} \\ & \cdot Inj_{i,d} - \sum_{d \in DX} SF_{i,c,f,d} \cdot With_{i,d} \\ & - \sum_{w=1..N_{ITLViol_{c,f,i}}} SITLViol_{c,f,i,w} \leq AdjEmMaxFlow_{i,c,f}. \end{aligned}$$



## 8.7.4 Penalty Price Variable Bounds

8.7.4.1 Penalty price variables shall be restricted to the ranges determined by the constraint violation penalty curves for the Real-Time Scheduling algorithm and for all intervals  $i \in I$ :

$$\begin{aligned} 0 \leq SLdViol_{i,w} &\leq QLdViolSch_{i,w} && \text{for all } w \in \{1, \dots, N_{LdViol_i}\}; \\ 0 \leq SGenViol_{i,w} &\leq QGenViolSch_{i,w} && \text{for all } w \in \{1, \dots, N_{GenViol_i}\}; \\ 0 \leq S10SViol_{i,w} &\leq Q10SViolSch_{i,w} && \text{for all } w \in \{1, \dots, N_{10SViol_i}\}; \\ 0 \leq S10RViol_{i,w} &\leq Q10RViolSch_{i,w} && \text{for all } w \in \{1, \dots, N_{10RViol_i}\}; \\ \\ 0 \leq S30RViol_{i,w} &\leq Q30RViolSch_{i,w} && \text{for all } w \in \{1, \dots, N_{30RViol_i}\}; \\ 0 \leq SREG10RViol_{r,i,w} &\leq QREG10RViolSch_{i,w} && \text{for all } r \in ORREG, w \in \{1, \dots, N_{REG10RViol_i}\}; \\ 0 \leq SREG30RViol_{r,i,w} &\leq QREG30RViolSch_{i,w} && \text{for all } r \in ORREG, w \in \{1, \dots, N_{REG30RViol_i}\}; \\ 0 \leq SXREG10RViol_{r,i,w} &\leq QXREG10RViolSch_{i,w} && \text{for all } r \in ORREG, w \in \{1, \dots, N_{XREG10RViol_i}\}; \\ 0 \leq SXREG30RViol_{r,i,w} &\leq QXREG30RViolSch_{i,w} && \text{for all } r \in ORREG, w \in \{1, \dots, N_{XREG30RViol_i}\}; \\ 0 \leq SPreITLViol_{f,i,w} &\leq QPreITLViolSch_{f,i,w} && \text{for all } f \in F_i, w \in \{1, \dots, N_{PreITLViol_{f,i}}\}; \\ \text{and} &&& \\ 0 \leq SITLViol_{c,f,i,w} &\leq QITLViolSch_{c,f,i,w} && \text{for all } c \in C, f \in F_{i,c}, w \in \{1, \dots, N_{ITLViol_{c,f,i}}\}. \end{aligned}$$

## 8.8 Outputs

8.8.1 Outputs for the Real-Time Scheduling algorithm includes *resource* schedules.

# 9 Real-Time Pricing

## 9.1 Purpose

9.1.1 The Real-Time Pricing algorithm shall perform a *security*-constrained economic *dispatch* to maximize gains from trade to meet the *IESO's* province-wide non-*dispatchable demand* forecast and the *IESO*-specified *operating reserve* requirements for each interval of the real-time look-ahead period.

## 9.2 Information, Sets, Indices and Parameters

9.2.1 Information, sets, indices and parameters used by the Real-Time Pricing algorithm are described in sections 3 and 4. In addition, the following *resource*

schedules from the Real-Time Scheduling algorithm in section 8 shall be used in the Real-Time Pricing algorithm:

- 9.2.1.1  $SD_{i,b}^{RTS} \in \{0,1\}$ , which designates whether the *dispatchable generation resource* at bus  $b \in B^{NQS}$  was scheduled on a shutdown trajectory in interval  $i \in I$  such that  $EvalSD_{i,b} = 1$ ;
- 9.2.1.2  $SDLInitSch_{0,b}$ , which designates the initial schedule for the *dispatchable load* at bus  $b \in B^{DL}$  used in the Real-Time Scheduling algorithm in section 8; and
- 9.2.1.3  $SDGInitSch_{0,b}$ , which designates the initial schedule for the *dispatchable generation resource* at bus  $b \in B^{DG}$  used in the Real-Time Scheduling algorithm in section 8.

### 9.3 Variables and Objective Function

- 9.3.1 The Real-Time Pricing algorithm shall solve for the same variables as the Real-Time Scheduling algorithm in section 8.3.1.
- 9.3.2 The objective function for the Real-Time Pricing algorithm shall maximize gains from trade by maximizing the expression in section 8.3.2 for the Real-Time Scheduling algorithm.

9.3.3  $ViolCost_i$  shall be calculated as follows:

$$\begin{aligned}
 ViolCost_i = & \sum_{w=1..N_{LdViol_i}} SLdViol_{i,w} \cdot PLdViolPrc_{i,w} \\
 & - \sum_{w=1..N_{GenViol_i}} SGenViol_{i,w} \cdot PGenViolPrc_{i,w} \\
 & + \sum_{w=1..N_{10SViol_i}} S10SViol_{i,w} \cdot P10SViolPrc_{i,w} \\
 & + \sum_{w=1..N_{10RViol_i}} S10RViol_{i,w} \cdot P10RViolPrc_{i,w} \\
 & + \sum_{w=1..N_{30RViol_i}} S30RViol_{i,w} \cdot P30RViolPrc_{i,w} \\
 & + \sum_{r \in ORREG} \left( \sum_{w=1..N_{REG10RViol_i}} SREG10RViol_{r,i,w} \cdot PREG10RViolPrc_{i,w} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{w=1..N_{REG30RViol_i}} SREG30RViol_{r,i,w} \cdot PREG30RViolPrc_{i,w} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{w=1..N_{XREG10RViol_i}} SXREG10RViol_{r,i,w} \cdot PXREG10RViolPrc_{i,w} \right) \\
 & + \sum_{r \in ORREG} \left( \sum_{w=1..N_{XREG30RViol_i}} SXREG30RViol_{r,i,w} \cdot PXREG30RViolPrc_{i,w} \right) \\
 & + \sum_{f \in F_i} \left( \sum_{w=1..N_{PreITLViol_{f,i}}} SPreITLViol_{f,i,w} \cdot PPreITLViolPrc_{f,i,w} \right) \\
 & + \sum_{c \in C} \sum_{f \in F_{i,c}} \left( \sum_{w=1..N_{ITLViol_{c,f,i}}} SITLViol_{c,f,i,w} \cdot PITLViolPrc_{c,f,i,w} \right).
 \end{aligned}$$

9.3.3.1 The constraints in section 9.4 shall apply to the Real-Time Pricing algorithm.

## 9.4 Constraints

9.4.1 The Real-Time Pricing algorithm optimization function shall apply the constraints described in sections 9.5 – 9.8.

## 9.5 Dispatch Data Constraints Applying to Individual Intervals

### 9.5.1 Scheduling Variable Bounds

9.5.1.1 The constraints in section 8.5.1 shall apply in the Real-Time Pricing algorithm, with the following exceptions for a *non-quick start resource* bus  $b \in B^{NQS}$  and interval  $i \in I$ , where:

9.5.1.1.1  $AtZero_{i,b}$  shall be replaced by  $AtZero_{i,b}^{RTP}$ ;

9.5.1.1.2  $AtMLP_{i,b}$  shall be replaced by  $AtMLP_{i,b}^{RTP}$ ; and

9.5.1.1.3  $EvalSD_{i,b}$  shall be replaced by  $EvalSD_{i,b}^{RTP}$ .

### 9.5.2 Resource Initial Conditions

9.5.2.1 The initial schedule for a *dispatchable load* at bus  $b \in B^{DL}$  shall be fixed to the *resource* initial schedules. For all *dispatchable load* buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{0,b}^E} SDL_{0,b,j} = SDLInitPrc_{0,b}$$

9.5.2.2 The initial schedule for a *dispatchable generation resource* at bus  $b \in B^{DG}$  shall be fixed to the *resource* initial schedules. For all *dispatchable generation resource* buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{0,b}^E} SDG_{0,b,k} = SDGInitPrc_{0,b}$$

### 9.5.3 Resource Minimums and Maximums

9.5.3.1 The constraints in section 8.5.3 shall apply in the Real-Time Pricing algorithm, with the following exception:

9.5.3.1.1  $AtMLP_{i,b}$  shall be replaced by  $AtMLP_{i,b}^{RTP}$

where  $AtMLP_{i,b}^{RTP}$  is determined in accordance with section 9.8.1.

### 9.5.4 Operating Reserve Requirements

9.5.4.1 The constraints in section 8.5.4 shall apply in the Real-Time Pricing algorithm.

#### 9.5.5 Pseudo-Units

9.5.5.1 The constraints in section 8.5.5 shall apply in the Real-Time Pricing algorithm.

#### 9.5.6 Dispatchable Hydroelectric Generation Resources

9.5.6.1 The constraints in section 8.5.6 shall apply in the Real-Time Pricing algorithm.

### 9.6 Dispatch Data Inter-Interval/Multi-Interval Constraints

#### 9.6.1 Energy Ramping

9.6.1.1 The constraints in section 8.6.1 shall apply in the Real-Time Pricing algorithm.

#### 9.6.2 Non-Quick Start Resource Start-up and Shutdown

9.6.2.1 The constraints in section 8.6.2 shall apply in the Real-Time Pricing algorithm, with the exception of the *non-quick start resource* start-up and shutdown statuses, which are determined in accordance with section 9.8.1.

#### 9.6.3 Operating Reserve Ramping

9.6.3.1 The constraints in section 8.6.3 shall apply in the Real-Time Pricing algorithm.

### 9.7 Constraints for Reliability Requirements

#### 9.7.1 Energy Balance

9.7.1.1 The constraint in section 8.7.1 shall apply in the Real-Time Pricing algorithm, with the following exceptions:

9.7.1.1.1  $FXLSch_{i,d}$  shall be replaced by  $FXLPr_{i,d}$  in section 8.7.1.2;

9.7.1.1.2  $FIGSch_{i,d}$  shall be replaced by  $FIGPr_{i,d}$  in section 8.7.1.4; and

9.7.1.1.3 The *energy* balance constraint in section 8.7.1.5 shall be modified to account for the *demand* adjustment required to calculate *locational marginal prices* when a

voltage reduction or load shedding has been implemented, as follows:

$$\begin{aligned}
& FL_i + CAAdj_i + \sum_{b \in B^{DL} \cup B^{HDR} \cup B^{NoBid}} (1 + MglLoss_{i,b}) \cdot With_{i,b} \\
& + \sum_{d \in DX} (1 + MglLoss_{i,d}) \cdot With_{i,d} \\
& - \sum_{w=1..N_{LdViol_i}} SLdViol_{i,w} \\
& = \sum_{b \in B^{NDG} \cup B^{DG} \cup B^{NoOffer}} (1 + MglLoss_{i,b}) \cdot Inj_{i,b} \\
& + \sum_{d \in DI} (1 + MglLoss_{i,d}) \cdot Inj_{i,d} \\
& - \sum_{w=1..N_{GenViol_i}} SGenViol_{i,w} + LossAdj_i.
\end{aligned}$$

## 9.7.2 Operating Reserve Requirements

9.7.2.1 The constraint in section 8.7.2 shall apply in the Real-Time Pricing algorithm, with the following exceptions:

- 9.7.2.1.1  $F10NXLSch_{i,d}$  shall be replaced by  $F10NXLPrc_{i,d}$  for all  $d \in DX$ ;
- 9.7.2.1.2  $F10NIGSch_{i,d}$  shall be replaced by  $F10NIGPrc_{i,d}$  for all  $d \in DI$ ;
- 9.7.2.1.3  $F30RXLSch_{i,d}$  shall be replaced by  $F30RXLPrc_{i,d}$  for all  $d \in DX$ ; and
- 9.7.2.1.4  $F30RIGSch_{i,d}$  shall be replaced by  $F30RIGPrc_{i,d}$  for all  $d \in DI$ .

## 9.7.3 IESO Internal Transmission Limits

9.7.3.1 The constraints in section 8.7.3 shall apply in the Real-Time Pricing algorithm except the sensitivities and limits considered shall be those provided by the most recent *security* assessment function iteration of the Real-Time Pricing algorithm.

## 9.7.4 Penalty Price Variable Bounds

9.7.4.1 The following constraints shall restrict the penalty price variables to the ranges determined by the constraint violation penalty curves. For all intervals  $i \in I$ :

$$\begin{aligned}
 0 \leq SLdViol_{i,w} &\leq QLdViolPrc_{i,w} && \text{for all } w \in \{1, \dots, N_{LdViol_i}\}; \\
 0 \leq SGenViol_{i,w} &\leq QGenViolPrc_{i,w} && \text{for all } w \in \{1, \dots, N_{GenViol_i}\}; \\
 0 \leq S10SViol_{i,w} &\leq Q10SViolPrc_{i,w} && \text{for all } w \in \{1, \dots, N_{10SViol_i}\}; \\
 0 \leq S10RViol_{i,w} &\leq Q10RViolPrc_{i,w} && \text{for all } w \in \{1, \dots, N_{10RViol_i}\}; \\
 0 \leq S30RViol_{i,w} &\leq Q30RViolPrc_{i,w} && \text{for all } w \in \{1, \dots, N_{30RViol_i}\}; \\
 0 \leq SREG10RViol_{r,i,w} &\leq QREG10RViolPrc_{i,w} && \text{for all } r \in ORREG, w \in \{1, \dots, N_{REG10RViol_i}\}; \\
 0 \leq SREG30RViol_{r,i,w} &\leq QREG30RViolPrc_{i,w} && \text{for all } r \in ORREG, w \in \{1, \dots, N_{REG30RViol_i}\}; \\
 0 \leq SXREG10RViol_{r,i,w} &\leq QXREG10RViolPrc_{i,w} && \text{for all } r \in ORREG, w \in \{1, \dots, N_{XREG10RViol_i}\}; \\
 0 \leq SXREG30RViol_{r,i,w} &\leq QXREG30RViolPrc_{i,w} && \text{for all } r \in ORREG, w \in \{1, \dots, N_{XREG30RViol_i}\}; \\
 0 \leq SPreITLViol_{f,i,w} &\leq QPreITLViolPrc_{f,i,w} && \text{for all } f \in F_i, w \in \{1, \dots, N_{PreITLViol_{f,i}}\}; \text{ and} \\
 0 \leq SITLViol_{c,f,i,w} &\leq QITLViolPrc_{c,f,i,w} && \text{for all } c \in C, f \in F_{i,c}, w \in \{1, \dots, N_{ITLViol_{c,f,i}}\}.
 \end{aligned}$$

## 9.8 Constraints to Ensure the Price Setting Eligibility of Offer/Bid Laminations

### 9.8.1 Non-Quick Start Resources

9.8.1.1 The Real-Time Pricing algorithm shall modify the following start-up and shutdown statuses for a *non-quick start resource* at bus  $b \in B^{NQS}$  and interval  $i \in I$ :

9.8.1.1.1  $AtZero_{i,b}^{RTP} \in \{0,1\}$ , which designates that the *resource* is not scheduled and is calculated as follows:

$$AtZero_{i,b}^{RTP} = AtZero_{i,b}.$$

9.8.1.1.2  $SU_{i,b}^{RTP} \in \{0,1\}$ , which designates that the *resource* must be scheduled for *energy* on its start-up trajectory and is calculated as follows:

$$SU_{i,b}^{RTP} = SU_{i,b}.$$

9.8.1.1.3  $AtMLP_{i,b}^{RTP} \in \{0,1\}$ , which designates that the *resource* is scheduled for *energy* at or above the *minimum loading point* and is calculated as follows:

$$AtMLP_{i,b}^{RTP} = \begin{cases} AtMLP_{i,b} & \text{if } EvalSD_{i,b} = 0 \\ 1 - SD_{i,b}^{RTS} & \text{if } EvalSD_{i,b} = 1 \end{cases}$$

9.8.1.1.4  $EvalSD_{i,b}^{RTP} \in \{0,1\}$ , which designates that the *resource* can be scheduled for *energy* below the *minimum loading point* and is calculated as follows:

$$EvalSD_{i,b}^{RTP} = 0.$$

9.8.1.1.5  $SD_{i,b}^{RTP} \in \{0,1\}$ , which designates that the *resource* must be scheduled for *energy* on its shutdown trajectory and is calculated as follows:

$$SD_{i,b}^{RTP} = \begin{cases} SD_{i,b} & \text{if } EvalSD_{i,b} = 0 \\ SD_{i,b}^{RTS} & \text{if } EvalSD_{i,b} = 1 \end{cases}$$

## 9.9 Outputs

9.9.1 Outputs for the Real-Time Pricing algorithm include:

9.9.1.1 shadow prices;

9.9.1.2 *locational marginal prices* and their components; and

9.9.1.3 sensitivity factors.

# 10 Pseudo-Unit Modelling

## 10.1 Pseudo-Unit Model Parameters

10.1.1 The *real-time calculation engine* shall use the following registration and *dispatch data* to determine the underlying relationship between a *pseudo-unit* and the associated physical *resources* for a *combined cycle plant* with  $K$  combustion turbine *resources* and one steam turbine *resource*:

10.1.1.1  $CMCR_{k_t}$  which designates the registered *maximum continuous rating* of combustion turbine *resource*  $k \in \{1, \dots, K\}$  in MW;



- 10.1.1.2  $CMLP_k$ , which designates the *minimum loading point* of combustion turbine *resource*  $k \in \{1,..,K\}$  in MW;
  - 10.1.1.3  $SMCR$ , which designates the registered *maximum continuous rating* of the steam turbine *resource* in MW;
  - 10.1.1.4  $SMLP$ , which designates the *minimum loading point* of the steam turbine *resource* in MW for a 1x1 configuration;
  - 10.1.1.5  $SDF$ , which designates the amount of duct firing capacity available on the steam turbine *resource* in MW;
  - 10.1.1.6  $STPortion_k$ , which designates the percentage of the steam turbine *resource's* capacity attributed to *pseudo-unit*  $k \in \{1,..,K\}$ ; and
  - 10.1.1.7  $CSCM_k \in \{0,1\}$ , which designates whether *pseudo-unit*  $k \in \{1,..,K\}$  is flagged to operate in *single cycle mode*.
- 10.1.2 The *real-time calculation engine* shall calculate the following model parameters for each *pseudo-unit*  $k \in \{1,..,K\}$ :
- 10.1.2.1  $MMCR_k$ , which designates the *maximum continuous rating* of *pseudo-unit*  $k$  and is calculated as follows:
$$CMCR_k + SMCR \cdot STPortion_k \cdot (1 - CSCM_k)$$
  - 10.1.2.2  $MMLP_k$ , which designates the *minimum loading point* of *pseudo-unit*  $k$  and is calculated as follows:
$$CMLP_k + SMLP \cdot (1 - CSCM_k)$$
  - 10.1.2.3  $MDF_k$ , which designates the duct firing capacity of *pseudo-unit*  $k$  and is calculated as follows:
$$SDF \cdot STPortion_k \cdot (1 - CSCM_k)$$
  - 10.1.2.4  $MDR_k$ , which designates the *dispatchable* capacity of *pseudo-unit*  $k$  and is calculated as follows:
$$MMCR_k - MMLP_k - MDF_k$$
- 10.1.3 The *real-time calculation engine* shall define three operating regions of *pseudo-unit*  $k \in \{1,..,K\}$ , as follows:
- 10.1.3.1 The *minimum loading point* region shall be the capacity between 0 and  $MMLP_k$ ;

10.1.3.2 The *dispatchable* region shall be the capacity between  $MMLP_k$  and  $MMLP_k + MDR_k$ ;

10.1.3.3 The duct firing region shall be the capacity between  $MMLP_k + MDR_k$  and  $MMCR_k$ .

10.1.4 The *real-time calculation engine* shall calculate the associated combustion turbine *resource* and steam turbine *resource* shares for the three operating regions of *pseudo-unit*  $k \in \{1, \dots, K\}$ , as follows:

10.1.4.1 For the *minimum loading point* region:

10.1.4.1.1 Steam turbine *resource* share:

$$STShareMLP_k = \frac{SMLP_k(1 - CSCM_k)}{MMLP_k};$$

10.1.4.1.2 Combustion turbine *resource* share:

$$CTShareMLP_k = \frac{CMLP_k}{MMLP_k}; \text{ and}$$

10.1.4.2 For the *dispatchable* region:

10.1.4.2.1 Steam turbine *resource* share:

$$STShareDR_k = \frac{(1 - CSCM_k)(SMCR \cdot STPortion_k - SMLP - SDF \cdot STPortion_k)}{MDR_k};$$

and

10.1.4.2.2 Combustion turbine *resource* share:

$$CTShareDR_k = \frac{CMCR_k - CMLP_k}{MDR_k}; \text{ and}$$

10.1.4.3 For the duct firing region:

10.1.4.3.1 Steam turbine *resource* share shall be equal to 1; and

10.1.4.3.2 Combustion turbine *resource* share shall be equal to 0.

## 10.2 Application of Physical Resource Deratings to the Pseudo-Unit Model

10.2.1 The *real-time calculation engine* shall apply deratings submitted by *market participants* to the applicable *dispatchable* capacity and duct firing capacity parameters for a *pseudo-unit*, where:

10.2.1.1  $CTCap_{i,k}$  designates the capacity of combustion turbine *resource*  $k \in \{1,...,K\}$  in interval  $i$  as determined by submitted deratings;

10.2.1.2  $STCap_i$  designates the capacity of the steam turbine *resource* in interval  $i$  as determined by submitted deratings; and

10.2.1.3  $TotalQ_{i,k}$  designates the total *offered* quantity of *energy* for *pseudo-unit*  $k \in \{1,...,K\}$  in interval  $i$ .

10.2.2 The *real-time calculation engine* shall solve for the following operating region parameters for each *pseudo-unit*  $k \in \{1,...,K\}$ :

10.2.2.1  $MLP_{i,k}$  designates the *minimum loading point* of *pseudo-unit*  $k$  in interval  $i$ ;

10.2.2.2  $DR_{i,k}$  designates the *dispatchable* capacity region of *pseudo-unit*  $k$  in interval  $i$ ; and

10.2.2.3  $DF_{i,k}$  designates the duct firing capacity region of *pseudo-unit*  $k$  in interval  $i$ .

10.2.3 Pre-Processing of De-rates

10.2.3.1 The *real-time calculation engine* shall perform the following pre-processing steps to determine the available operating regions for a *pseudo-unit* based on the combustion turbine *resource's* and steam turbine *resource's* share and the application of the *pseudo-unit* deratings. For *pseudo-unit*  $k \in \{1,...,K\}$  for interval  $i \in I$ :

10.2.3.1.1 Step 1: Calculate the amount of the *offer* for *energy* that is attributed to each combustion turbine *resource* ( $CTAmt_{i,k}$ ) and steam turbine *resource* portion ( $STAmt_{i,k}$ ):

If  $TotalQ_{i,k} < MMLP_k$ , then:

Calculate  $CTAmt_{i,k} = 0$ ; and

Calculate  $STAmt_{i,k} = 0$ .

Otherwise:

$CTAmtMLP = MMLP_k \cdot CTShareMLP_k$ ; and

$STAmtMLP = MMLP_k \cdot STShareMLP_k$ .

If  $TotalQ_{i,k} > MMLP_k + MDR_k$ , then:

$CTAmtDR = MDR_k \cdot CTShareDR_k$ ;

$STAmtDR = MDR_k \cdot STShareDR_k$ ; and

$STAmtDF = (1 - CSCM_k) \cdot (TotalQ_{i,k} - MMLP_k - MDR_k)$ .

Otherwise:

$CTAmtDR = (TotalQ_{i,k} - MMLP_k) \cdot CTShareDR_k$ ;

$STAmtDR = (TotalQ_{i,k} - MMLP_k) \cdot STShareDR_k$ ;

$STAmtDF = 0$ ;

$CTAmt_{i,k} = CTAmtMLP + CTAmtDR$ ; and

$STAmt_{i,k} = STAmtMLP + STAmtDR + STAmtDF$ .

10.2.3.1.2 Step 2: Allocate the steam turbine *resource's* capacity to each *pseudo-unit*:

$$PRSTCap_{i,k} = \left( \frac{STAmt_{i,k}}{\sum_{w \in \{1, \dots, K\}} STAmt_{i,w}} \right) \cdot STCap_i$$

10.2.3.1.3 Step 3: Determine if the *pseudo-unit* is available:

If  $CTAmt_{i,k} < CMLP_k$ , then the *pseudo-unit* is unavailable.

If  $STAmt_{i,k} < SMLP \cdot (1 - CSCM_k)$ , then the *pseudo-unit* is unavailable.

If  $CTCap_{i,k} < CMLP_k$ , then the *pseudo-unit* is unavailable.

If  $PRSTCap_{i,k} < SMLP \cdot (1 - CSCM_k)$ , then the *pseudo-unit* is unavailable.

10.2.3.1.4 Step 4: Initialize the operating region parameters for interval  $i \in I$  to the model parameter values:

Set  $MLP_{i,k} = MMLP_k$ .

Set  $DR_{i,k} = MDR_k$ .

Set  $DF_{i,k} = MDF_k$ .

10.2.3.1.5 Step 5: Apply the derating for the combustion turbine *resource* to the *dispatchable* region:

Calculate P so that  $CMLP_k + P \cdot CTShareDR_k \cdot MDR_k = CTCap_{i,k}$ ; and

Set  $DR_{i,k} = \min(DR_{i,k}, P \cdot MDR_k)$ .

10.2.3.1.6 Step 6: Apply the derating for the steam turbine *resource* to the duct firing and *dispatchable* regions for *pseudo-units* not operating in *single cycle mode*:

Calculate R so that  $SMLP + R \cdot STShareDR_k \cdot MDR_k = PRSTCap_{i,k}$ .

If  $R \leq 1$ , update  $DF_{i,k} = 0$ , and  $DR_{i,k} = \min(DR_{i,k}, R \cdot MDR_k)$ .

If  $R > 1$ , update  $DF_{i,k} = \min(DF_{i,k}, PRSTCap_{i,k} - SMLP - STShareDR_k \cdot MDR_k)$ .

## 10.2.4 Available Energy Laminations

10.2.4.1 The *real-time calculation engine* shall determine the *offer* quantity laminations that may be scheduled for *energy* and *operating reserve* in each operating region for interval  $i \in I$  for each *pseudo-unit*  $k \in \{1, \dots, K\}$ , subject to section 10.2.4.2, where:

10.2.4.1.1  $QMLP_{i,k}$  designates the total quantity that may be scheduled in the *minimum loading point* region;

10.2.4.1.2  $QDR_{i,k}$  designates the total quantity that may be scheduled in the *dispatchable* region; and

10.2.4.1.3  $QDF_{i,k}$  designates the total quantity that may be scheduled in the duct firing region.

10.2.4.2 The available *offered* quantity laminations shall be subject to the following conditions:

$$0 \leq QMLP_{i,k} \leq MLP_{i,k};$$

$$0 \leq QDR_{i,k} \leq DR_{i,k};$$

$$0 \leq QDF_{i,k} \leq DF_{i,k};$$

if  $QMLP_{i,k} < MLP_{i,k}$ , then the *pseudo-unit* is unavailable and  $QDR_{i,k} = QDF_{i,k} = 0$ ; and  
if  $QDR_{i,k} < DR_{i,k}$ , then  $QDF_{i,k} = 0$ .

## 10.3 Convert Physical Resource Constraints to Pseudo-Unit Constraints

10.3.1 The *real-time calculation engine* shall convert physical *resource* constraints to *pseudo-unit* constraints, where:

10.3.1.1  $PSUMin_{i,k}^q$  designates the minimum limitation on *pseudo-unit*  $k$  determined by translating constraint  $q$ . When constraint  $q$  does not provide a minimum limitation on *pseudo-unit*  $k$ , then  $PSUMin_{i,k}^q$  shall be set equal to 0;

10.3.1.2  $PSUMax_{i,k}^q$  designates the maximum limitation on *pseudo-unit*  $k$  determined by translating constraint  $q$ . When constraint  $q$  does not provide a maximum limitation on *pseudo-unit*  $k$ , then  $PSUMax_{i,k}^q$  shall be set equal to  $MLP_{i,k} + DR_{i,k} + DF_{i,k}$ ; and

10.3.1.3  $CTCmt_{i,k} \in \{0,1\}$  designates whether combustion turbine *resource*  $k \in \{1,..,K\}$  is considered committed in interval  $i \in I$ .

10.3.2 The *real-time calculation engine* shall calculate the minimum and maximum limitations, subject to section 10.3.3.1, as follows:

10.3.2.1 Minimum limitation:  $MinDG_{i,k} = \max_{q \in \{1,..,Q\}} PSUMin_{i,k}^q$

10.3.2.2 Maximum limitation:  $MaxDG_{i,k} = \min_{q \in \{1,..,Q\}} PSUMax_{i,k}^q$

where  $Q$  designates the number of constraints impacting a *combined cycle plant* that have been provided to the *real-time calculation engine*.

10.3.3 Pseudo-Unit Minimum and Maximum Constraints

10.3.3.1 *Pseudo-unit* minimum and maximum constraints shall be calculated as follows:

10.3.3.1.1  $PSUMin_{i,k} = PMin$  where  $PMin$  shall be a minimum constraint provided on *pseudo-unit*  $k \in \{1,..,K\}$  for interval  $i \in I$ ; and

10.3.3.1.2  $PSUMax_{i,k} = PMax$  where  $PMax$  shall be a maximum constraint provided on *pseudo-unit*  $k \in \{1,..,K\}$  for interval  $i \in I$ .

#### 10.3.4 Combustion Turbine Resource Minimum and Maximum Constraints

10.3.4.1 If the *pseudo-unit* is not flagged to operate in *single cycle mode*, then the combustion turbine *resource's* minimum constraint shall be converted to a *pseudo-unit* constraint as follows:

If  $CTMin < MLP_{i,k} \cdot CTShareMLP_k$ , then set

$$STMinMLP = CTMin \cdot \left( \frac{STShareMLP_k}{CTShareMLP_k} \right),$$

$$STMinDR = 0.$$

Otherwise, if  $CTMin \geq MLP_{i,k} \cdot CTShareMLP_k$ , then set

$$STMinMLP = MLP_{i,k} \cdot STShareMLP_k,$$

$$STMinDR = (CTMin - MLP_{i,k} \cdot CTShareMLP_k) \cdot \left( \frac{STShareDR_k}{CTShareDR_k} \right).$$

Therefore:

$$PSUMin_{i,k} = CTMin + STMinMLP + STMinDR.$$

10.3.4.2 If a *pseudo-unit* is flagged to operate in *single cycle mode*, then the combustion turbine *resource's* minimum constraint shall be converted to a *pseudo-unit* constraint as follows:

$$PSUMin_{i,k} = CTMin$$

10.3.4.3 If the *pseudo-unit* is not flagged to operate in *single cycle mode*, then the combustion turbine *resource's* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

If  $CTMax < MLP_{i,k} \cdot CTShareMLP_k$ , then  $PSUMax_{i,k} = 0$  and the *pseudo-unit* is unavailable.

Otherwise, calculate the value of the constraint on the steam turbine *resource* within the *minimum loading point* and *dispatchable* regions:

$$STMaxMLP = MLP_{i,k} \cdot STShareMLP_k$$

$$STMaxDR = (CTMax - MLP_{i,k} \cdot CTShareMLP_k) \cdot \left( \frac{STShareDR_k}{CTShareDR_k} \right)$$

$$PSUMax_{i,k} = CTMax + STMaxMLP + STMaxDR$$

- 10.3.4.4 If a *pseudo-unit* is flagged to operate in *single cycle mode*, then the combustion turbine *resource's* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

$$PSUMax_{i,k} = CTMax.$$

### 10.3.5 Steam Turbine Resource Minimum and Maximum Constraints

- 10.3.5.1 The *real-time calculation engine* shall convert a steam turbine *resource's* minimum constraint to a *pseudo-unit* constraints as follows:

- 10.3.5.1.1 Step 1: Identify  $A \subseteq \{1,...,K\}$ , which designates the set of *pseudo-units* to which the constraint may be allocated where *pseudo-unit*  $k \in \{1,...,K\}$  is placed in set  $A$  if and only if  $CSCM_k = 0$  and  $CTCmt_{i,k} = 1$ . If the set  $A$  is empty, then no further steps are required, otherwise proceed to Step 2.

- 10.3.5.1.2 Step 2: Determine the steam turbine *resource's* portion of the capacity for *pseudo-unit*  $k \in A$ :

$$STCap_k = QMLP_{i,k} \cdot STShareMLP_k + QDR_{i,k} \cdot STShareDR_k + QDF_{i,k}.$$

- 10.3.5.1.3 Step 3: Allocate the *STMin* constraint to each *pseudo-unit*  $k \in A$ , where *STMin* constraint shall be allocated equally to each *pseudo-unit*  $k \in A$ , where  $STPMin_k$  is limited by  $STCap_k$ .

- 10.3.5.1.4 Step 4: The steam turbine *resource* portion minimum constraint shall be converted to a *pseudo-unit* constraint, where for each *pseudo-unit*  $k \in A$ :



If  $STPMin_k < MLP_{i,k} \cdot STShareMLP_k$ , then set

$$CTMinMLP_k = STPMin_k \cdot \left( \frac{CTShareMLP_k}{STShareMLP_k} \right); \text{ and}$$

$$CTMinDR_k = 0.$$

Otherwise, if  $STPMin_k \geq MLP_{i,k} \cdot STShareMLP_k$ , then set

$$CTMinMLP_k = MLP_{i,k} \cdot CTShareMLP_k; \text{ and}$$

$$CTMinDR_k = (STPMin_k - MLP_{i,k} \cdot STShareMLP_k) \cdot \left( \frac{CTShareDR_k}{STShareDR_k} \right).$$

Therefore:

$$PSUMin_{i,k} = STPMin_k + CTMinMLP_k + CTMinDR_k.$$

10.3.5.1.4 If *pseudo-units* with sufficient steam turbine *resource* capacity are not committed, then the *real-time calculation engine* shall not convert the entire quantity of the steam turbine *resource's* minimum constraint to *pseudo-unit* constraints.

10.3.5.2 The steam turbine *resource's* maximum constraint shall be converted to a *pseudo-unit* constraint as follows:

$$PRSTMax_{i,k} = \left( \frac{STAmt_{i,k}}{\sum_{w \in \{1, \dots, K\}} STAmt_{i,w}} \right) \cdot STMax.$$

If the converted steam turbine *resource* maximum constraint limits the steam turbine *resource* portion to below its *minimum loading point*, then

$$PSUMax_{i,k} = 0.$$

Otherwise, calculate  $R$  so that  $SMLP + R \cdot STShareDR_k \cdot MDR_k = PRSTMax_{i,k}$

If  $R \leq 1$ , set  $PSUMax_{i,k} = MLP_{i,k} + \min(DR_{i,k}, R \cdot MDR_k)$ .

If  $R > 1$ , set  $PSUMax_{i,k} = MLP_{i,k} + DR_{i,k} + PRSTMax_{i,k} - SMLP - STShareDR_k \cdot MDR_k$ .

10.3.5.3 If the steam turbine *resource's* minimum and maximum constraints are equal but do not convert to equal *pseudo-unit* minimum and maximum constraints, then the steam turbine *resource* minimum

constraint conversion in section 10.3.5.1 shall be used to determine equal *pseudo-unit* minimum and maximum constraints.

## 10.4 Steam Turbine Resource Forced Outages

- 10.4.1 If the steam turbine *resource* experiences a *forced outage*, the *real-time calculation engine* shall evaluate the corresponding *pseudo-units* as being *offered* in *single cycle mode*.

## 10.5 Determination of Energy Management System MW Values for Pseudo-Units

- 10.5.1 The *real-time calculation engine* shall determine the effective *energy* management system MW value for each *pseudo-unit* from the *IESO's energy* management system MW values for the corresponding physical *resources*, where:
- 10.5.1.1  $CTTel_k$  designates the *energy* management system MW value for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
  - 10.5.1.2  $STTel$  designates the *energy* management system MW value for the steam turbine *resource*;
  - 10.5.1.3  $PSUTel_k$  designates the effective *energy* management system MW value for *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
  - 10.5.1.4  $TMLP_k$  designates the effective *minimum loading point* operating range for the time at which *energy* management system MW value was determined;
  - 10.5.1.5  $TDR_k$  designates the effective *dispatchable* region operating range for the time at which *energy* management system MW value was determined; and
  - 10.5.1.6  $TDF_{kt}$  designates the effective duct firing region operating range for the time at which *energy* management system MW value was determined.
- 10.5.2 The *real-time calculation engine* shall determine the effective *energy* management system MW values for *pseudo-units* as follows:
- 10.5.2.1 Step 1: For all combustion turbine *resources*, assign the following *energy* management system MW values to the corresponding *pseudo-unit*  $k \in \{1, \dots, K\}$ :

10.5.2.1.1  $CTMLPTel_k$ , which designates the MW value assigned to the combustion turbine *resource's* share of the *minimum loading point* region and is calculated as follows:

$$CTMLPTel_k = \min\{CTTel_k, CTShareMLP_k \cdot TMLP_k\}.$$

10.5.2.1.2  $CTDRTel_k$ , which designates the MW value assigned to the combustion turbine *resource's* share of the *dispatchable* region and is calculated as follows:

If  $CTMLPTel_k < CTTel_k$ , then set  $CTDRTel_k = \min\{(CTTel_k - CTMLPTel_k), CTShareDR_k \cdot TDR_k\}$

Otherwise, set  $CTDRTel_k = 0$ .

10.5.2.2 Step 2: Determine the maximum *energy* management system MW value for the steam turbine *resource* that may be assigned to the steam turbine *resource's* share of the *pseudo-unit's minimum loading point* and *dispatchable* regions based on the amount assigned to the combustion turbine *resource's* share of the *minimum loading point* and *dispatchable* regions. For *pseudo-unit*  $k \in \{1, \dots, K\}$ :

10.5.2.2.1  $STMLPMax_k$  designates the maximum MW value that may be assigned to the steam turbine *resource's* share of the *minimum loading point* region and is calculated as follows:

$$STMLPMax_k = CTMLPTel_k \cdot \left( \frac{STShareMLP_k}{CTShareMLP_k} \right).$$

10.5.2.2.2  $STDRMax_k$  designates the maximum MW value that may be assigned to the steam turbine *resource's* share of the *dispatchable* region and is calculated as follows:

$$STDRMax_k = CTDRTel_k \cdot \left( \frac{STShareDR_k}{CTShareDR_k} \right).$$

10.5.2.3 Step 3: Allocate the *energy* management system MW value for the steam turbine *resource* to the *minimum loading point* and *dispatchable* regions of the *pseudo-unit* in proportion to the maximum amount that may be allocated. For *pseudo-unit*  $k \in \{1, \dots, K\}$ :

10.5.2.3.1  $STMLPTel_k$  designates the MW value assigned to the steam turbine *resource's* share of the *minimum loading point* region and is calculated as follows:

$$STMLPTel_k = \min \left\{ STMLPMax_k, \left( \frac{STMLPMax_k}{\sum_{w=1..K} (STMLPMax_w + STDRMax_w)} \right) \cdot STTel \right\}$$

- 10.5.2.3.2  $STDRTel_k$  designates the MW value assigned the steam turbine *resource's* share of the *dispatchable* region and is calculated as follows

$$STDRTel_k = \min \left\{ STDRMax_k, \left( \frac{STDRMax_k}{\sum_{w=1..K} (STMLPMax_w + STDRMax_w)} \right) \cdot STTel \right\}$$

- 10.5.2.4 Step 4: Determine the remaining portion of the *energy* management system MW value for the steam turbine *resource* that is yet to be distributed ( $STRemTel$ ) as follows:

$$STRemTel = STTel - \sum_{k=1..K} (STMLPTel_k + STDRTel_k)$$

- 10.5.2.5 Step 5: Determine the maximum *energy* management system MW value for the remaining steam turbine *resource* that may be assigned to the duct firing region for the *pseudo-unit* based on whether the *pseudo-unit* is fully loaded for its *minimum loading point* and *dispatchable* regions. For *pseudo-unit*  $k \in \{1,..,K\}$ :

- 10.5.2.5.1  $STDFMax_k$  designates the maximum MW value that may be assigned to the duct firing region and is calculated as follows:

$$\text{If } (CTMLPTel_k + CTDRTel_k + STMLPTel_k + STDRTel_k) \geq TMLP_k + TDR_k, \text{ then set } STDFMax_k = TDF_k$$

Otherwise, set  $STDFMax_k = 0$ .

- 10.5.2.6 Step 6: Distribute the remaining portion of the *energy* management system MW value for the steam turbine *resource* to the duct firing regions of the *pseudo-unit* in proportion to the maximum amount that may be allocated. For *pseudo-unit*  $k \in \{1,..,K\}$ :

- 10.5.2.6.1  $STDFTel_k$  designates the MW value assigned to the duct firing region and is calculated as follows:

$$STDFTel_k = \min \left\{ STDFMax_k, \left( \frac{STDFMax_k}{\sum_{w=1..K} STDFMax_w} \right) \cdot STRemTel \right\}$$

- 10.5.2.7 Step 7: Determine the effective real-time *energy* management system MW value for the *pseudo-unit* by summing the MW values assigned to operating regions of the *pseudo-unit*. For *pseudo-unit*  $k \in \{1, \dots, K\}$ :

$$PSUTel_k = CTMLPTel_k + CTDRTel_k + STMLPTel_k + STDRTel_k + STDFTel_k.$$

## 10.6 Conversion of Pseudo-Unit Schedules to Physical Resource Schedules

- 10.6.1 For a *combined cycle plant* with  $K$  combustion turbine *resources* and one steam turbine *resource*, the *real-time calculation engine* shall compute the following *energy* and *operating reserve* schedules for interval  $i \in I$ :

- 10.6.1.1  $CTE_{i,k}$  designates the *energy* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
- 10.6.1.2  $STPE_{i,k}$  designates the *energy* schedule for the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
- 10.6.1.3  $STE_i$  designates the *energy* schedule for the steam turbine *resource*;
- 10.6.1.4  $CT10S_{i,k}$  designates the synchronized *ten-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
- 10.6.1.5  $STP10S_{i,k}$  designates the synchronized *ten-minute operating reserve* schedule for the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
- 10.6.1.6  $ST10S_i$  designates the synchronized *ten-minute operating reserve* schedule for the steam turbine *resource*;
- 10.6.1.7  $CT10N_{i,k}$  designates the non-synchronized *ten-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;
- 10.6.1.8  $STP10N_{i,k}$  designates the non-synchronized *ten-minute operating reserve* schedule for the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ;
- 10.6.1.9  $ST10N_i$  designates the non-synchronized *ten-minute operating reserve* schedule for the steam turbine *resource*;
- 10.6.1.10  $CT30R_{i,k}$  designates the *thirty-minute operating reserve* schedule for combustion turbine *resource*  $k \in \{1, \dots, K\}$ ;

- 10.6.1.11  $STP30R_{i,k}$  designates the *thirty-minute operating reserve* schedule for the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1, \dots, K\}$ ; and
- 10.6.1.12  $ST30R_i$  designates the *thirty-minute operating reserve* schedule for the steam turbine *resource*.
- 10.6.2 The *real-time calculation engine* shall determine the following *energy* and *operating reserve* schedules for *pseudo-unit*  $k \in \{1, \dots, K\}$  in interval  $i \in I$ :
- 10.6.2.1  $SE_{i,k}$  designates the total amount of *energy* scheduled and  $SE_{i,k} = SEMLP_{i,k} + SEDR_{i,k} + SEDF_{i,k}$ , where:
- 10.6.2.1.1  $SEMLP_{i,k}$  designates the portion of the schedule corresponding to the *minimum loading point* region, where  $0 \leq SEMLP_{i,k} \leq QMLP_{i,k}$ ;
- 10.6.2.1.2  $SEDR_{i,k}$  designates the portion of the schedule corresponding to the *dispatchable* region, where  $0 \leq SEDR_{i,k} \leq QDR_{i,k}$  and  $SEDR_{i,k} > 0$  only if  $SEMLP_{i,k} = QMLP_{i,k}$ ;
- 10.6.2.1.3  $SEDF_{i,k}$  designates the portion of the schedule corresponding to the duct firing region, where  $0 \leq SEDF_{i,k} \leq QDF_{i,k}$  and  $SEDF_{i,k} > 0$  only if  $SEDR_{i,k} = QDR_{i,k}$ ;
- 10.6.2.2  $S10S_{i,k}$  designates the total amount of synchronized *ten-minute operating reserve* scheduled;
- 10.6.2.3  $S10N_{i,k}$  designates the total amount of non-synchronized *ten-minute operating reserve* scheduled. If the *pseudo-unit* cannot provide *operating reserve* from its duct firing region, then  $0 \leq SE_{i,k} + S10S_{i,k} + S10N_{i,k} \leq QMLP_{i,k} + QDR_{i,k}$ ; and
- 10.6.2.4  $S30R_{i,k}$  designates the total amount of *thirty-minute operating reserve* scheduled, where  $0 \leq SE_{i,k} + S10S_{i,k} + S10N_{i,k} + S30R_{i,k} \leq QMLP_{i,k} + QDR_{i,k} + QDF_{i,k}$ .
- 10.6.3 The *real-time calculation engine* shall convert *pseudo-unit* schedules to physical *generation resource* schedules for *energy* and *operating reserve*, where:
- 10.6.3.1  $STOn \in \{0,1\}$  designates whether the steam turbine *resource* is currently online;

10.6.3.2  $CTE_{0,k}$  designates the initial *energy* schedule allocated to the combustion turbine *resource*  $k \in \{1,...,K\}$ ; and

10.6.3.3  $STPE_{0,k}$  designates the initial *energy* schedule allocated to the steam turbine *resource's* portion of *pseudo-unit*  $k \in \{1,...,K\}$ .

10.6.4 The *real-time calculation engine* shall convert *pseudo-unit* schedules to physical *resource* schedules for *energy* and *operating reserve*, as follows:

10.6.4.1 If  $SE_{i,k} \geq MLP_{i,k}$ , then:

$$CTE_{i,k} = SEMLP_{i,k} \cdot CTShareMLP_k + SEDR_{i,k} \cdot CTShareDR_k;$$

$$STPE_{i,k} = SEMLP_{i,k} \cdot STShareMLP_k + SEDR_{i,k} \cdot STShareDR_k + SEDF_{i,k};$$

$$RoomDR_{i,k} = QDR_{i,k} - SEDR_{i,k};$$

$$10SDR_{i,k} = \min(RoomDR_{i,k}, S10S_{i,k});$$

$$10NDR_{i,k} = \min(RoomDR_{i,k} - 10SDR_{i,k}, S10N_{i,k});$$

$$30RDR_{i,k} = \min(RoomDR_{i,k} - 10SDR_{i,k} - 10NDR_{i,k}, S30R_{i,k});$$

$$CT10S_{i,k} = 10SDR_{i,k} \cdot CTShareDR_k;$$

$$STP10S_{i,k} = 10SDR_{i,k} \cdot STShareDR_k + (S10S_{i,k} - 10SDR_{i,k});$$

$$CT10N_{i,k} = 10NDR_{i,k} \cdot CTShareDR_k;$$

$$STP10N_{i,k} = 10NDR_{i,k} \cdot STShareDR_k + (S10N_{i,k} - 10NDR_{i,k});$$

$$CT30R_{i,k} = 30RDR_{i,k} \cdot CTShareDR_k; \text{ and}$$

$$STP30R_{i,k} = 30RDR_{i,k} \cdot STShareDR_k + (S30R_{i,k} - 30RDR_{i,k}).$$

10.6.4.2 If  $SE_{i,k} < MLP_{i,k}$  and is on a ramp up trajectory, then the *energy* schedules for the combustion turbine *resource* and steam turbine *resource* are determined as follows:

10.6.4.3 If the steam turbine *resource* is not online, then the *pseudo-unit* schedule will be assigned to the combustion turbine *resource* as follows:

$$CTE_{i,k} = SE_{i,k}; \text{ and}$$

$$STPE_{i,k} = 0.$$

10.6.4.4 If the steam turbine *resource* is online, the incremental *pseudo-unit* schedule will be assigned to the steam turbine *resource* until the

assigned combustion turbine *resource's* and steam turbine *resource's* schedules adhere to the *pseudo-unit* model as follows:

If  $\left(\frac{STPE_{i-1,k}}{STPE_{i-1,k} + CTE_{i-1,k}}\right) < STShareMLP_k$ , then

$$CTE_{i,k} = CTE_{i-1,k},$$

$$STPE_{i,k} = SE_{i,k} - CTE_{i-1,k}.$$

Otherwise:

$$CTE_{i,k} = SE_{i,k} \cdot CTShareMLP_k; \text{ and}$$

$$STPE_{i,k} = SE_{i,k} \cdot STShareMLP_k.$$

10.6.4.5 If  $SE_{i,k} < MLP_{i,k}$  and is on a ramp-down trajectory, then the *energy* schedules for the combustion turbine *resource* and steam turbine *resource* are determined as follows:

10.6.4.6 If the steam turbine *resource* is not online, then the *pseudo-unit* schedule will be assigned to the combustion turbine *resource* as follows:

$$CTE_{i,k} = SE_{i,k}; \text{ and}$$

$$STPE_{i,k} = 0.$$

10.6.4.7 If the steam turbine *resource* is online, the *pseudo-unit* schedule will be assigned according to the *pseudo-unit* model as follows

$$CTE_{i,k} = SE_{i,k} \cdot CTShareMLP_k; \text{ and}$$

$$STPE_{i,k} = SE_{i,k} \cdot STShareMLP_k.$$

10.6.4.8 If  $SE_{i,k} < MLP_{i,k}$ , then the *operating reserve* schedules for the combustion turbine *resource* and steam turbine *resource* are as follows:

$$S10S_{i,k} = S10N_{i,k} = S30R_{i,k} = 0;$$

$$CT10S_{i,k} = 0;$$

$$STP10S_{i,k} = 0;$$

$$CT10N_{i,k} = 0;$$

$$STP10N_{i,k} = 0;$$

$$CT30R_{i,k} = 0; \text{ and}$$

$$STP30R_{i,k} = 0.$$



- 10.6.4.9 The steam turbine *resources* portion schedules from section 10.6.4.1 through 10.6.4.8 shall be summed to obtain the steam turbine *resource* schedule as follows:

$$STE_i = \sum_{k=1, \dots, K} STPE_{i,k} ;$$

$$ST10S_i = \sum_{k=1, \dots, K} STP10S_{i,k} ;$$

$$ST10N_i = \sum_{k=1, \dots, K} STP10N_{i,k} ;$$

and

$$ST30R_i = \sum_{k=1, \dots, K} STP30R_{i,k} ;$$

# 11 Pricing Formulas

## 11.1 Purpose

- 11.1.1 The *real-time calculation engine* shall calculate *locational marginal prices* using shadow prices, constraint sensitivities and marginal loss factors.

## 11.2 Sets, Indices and Parameters

- 11.2.1 The sets, indices and parameters used to calculate *locational marginal prices* are described in section 4. In addition, the following shadow prices from Pass 1 shall be used:

- 11.2.1.1  $SPEmT_{i,c,f}^1$  designates the Pass 1 shadow price for the post-contingency transmission constraint for *facility*  $f \in F$  in contingency  $c \in C$  in interval  $i$ ;
- 11.2.1.2  $SPL_i^1$  designates the Pass 1 shadow price for the *energy* balance constraint in interval  $i$ ;
- 11.2.1.3  $SPNormT_{i,f}^1$  designates the Pass 1 shadow price for the pre-contingency transmission constraint for *facility*  $f \in F$  in interval  $i$ ;

- 11.2.1.4  $SP10S_i^1$  designates the Pass 1 shadow price for the total synchronized *ten-minute operating reserve* requirement constraint in interval  $i$ ;
- 11.2.1.5  $SP10R_i^1$  designates the Pass 1 shadow price for the total *ten-minute operating reserve* requirement constraint in interval  $i$ ;
- 11.2.1.6  $SP30R_i^1$  designates the Pass 1 shadow price for the total *thirty-minute operating reserve* requirement constraint in interval  $i$ ;
- 11.2.1.7  $SPREGMin10R_{i,r}^1$  designates the Pass 1 shadow price for the minimum *ten-minute operating reserve* constraint for region  $r \in ORREG$  in interval  $i$ ;
- 11.2.1.8  $SPREGMin30R_{i,r}^1$  designates the Pass 1 shadow price for the minimum *thirty-minute operating reserve* constraint for region  $r \in ORREG$  in interval  $i$ ;
- 11.2.1.9  $SPREGMax10R_{i,r}^1$  designates the Pass 1 shadow price for the maximum *ten-minute operating reserve* constraint for region  $r \in ORREG$  in interval  $i$ ;
- 11.2.1.10  $SPREGMax30R_{i,r}^1$  designates the Pass 1 shadow price for the maximum *thirty-minute operating reserve* constraint for region  $r \in ORREG$  in interval  $i$ .

## 11.3 Locational Marginal Prices for Energy

### 11.3.1 Energy Locational Marginal Prices for Delivery Points

- 11.3.1.1 The *real-time calculation engine* shall calculate a *locational marginal price* and components for *energy* for Pass 1 and each interval  $i \in I$  for every bus  $b \in L$  and:
  - 11.3.1.1.1  $LMP_{i,b}^1$  designates the Pass 1 interval  $i$  *locational marginal price* for *energy*;
  - 11.3.1.1.2  $PRef_i^1$  designates the Pass 1 interval  $i$  *locational marginal price* for *energy* at the *reference bus*;
  - 11.3.1.1.3  $PLoss_{i,b}^1$  designates the Pass 1 interval  $i$  loss component; and
  - 11.3.1.1.4  $PCong_{i,b}^1$  designates the Pass 1 interval  $i$  congestion component.

- 11.3.1.2 The *real-time calculation engine* shall calculate an initial *locational marginal price for energy*, a *locational marginal price for energy* at the *reference bus*, a loss component and a congestion component for Pass 1 at bus  $b \in L$  in interval  $i \in I$ , as follows:

$$InitLMP_{i,b}^1 = InitPRef_i^1 + InitPLoss_{i,b}^1 + InitPCong_{i,b}^1$$

where:

$$InitPRef_i^1 = SPL_i^1;$$

$$InitPLoss_{i,b}^1 = MglLoss_{i,b} \cdot SPL_i^1;$$

and

$$InitPCong_{i,b}^1 = \sum_{f \in F_i} PreConSF_{i,f,b} \cdot SPNormT_{i,f}^1 + \sum_{c \in C} \sum_{f \in F_{i,c}} SF_{i,c,f,b} \cdot SPEmT_{i,c,f}^1.$$

- 11.3.1.3 If the initial *locational marginal price for energy* at the *reference bus* ( $InitPRef_i^1$ ) is not within the *settlement bounds* ( $EngyPrcFlr$ ,  $EngyPrcCeil$ ), then the *real-time calculation engine* shall modify the *locational marginal price for energy* at the *reference bus* as follows:

If  $InitPRef_i^1 > EngyPrcCeil$ , set  $PRef_i^1 = EngyPrcCeil$

If  $InitPRef_i^1 < EngyPrcFlr$ , set  $PRef_i^1 = EngyPrcFlr$

Otherwise, set  $PRef_i^1 = InitPRef_i^1$

- 11.3.1.4 If the initial *locational marginal price for energy* ( $InitLMP_{i,b}^1$ ) is not within the *settlement bounds* ( $EngyPrcFlr$ ,  $EngyPrcCeil$ ), then the *real-time calculation engine* shall modify the *locational marginal price for energy* as follows:

If  $InitLMP_{i,b}^1 > EngyPrcCeil$ , set  $LMP_{i,b}^1 = EngyPrcCeil$ .

If  $InitLMP_{i,b}^1 < EngyPrcFlr$ , set  $LMP_{i,b}^1 = EngyPrcFlr$ .

Otherwise, set  $LMP_{i,b}^1 = InitLMP_{i,b}^1$

- 11.3.1.5 The *real-time calculation engine* shall modify the loss component as follows:

If  $PRef_i^1 \neq InitPRef_i^1$ , set  $PLoss_{i,b}^1 = MglLoss_{i,b} \cdot PRef_i^1$

Otherwise, set  $PLoss_{i,b}^1 = InitPLoss_{i,b}^1$

- 11.3.1.6 The *real-time calculation engine* shall modify the congestion component as follows:

If  $LMP_{i,b}^1 - PRef_i^1 -$

$PLoss_{i,b}^1$  and  $InitPCong_{i,b}^1$  have the same mathematical sign, then set  $PCong_{i,b}^1 = LMP_{i,b}^1 - PRef_i^1 - PLoss_{i,b}^1$

Otherwise, set  $PCong_{i,b}^1 = 0$  and set  $PLoss_{i,b}^1 = LMP_{i,b}^1 - PRef_i^1$

### 11.3.2 Energy Locational Marginal Prices for Intertie Metering Points

- 11.3.2.1 The *real-time calculation engine* shall calculate a *locational marginal price* and components for *energy* for Pass 1 and each interval  $i \in I$  for *intertie zone* bus  $d \in D$ , where:

11.3.2.1.1  $ExtLMP_{i,d}^{PD}$  designates the *locational marginal price* for *energy* for the *dispatch hour* in which interval  $i$  falls as calculated by the *pre-dispatch calculation engine*;

11.3.2.1.2  $ICP_{i,d}^1$  designates the Pass 1 interval  $i$  *intertie congestion price*;

11.3.2.1.3  $ICP_{i,d}^{PD}$  designates the *intertie congestion price* for the *dispatch hour* in which interval  $i$  falls as calculated by the *pre-dispatch calculation engine*;

11.3.2.1.4  $IntLMP_{i,d}^1$  designates the Pass 1 interval  $i$  *intertie border price* for *energy*;

11.3.2.1.5  $ExtLMP_{i,d}^1$  designates the Pass 1 interval  $i$  *locational marginal price* for *energy*;

11.3.2.1.6  $PExtCong_{i,d}^1$  designates the Pass 1 interval  $i$  external congestion component for the *intertie congestion price*;

11.3.2.1.7  $PExtCong_{i,d}^{PD}$  designates the external congestion component for the *intertie congestion price* for the *dispatch hour* in which interval  $i$  falls as calculated by the *pre-dispatch calculation engine*;

11.3.2.1.8  $PIntCong_{i,d}^1$  designates the Pass 1 interval  $i$  internal congestion component for *energy*;

11.3.2.1.9  $PLoss_{i,d}^1$  designates the Pass 1 interval  $i$  loss component;

11.3.2.1.10  $PNISL_{i,d}^1$  designates the Pass 1 interval  $i$  net interchange scheduling limit congestion component for the *intertie congestion price*;

11.3.2.1.11  $PNISL_{i,d}^{PD}$  designates the net interchange scheduling limit congestion component for the *intertie congestion price* for the *dispatch hour* in which interval  $i$  falls as calculated by the *pre-dispatch calculation engine*; and

11.3.2.2 The *real-time calculation engine* shall calculate an *intertie border price for energy*, a *locational marginal price for energy* for the *reference bus*, a loss component and a congestion component for *energy* for Pass 1 at *intertie zone* bus  $d \in D_a$  in *intertie zone*  $a \in A$  in interval  $i \in I$ , subject to section 11.3.2.11, as follows:

$$InitIntLMP_{i,d}^1 = InitPRef_i^1 + InitPLoss_{i,d}^1 + InitPIntCong_{i,d}^1$$

where

$$InitPRef_i^1 = SPL_i^1;$$

$$InitPLoss_{i,d}^1 = MglLoss_{i,d} \cdot SPL_i^1;$$

and

$$\begin{aligned} InitPIntCong_{i,d}^1 &= \sum_{f \in F_i} PreConSF_{i,f,d} \cdot SPNormT_{i,f}^1 \\ &+ \sum_{c \in C} \sum_{f \in F_{i,c}} SF_{i,c,f,d} \cdot SPEmT_{i,c,f}^1 \end{aligned}$$

11.3.2.3 If there is import congestion in pre-dispatch such that  $ICP_{i,d}^{PD} < 0$ , the *real-time calculation engine* shall calculate an initial *locational marginal price*, an *intertie congestion price*, and the net interchange scheduling limit congestion component for the *intertie congestion price* for *energy* for Pass 1 at *intertie zone* bus  $d \in D$  in interval  $i \in I$  as follows:

$$InitExtLMP_{i,d}^1 = \min(InitIntLMP_{i,d}^1, ExtLMP_{i,d}^{PD});$$

$$InitICP_{i,d}^1 = InitExtLMP_{i,d}^1 - InitIntLMP_{i,d}^1;$$

where:

If  $InitExtLMP_{i,d}^1 = InitIntLMP_{i,d}^1$ , then  $InitICP_{i,d}^1 = 0$  and  $InitPNISL_{i,d}^1 = 0$ ;

and

If  $InitExtLMP_{i,d}^1 = ExtLMP_{i,d}^{PD}$ , then  $InitICP_{i,d}^1$  and  $InitPNISL_{i,d}^1$  shall be prorated based on their pre-dispatch magnitudes so that their sum equals the effective real-time *intertie congestion price*.

- 11.3.2.4 If there is export congestion in pre-dispatch such that  $ICP_{i,d}^{PD} > 0$ , the *real-time calculation engine* shall calculate an initial *locational marginal price*, an *intertie congestion price*, and the net interchange scheduling limit congestion component for the *intertie congestion price for energy* for Pass 1 at *intertie zone* bus  $d \in D$  in interval  $i \in I$  as follows:

$$InitExtLMP_{i,d}^1 = InitIntLMP_{i,d}^1 + InitICP_{i,d}^1$$

where:

$$InitICP_{i,d}^1 = InitPExtCong_{i,d}^1 + InitPNISL_{i,d}^1;$$

$$InitPExtCong_{i,d}^1 = PExtCong_{i,d}^{PD};$$

and

$$InitPNISL_{i,d}^1 = PNISL_{i,d}^{PD}.$$

- 11.3.2.5 If there is no *intertie* congestion in pre-dispatch such that  $ICP_{i,d}^{PD} = 0$  or an *intertie zone* is out-of-service in real-time, then the *real-time calculation engine* shall calculate an initial *locational marginal price*, an *intertie congestion price*, and the net interchange scheduling limit congestion component for the *intertie congestion price for energy* for Pass 1 at *intertie zone* bus  $d \in D$  in interval  $i \in I$  as follows:

$$InitExtLMP_{i,d}^1 = InitIntLMP_{i,d}^1 + InitICP_{i,d}^1$$

where

$$InitICP_{i,d}^1 = InitPExtCong_{i,d}^1 + InitPNISL_{i,d}^1 = 0$$

$$InitPExtCong_{i,d}^1 = PExtCong_{i,d}^{PD};$$

and

$$InitPNISL_{i,d}^1 = PNISL_{i,d}^{PD}.$$

- 11.3.2.6 If the *intertie border price for energy* ( $InitIntLMP_{i,d}^1$ ) is not within the *settlement bounds* ( $EngyPrcFlr$ ,  $EngyPrcCeil$ ), then the *real-time*

*calculation engine* shall modify the *intertie border price* for *energy*, and its components, as follows:

- 11.3.2.6.1 The initial *locational marginal price* for the *reference bus* ( $InitPRef_i^1$ ) shall be modified as per section 11.3.1.3;
  - 11.3.2.6.2 The initial *intertie border price* ( $InitIntLMP_{i,d}^1$ ) shall be modified as per section 11.3.1.4, where  $InitLMP_{i,b}^1 = InitIntLMP_{i,d}^1$ ;
  - 11.3.2.6.3 The initial loss component ( $InitPLoss_{i,d}^1$ ) shall be modified as per section 11.3.1.5; and
  - 11.3.2.6.4 The initial internal congestion component ( $InitPIntCong_{i,d}^1$ ) shall be modified as per section 11.3.1.6, where  $InitPCong_{i,b}^1 = InitPIntCong_{i,d}^1$ .
- 11.3.2.7 If the initial *locational marginal price* for *energy* ( $InitExtLMP_{i,d}^1$ ) is not within the *settlement* bounds ( $EngyPrcFlr$ ,  $EngyPrcCeil$ ), then the *real-time calculation engine* shall modify the *locational marginal price* for *energy*, as follows:
- If  $InitExtLMP_{i,d}^1 > EngyPrcCeil$ , set  $ExtLMP_{i,d}^1 = EngyPrcCeil$ .
- If  $InitExtLMP_{i,d}^1 < EngyPrcFlr$ , set  $ExtLMP_{i,d}^1 = EngyPrcFlr$ .
- Otherwise, set  $ExtLMP_{i,d}^1 = InitExtLMP_{i,d}^1$ .
- 11.3.2.8 If the modified *locational marginal price* for *energy* ( $ExtLMP_{i,d}^1$ ) determined in section 11.3.2.7 is equal to the *intertie border price* for *energy* ( $IntLMP_{i,d}^1$ ), then the *real-time calculation engine* shall modify the external congestion component for the *intertie congestion price* and net interchange scheduling limit congestion component for the *intertie congestion price*, as follows:
- If  $ExtLMP_{i,d}^1 = IntLMP_{i,d}^1$ , set  $PExtCong_{i,d}^1 = 0$  and  $PNISL_{i,d}^1 = 0$ .
- 11.3.2.9 If the modified *locational marginal price* for *energy* ( $ExtLMP_{i,d}^1$ ) determined in section 11.3.2.7 is not equal to the *intertie border price* for *energy* ( $IntLMP_{i,d}^1$ ), then the *real-time calculation engine* shall modify the external congestion component for the *intertie congestion*

price and net interchange scheduling limit congestion component for the *intertie congestion price*, as follows:

If  $ExtLMP_{i,d}^1 \neq IntLMP_{i,d}^1$ , then set

$$PNISL_{i,d}^1 = (ExtLMP_{i,d}^1 - IntLMP_{i,d}^1) \cdot \left( \frac{InitPNISL_{i,d}^1}{InitPNISL_{i,d}^1 + InitPExtCong_{i,d}^1} \right).$$

If  $PNISL_{i,d}^1 > NISLPen$ , then set  $PNISL_{i,d}^1 = NISLPen$ ;

If  $PNISL_{i,d}^1 < (-1) \cdot NISLPen$ , then set  $PNISL_{i,d}^1 = (-1) \cdot NISLPen$ ; and

Set  $PExtCong_{i,d}^1 = ExtLMP_{i,d}^1 - IntLMP_{i,d}^1 - PNISL_{i,d}^1$

- 11.3.2.10 The *real-time calculation engine* shall calculate the *intertie congestion price* as follows:

$$ICP_{i,d}^1 = PExtCong_{i,d}^1 + PNISL_{i,d}^1.$$

- 11.3.2.11 The *locational marginal price* for *energy* calculated by the *real-time calculation engine* shall be the same for all *boundary entity resource* buses at the same *intertie zone*. *Intertie* transactions associated with the same *boundary entity resource* bus, but specified as occurring at different *intertie zones*, subject to phase shifter operation, shall be modelled as flowing across independent paths. Pricing of these transactions shall utilize shadow prices associated with the internal transmission constraints, *intertie* limits and transmission losses applicable to the path associated to the relevant *intertie zone*.

### 11.3.3 Zonal Prices for Energy

- 11.3.3.1 The *real-time calculation engine* shall calculate the zonal price for *energy* and its components for Pass 1 and each interval  $i \in I$ , the *energy price* for *virtual transaction zone*  $m \in M$ , as follows:

$$VZonalP_{i,m}^1 = PRef_i^1 + VZonalP_{i,m}^1 + VZonalPCong_{i,m}^1$$

where:

$$VZonalP_{i,m}^1 = \sum_{b \in L_m^{VIRT}} WF_{i,m,b}^{VIRT} \cdot P_{i,b}^1$$

and



$$VZonalPCong_{i,m}^1 = \sum_{b \in L_m^{VIRT}} WF_{i,m,b}^{VIRT} \cdot PCong_{i,b}^1$$

- 11.3.3.2 The *real-time calculation engine* shall calculate the zonal price for *energy* and its components for Pass 1 and each interval  $i \in I$  for *non-dispatchable load* zone  $y \in Y$ , as follows:

$$ZonalP_{i,y}^1 = PRef_i^1 + ZonalP_{i,y}^{Loss1} + ZonalPCong_{i,y}^1$$

where:

$$ZonalP_{i,y}^{Loss1} = \sum_{b \in L_y^{NDL}} WF_{i,y,b}^{NDL} \cdot P_{i,b}^{Loss1}$$

and

$$ZonalPCong_{i,y}^1 = \sum_{b \in L_y^{NDL}} WF_{i,y,b}^{NDL} \cdot PCong_{i,b}^1$$

- 11.3.3.3 The *Ontario zonal price* is calculated per section 11.3.3.2 where the *non-dispatchable load* zone is comprised of all *non-dispatchable loads* within Ontario.

#### 11.3.4 Pseudo-Unit Pricing

- 11.3.4.1 The *real-time calculation engine* shall calculate a *locational marginal price* and components for *energy* for Pass 1 and each interval  $i \in I$  for every *pseudo-unit*  $k \in \{1, \dots, K\}$ , where:

11.3.4.1.1  $CTMglLoss_{i,k}^1$  designates the marginal loss factor for the combustion turbine *resource* identified by *pseudo-unit*  $k$  for each interval  $i$  in Pass 1;

11.3.4.1.2  $STMglLoss_{i,k}^D$  designates the marginal loss factor for the steam turbine *resource* identified by *pseudo-unit*  $k$  for each interval  $i$  in Pass 1;

11.3.4.1.3  $CTPreConSF_{i,f,k}$  designates the pre-contingency sensitivity factor for the combustion turbine *resource* identified by *pseudo-unit*  $k$  on *facility*  $f$  during interval  $i$  under pre-contingency conditions;

11.3.4.1.4  $STPreConSF_{i,f,k}$  designates the pre-contingency sensitivity factor for the steam turbine *resource*

identified by *pseudo-unit k* on *facility f* during interval *i* under pre-contingency conditions;

11.3.4.1.5  $CTSF_{i,c,f,k}$  designates the post-contingency sensitivity factor for the combustion turbine *resource* identified by *pseudo-unit k* on *facility f* during interval *i* under post-contingency conditions for contingency *c*; and

11.3.4.1.6  $STSF_{i,c,f,k}$  designates the post-contingency sensitivity factor for the steam turbine *resource* identified by *pseudo-unit k* on *facility f* during interval *i* under post-contingency conditions for contingency *c*.

11.3.4.2 The *real-time calculation engine* shall calculate an initial *locational marginal price for energy*, a *locational marginal price for energy* at the *reference bus*, a loss component and a congestion component for Pass 1 and each interval *i* for every *pseudo-unit k*  $k \in \{1, \dots, K\}$ , as follows:

$$InitLMP_{i,k}^1 = InitPRef_i^1 + InitPLoss_{i,k}^1 + InitPCong_{i,k}^1$$

where:

$$InitPRef_i^1 = SPL_i^1;$$

$$InitPLoss_{i,k}^1 = MglLoss_{i,k}^1 \cdot SPL_i^1;$$

and

$$InitPCong_{i,k}^1 = \sum_{f \in F_i} PreConSF_{i,f,k} \cdot SPNormT_{i,f}^1 + \sum_{c \in C} \sum_{f \in F_{i,c}} SF_{i,c,f,k} \cdot SPEmT_{i,c,f}^1$$

11.3.4.3 If *pseudo-unit k*  $k \in \{1, \dots, K\}$  is scheduled within its *minimum loading point* range or not scheduled at all, its marginal loss and sensitivity factors shall be:

$$MglLoss_{i,k}^1 = CTShareMLP_k \cdot CTMglLoss_{i,k}^1 + STShareMLP_k \cdot STMglLoss_{i,k}^1$$

$$PreConSF_{i,f,k} = CTShareMLP_k \cdot CTPreConSF_{i,f,k} + STShareMLP_k \cdot STPreConSF_{i,f,k}$$

$$SF_{i,c,f,k} = CTShareMLP_k \cdot CTSF_{i,c,f,k} + STShareMLP_k \cdot STSF_{i,c,f,k}$$

- 11.3.4.4 If *pseudo-unit*  $k \in \{1, \dots, K\}$  is scheduled within its *dispatchable* region, its marginal loss and sensitivity factors shall be:

$$MglLoss_{i,k}^1 = CTShareDR_k \cdot CTMglLoss_{i,k}^1 + STShareDR_k \cdot STMglLoss_{i,k}^1$$

$$PreConSF_{i,f,k} = CTShareDR_k \cdot CTPreConSF_{i,f,k} + STShareDR_k \cdot STPreConSF_{i,f,k}$$

$$SF_{i,c,f,k} = CTShareDR_k \cdot CTSF_{i,c,f,k} + STShareDR_k \cdot STSF_{i,c,f,k}$$

- 11.3.4.5 If *pseudo-unit*  $k \in \{1, \dots, K\}$  is scheduled within its duct firing region, its marginal loss and sensitivity factors shall be:

$$MglLoss_{i,k}^1 = STMglLoss_{i,k}^1$$

$$PreConSF_{i,f,k} = STPreConSF_{i,f,k}$$

$$SF_{i,c,f,k} = STSF_{i,c,f,k}$$

## 11.4 Locational Marginal Prices for Operating Reserve

### 11.4.1 Operating Reserve Locational Marginal Prices for Delivery Points

- 11.4.1.1 The *real-time calculation engine* shall calculate *locational marginal prices* and components for *operating reserve* for Pass 1 and each interval  $i$  for a *delivery point* associated with the *dispatchable generation resource* or *dispatchable load* bus  $b \in B$ , where:

- 11.4.1.1.1  $L30RP_{i,b}^1$  designates the Pass 1 interval  $i$  *locational marginal price* for *thirty-minute operating reserve*;

- 11.4.1.1.2  $P30RRef_i^1$  designates the Pass 1 interval  $i$  *locational marginal price* for *thirty-minute operating reserve* at the *reference bus*;

- 11.4.1.1.3  $P30RCong_{i,b}^1$  designates the Pass 1 interval  $i$  congestion component for *thirty-minute operating reserve*;

- 11.4.1.1.4  $L10NP_{i,b}^1$  designates the Pass 1 interval  $i$  *locational marginal price* for non-synchronized *ten-minute operating reserve*;

- 11.4.1.1.5  $P10NRef_i^1$  designates the Pass 1 interval  $i$  *locational marginal price* for non-synchronized *ten-minute operating reserve* at the *reference bus*;

- 11.4.1.1.6  $P10NCong_{i,b}^1$  designates the Pass 1 interval  $i$  congestion component for non-synchronized *ten-minute operating reserve*;
  - 11.4.1.1.7  $L10SP_{i,b}^1$  designates the Pass 1 interval  $i$  *locational marginal price* for synchronized *ten-minute operating reserve*;
  - 11.4.1.1.8  $P10SRef_i^1$  designates the Pass 1 interval  $i$  *locational marginal price* for synchronized *ten-minute operating reserve* at the *reference bus*;
  - 11.4.1.1.9  $P10SCong_{i,b}^1$  designates the Pass 1 interval  $i$  congestion component for synchronized *ten-minute operating reserve*; and
  - 11.4.1.1.10  $ORREG_b \subseteq ORREG$  as the subset of  $ORREG$  consisting of regions that include bus  $b$ .
- 11.4.1.2 The *real-time calculation engine* shall calculate an initial *locational marginal price*, a *locational marginal price* at the *reference bus*, and congestion components for Pass 1 for a *delivery point* associated with the *dispatchable generation resource* or *dispatchable load* at bus  $b \in B$  in interval  $i \in I$  for each class of *operating reserve*, as follows:

$$InitL30RP_{i,b}^1 = InitP30RRef_i^1 + InitP30RCong_{i,b}^1$$

where:

$$InitP30RRef_i^1 = SP30R_i^1$$

and

$$\begin{aligned} InitP30RCong_{i,b}^1 &= \sum_{r \in ORREG_b} SPREGMin30R_{i,r}^1 \\ &+ \sum_{r \in ORREG_b} SPREGMax30R_{i,r}^1 \end{aligned}$$

$$InitL10NP_{i,b}^1 = InitP10NRef_i^1 + InitP10NCong_{i,b}^1$$

where:

$$InitP10NRef_i^1 = SP10R_i^1 + SP30R_i^1$$

and

$$\begin{aligned} InitP10NCong_{i,b}^1 &= \sum_{r \in ORREG_b} (SPREGMin10R_{i,r}^1 \\ &\quad + SPREGMin30R_{i,r}^1) \\ &\quad + \sum_{r \in ORREG_b} (SPREGMax10R_{i,r}^1 \\ &\quad + SPREGMax30R_{i,r}^1) \end{aligned}$$

$$InitL10SP_{i,b}^1 = InitP10SRef_i^1 + InitP10SCong_{i,b}^1$$

where:

$$InitP10SRef_i^1 = SP10S_i^1 + SP10R_i^1 + SP30R_i^1$$

and

$$\begin{aligned} InitP10SCong_{i,b}^1 &= \sum_{r \in ORREG_b} (SPREGMin10R_{i,r}^1 \\ &\quad + SPREGMin30R_{i,r}^1) \\ &\quad + \sum_{r \in ORREG_b} (SPREGMax10R_{i,r}^1 \\ &\quad + SPREGMax30R_{i,r}^1) \end{aligned}$$

- 11.4.1.3 If the initial *locational marginal price* at the *reference bus* ( $InitP30RRef_i^1$ ,  $InitP10NRef_i^1$  or  $InitP10SRef_i^1$ ) is not within the *settlement bounds* ( $ORPrcFlr$ ,  $ORPrcCeil$ ), then the *real-time calculation engine* shall modify the *locational marginal price* at the *reference bus* for each class of *operating reserve* as follows:

If  $InitP30RRef_i^1 > ORPrcCeil$ , set  $P30RRef_i^1 = ORPrcCeil$ ;

If  $InitP30RRef_i^1 < ORPrcFlr$ , set  $P30RRef_i^1 = ORPrcFlr$ ;

Otherwise, set  $P30RRef_i^1 = InitP30RRef_i^1$ .

If  $InitP10NRef_i^1 > ORPrcCeil$ , set  $P10NRef_i^1 = ORPrcCeil$

If  $InitP10NRef_i^1 < ORPrcFlr$ , set  $P10NRef_i^1 = ORPrcFlr$

Otherwise, set  $P10NRef_i^1 = InitP10NRef_i^1$

If  $InitP10SRef_i^1, ORPrcFlr > ORPrcCeil$ , set  $P10SRef_i^1 = ORPrcCeil$

If  $InitP10SRef_i^1, ORPrcFlr < ORPrcFlr$ , set  $P10SRef_i^1 = ORPrcFlr$

Otherwise, set  $P10SRef_i^1 = InitP10SRef_i^1$

- 11.4.1.4 If the initial *locational marginal price* ( $InitL30RP_{i,b}^1$ ,  $InitL10NP_{i,b}^1$ , or  $InitL10SP_{i,b}^1$ ) is not within the *settlement* bounds ( $ORPrcFlr$ ,  $ORPrcCeil$ ), then the *real-time calculation engine* shall modify the *locational marginal price* for each class of *operating reserve* as follows:

If  $InitL30RP_{i,b}^1 > ORPrcCeil$ , set  $L30RP_{i,b}^1 = ORPrcCeil$ ;

If  $InitL30RP_{i,b}^1 < ORPrcFlr$ , set  $L30RP_{i,b}^1 = ORPrcFlr$ ;

Otherwise, set  $L30RP_{i,b}^1 = InitL30RP_{i,b}^1$ .

If  $InitL10NP_{i,b}^1 > ORPrcCeil$ , set  $L10NP_{i,b}^1 = ORPrcCeil$ ;

If  $InitL10NP_{i,b}^1 < ORPrcFlr$ , set  $L10NP_{i,b}^1 = ORPrcFlr$ ;

Otherwise, set  $L10NP_{i,b}^1 = InitL10NP_{i,b}^1$ .

If  $InitL10SP_{i,b}^1 > ORPrcCeil$ , set  $L10SP_{i,b}^1 = ORPrcCeil$ ;

If  $InitL10SP_{i,b}^1 < ORPrcFlr$ , set  $L10SP_{i,b}^1 = ORPrcFlr$ ;

Otherwise, set  $L10SP_{i,b}^1 = InitL10SP_{i,b}^1$ .

- 11.4.1.5 If the initial *locational marginal price* ( $InitL30RP_{i,b}^1$ ,  $InitL10NP_{i,b}^1$ , or  $InitL10SP_{i,b}^1$ ) is not within the *settlement* bounds ( $ORPrcFlr$ ,  $ORPrcCeil$ ), then the *real-time calculation engine* shall modify the congestion component for each class of *operating reserve* as follows:

Set  $P30RCong_{i,b}^1 = L30RP_{i,b}^1 - P30RRef_i^1$ ;

Set  $P10NCong_{i,b}^1 = L10NP_{i,b}^1 - P10NRef_i^1$ ; and

Set  $P10SCong_{i,b}^1 = L10SP_{i,b}^1 - P10SRef_i^1$ .

## 11.4.2 Operating Reserve Locational Marginal Prices for Intertie Metering Points

11.4.2.1 The *real-time calculation engine* shall calculate *locational marginal prices* and components for *operating reserve* for Pass 1 and each interval  $i \in I$ , for *intertie zone* bus  $d \in D$ , where:

- 11.4.2.1.1  $ExtL30RP_{i,d}^1$  designates the Pass 1 interval  $i$  *locational marginal price* for *thirty-minute operating reserve*;
- 11.4.2.1.2  $ExtL30RP_{i,d}^{PD}$  designates the *locational marginal price* for *thirty-minute operating reserve* for the *dispatch hour* in which interval  $i$  falls as calculated by the *pre-dispatch calculation engine*;
- 11.4.2.1.3  $P30RExtCong_{i,d}^1$  designates the Pass 1 interval  $i$  congestion component for *thirty-minute operating reserve*;
- 11.4.2.1.4  $P30RExtCong_{i,d}^{PD}$  designates the *intertie congestion* component for *thirty-minute operating reserve* for the *dispatch hour* in which interval  $i$  falls as calculated by the *pre-dispatch calculation engine*;
- 11.4.2.1.5  $ExtL10NP_{i,d}^1$  designates the Pass 1 interval  $i$  *locational marginal price* for non-synchronized *ten-minute operating reserve*;
- 11.4.2.1.6  $ExtL10NP_{i,d}^{PD}$  designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* for the *dispatch hour* in which interval  $i$  falls as calculated by the *pre-dispatch calculation engine*;
- 11.4.2.1.7  $P30RRef_i^1$  designates the Pass 1 interval  $i$  *locational marginal price* for *thirty-minute operating reserve* at the *reference bus*;
- 11.4.2.1.8  $P30RIntCong_{i,d}^1$  designates the Pass 1 interval  $i$  internal congestion component for *thirty-minute operating reserve*;
- 11.4.2.1.9  $P10NRef_i^1$  designates the Pass 1 interval  $i$  *locational marginal price* for non-synchronized *ten-minute operating reserve* at the *reference bus*;

- 11.4.2.1.10  $P10NIntCong_{i,d}^1$  designates the Pass 1 interval  $i$  internal congestion component for non-synchronized *ten-minute operating reserve*;
- 11.4.2.1.11  $P10NExtCong_{i,d}^1$  designates the Pass 1 interval  $i$  *intertie* congestion component for non-synchronized *ten-minute operating reserve*; and
- 11.4.2.1.12  $P10NExtCong_{i,d}^{PD}$  designates the *intertie* congestion component for non-synchronized *ten-minute operating reserve* for the *dispatch hour* in which interval  $i$  falls as calculated by the *pre-dispatch calculation engine*.

11.4.2.2 The *real-time calculation engine* shall calculate an initial *locational marginal price*, a *locational marginal price* at the *reference bus*, an internal congestion component and an *intertie* congestion component for Pass 1 at *intertie zone bus*  $d \in D$  in interval  $i \in I$ , for each class of *operating reserve*, subject to section 11.4.2.8, as follows:

$$InitIntL30RP_{i,d}^1 = InitP30RRef_i^1 + InitP30RIntCong_{i,d}^1$$

where:

$$InitP30RRef_i^1 = SP30R_i^1$$

and

$$InitP30RIntCong_{i,d}^1 = \sum_{r \in ORREG_d} SPREGMin30R_{i,r}^1 + \sum_{r \in ORREG_d} SPREGMax30R_{i,r}^1$$



$$InitIntL10NP_{i,d}^1 = InitP10NRef_i^A + InitP10NIntCong_{i,d}^1$$

where:

$$InitP10NRef_i^A = SP10R_i^1 + SP30R_i^1$$

and

$$\begin{aligned} InitP10NIntCong_{i,d}^1 &= \sum_{r \in ORREG_d} (SPREGMin10R_{i,r}^1 \\ &+ SPREGMin30R_{i,r}^1) \\ &+ \sum_{r \in ORREG_d} (SPREGMax10R_{i,r}^1 \\ &+ SPREGMax30R_{i,r}^1) \end{aligned}$$

11.4.2.3 The *real-time calculation engine* shall calculate initial *locational marginal prices*, and its components for Pass 1 at *intertie zone* bus  $d \in D$  in interval  $i \in I$  for each class of *operating reserve* as follows:

11.4.2.3.1 If the *intertie* is import congested in pre-dispatch ( $P30RExtCong_{i,d}^{PD} < 0$  or  $P10NExtCong_{i,d}^{PD} < 0$ ), then the prices and components are determined in accordance with section 11.4.2.4;

11.4.2.3.2 If the *intertie* is not import congestion in pre-dispatch ( $P30RExtCong_{i,d}^{PD} \geq 0$  or  $P10NExtCong_{i,d}^{PD} \geq 0$ ) or if an *intertie zone* is out-of-service, then the prices and components are determined in accordance with section 11.4.2.5.

11.4.2.4 The *real-time calculation engine* shall calculate an initial *locational marginal price* and an external congestion component for the *intertie congestion price* for each class of *operating reserve* for Pass 1 at *intertie zone* bus  $d \in D$  in interval  $i \in I$  as follows:

$$InitExtL30RP_{i,d}^1 = \min(InitIntL30RP_{i,d}^1, ExtL30RP_{i,d}^{PD});$$

and

$$InitP30RExtCong_{i,d}^1 = InitExtL30RP_{i,d}^1 - InitIntL30RP_{i,d}^1.$$

$$InitExtL10NP_{i,d}^1 = \min(InitIntL10NP_{i,d}^1, ExtL10NP_{i,d}^{PD});$$

and

$$InitP10NExtCong_{i,d}^1 = InitExtL10NP_{i,d}^1 - InitIntL10NP_{i,d}^1.$$

- 11.4.2.5 The *real-time calculation engine* shall calculate an initial *locational marginal price* and an external congestion component for the *intertie congestion price* for each class of *operating reserve* for Pass 1 at *intertie zone bus*  $d \in D$  in interval  $i \in I$  as follows:

$$InitExtL30RP_{i,d}^1 = InitIntL30RP_{i,d}^1;$$

and

$$InitP30RExtCong_{i,d}^1 = 0.$$

$$InitExtL10NP_{i,d}^1 = InitIntL10NP_{i,d}^1;$$

and

$$InitP10NExtCong_{i,d}^1 = 0.$$

- 11.4.2.6 If the initial *locational marginal price* ( $InitExtL30RP_{i,b}^1$ ) is not within the *settlement bounds* ( $ORPrCflr$ ,  $ORPrCCeil$ ), then the *real-time calculation engine* shall modify the *locational marginal price*, the *locational marginal price at the reference bus*, and the congestion components for *thirty-minute operating reserve* as follows:

$$IntL30R = InitP30RRef_i^1 + InitP30RIntCong_{i,d}^1$$

If  $InitP30RRef_i^1 > ORPrCCeil$ , set  $P30RRef_i^1 = ORPrCCeil$ ;

If  $InitP30RRef_i^1 < ORPrCflr$ , set  $P30RRef_i^1 = ORPrCflr$ ;

Otherwise, set  $P30RRef_i^1 = InitP30RRef_i^1$ ;

Set  $P30RIntCong_{i,d}^1 = ExtL30RP_{i,b}^1 - P30RRef_i^1$ ;

If  $InitExtL30RP_{i,b}^1 > ORPrCCeil$ , set  $ExtL30RP_{i,b}^1 = ORPrCCeil$ ;

If  $InitExtL30RP_{i,b}^1 < ORPrCflr$ , set  $ExtL30RP_{i,b}^1 = ORPrCflr$ ;

Otherwise,  $ExtL30RP_{i,b}^1 = InitExtL30RP_{i,b}^1$ ; and

Set  $P30RExtCong_{i,d}^1 = ExtL30RP_{i,b}^1 - P30RRef_i^1 - P30RIntCong_{i,d}^1$

- 11.4.2.7 If the initial *locational marginal price* ( $InitExtL10NP_{i,d}^1$ ) is not within the *settlement bounds* ( $ORPrCflr$ ,  $ORPrCCeil$ ), then the *real-time calculation engine* shall modify the *locational marginal price*, the *locational marginal price at the reference bus*, and the congestion components for *ten-minute operating reserve* as follows:

$$IntL10N = InitP10NRef_i^1 + InitP10NIntCong_{i,d}^1$$

If  $InitP10NRef_i^1 > ORPrCCeil$ , set  $P10NRef_i^1 = ORPrCCeil$ ;

If  $InitP10NRef_i^1 < ORPrCflr$ , set  $P10NRef_i^1 = ORPrCflr$ ;

Otherwise,  $P10NRef_i^1 = InitP10NRef_i^1$ ; and  
Set  $P10NIntCong_{i,d}^1 = L10NP_{i,b}^1 - P10NRef_i^1$   
If  $InitExtL10NP_{i,b}^1 > ORPrCceil$ , set  $ExtL10NP_{i,b}^1 = ORPrCceil$ ;  
If  $InitExtL10NP_{i,b}^1 < ORPrCflr$ , set  $ExtL10NP_{i,b}^1 = ORPrCflr$ ;  
Otherwise,  $ExtL30RP_{i,b}^1 = InitExtL10NP_{i,b}^1$ ; and  
Set  $P10NExtCong_{i,d}^1 = ExtL10NP_{i,b}^1 - P10NRef_i^1 - P10NIntCong_{i,d}^1$

- 11.4.2.8 The *locational marginal price* calculated by the *real-time calculation engine* shall be the same for all *boundary entity resource* buses at the same *intertie zone*. Reserve imports associated with the same *boundary entity resource* bus, but specified as occurring at a different *intertie zone*, subject to phase shifter operation, shall be modelled as flowing across independent paths. Pricing of these reserve imports shall utilize shadow prices associated with *intertie* limits and regional minimum and maximum *operating reserve* requirements applicable to the path associated to the relevant *intertie zone*.

## 11.5 Pricing for Islanded Nodes

- 11.5.1 For *non-quick start resources* that are not connected to the *main island*, the *real-time calculation engine* shall use the following reconnection logic where enabled by the *IESO* in the order set out below to calculate the *locational marginal prices* for *energy*:
- 11.5.1.1 Determine the connection paths over open switches that connect the *non-quick start resource* to the *main island*;
  - 11.5.1.2 Determine the priority rating for each connection path identified based on a weighted sum of the base voltage over all open switches used by the reconnection path and the MW ratings of the newly connected branches; and
  - 11.5.1.3 Select the reconnection path with the highest priority rating, breaking ties arbitrarily.
- 11.5.2 For all (i) *resources* other than those specified in section 11.5.1 not connected to the *main island*; (ii) *non-quick start resources* where a price was not able to be determined in accordance with section 11.5.1; the *real-time calculation engine* shall use the following logic in the order set out below to calculate *locational*

*marginal prices for energy*, using a node-level and *facility*-level substitution list determined by the *IESO*:

- 11.5.2.1 Use the *locational marginal price for energy* at a node in the node-level substitution list where defined and enabled by the *IESO*, provided such node is connected to the *main island*;
- 11.5.2.2 If no such nodes are identified, use the average *locational marginal price for energy* of all nodes at the same voltage level within the same *facility* that are connected to the *main island*;
- 11.5.2.3 If no such nodes are identified, use the average *locational marginal price for energy* of all nodes within the same *facility* that are connected to the *main island*;
- 11.5.2.4 If no such nodes are identified, use the average *locational marginal price for energy* of all nodes from another *facility* that is connected to the *main island*, as determined by the *facility*-level substitution list where defined and enabled by the *IESO*; and
- 11.5.2.5 If a price is unable to be determined in accordance with sections 11.5.2.1 through 11.5.2.4, use the *locational marginal price for energy* for the *reference bus*.

# Appendix 7.7 – Radial Intertie Transactions

## 1.1 Applicable Configurations

- 1.1.1 An electricity *generation resource* associated with a *generation facility* that is connected electrically over a *radial intertie* to a neighbouring *control area* may only provide electricity or any *physical service* for delivery out of the *integrated power system* if it is, with the approval of the *IESO*, operating such *generation resource* in a *segregated mode of operation*.

## 1.2 Dispatch Data

- 1.2.1 A *market participant* that intends for a *generation resource* to operate in a *segregated mode of operation* shall maintain *dispatch data* that was submitted for that *generation resource* for each *dispatch hour* during which a *generation resource* will or is intended to operate in *segregated mode of operation*. The *market participant* may revise the applicable *dispatch data* in accordance with the timelines for submission of revised *dispatch data* specified in MR Ch.7 ss.3.2 and 3.3.

- 1.2.2 Notwithstanding the provisions of MR Ch.7 s.3.3, if the *IESO*:

1.2.2.1 denies a *Request for Segregation*; or

1.2.2.2 revokes its approval to operate a *generation resource* in a *segregated mode of operation* or terminates the operation of a *generation resource* in a *segregated mode of operation* in accordance with section 1.3.6,

the *IESO* shall permit new or revised *dispatch data* to be submitted to the *IESO* in respect of the *generation resource* for the *dispatch hours* to which such denied request pertains.

## 1.3 Scheduling & Scheduling Approval

- 1.3.1 A *registered market participant* shall, within the time required by section 1.3.3, submit a *Request for Segregation* to the *IESO* for approval to operate its *generation resource* in a *segregated mode of operation* and shall submit an *outage* request, in accordance with the provisions specified in MR Ch.5 s.6.4 and the applicable *market manual*, to the *IESO* for the *generation resources* intended to operate in a *segregated mode of operation*. The *registered market participant* shall make such a *Request for Segregation* in accordance with the applicable *market manual* and the information contained in such *Request for Segregation* shall include, but not be limited to:
- 1.3.1.1 the time at which operation in a *segregated mode of operation* is intended to commence;
  - 1.3.1.2 the length of time that the applicable *generation resources* are intended to operate in a *segregated mode of operation*; and
  - 1.3.1.3 a list of the *generation resources* that are intended to operate in a *segregated mode of operation*.
- 1.3.2 If a *registered market participant* wishes to revise the contents of a *Request for Segregation* it shall submit a new *Request for Segregation* and shall submit a new *outage* request to the *IESO* in accordance with section 1.3.1.
- 1.3.3 If a *Request for Segregation* requires an *outage* to equipment that the *IESO* has designated as critical in accordance with the applicable *market manual*, the request shall be made by 8:00 EPT on the day prior to the relevant *dispatch day*, unless otherwise agreed by the *IESO*. If a *Request for Segregation* does not require an *outage* to such equipment, the *registered market participant* shall make the *Request for Segregation* by 9:00 EPT on the day prior to the relevant *dispatch day* for inclusion in the *day-ahead market* or no later than two hours prior to the start of the first *dispatch hour* to which the request pertains for inclusion in the *real-time market*. When the *Request for Segregation* is for the operation of a *generation resource* in a *segregated mode of operation* for more than one day the *IESO* may approve such operation for up to two *business days*.
- 1.3.4 The *IESO* shall make a decision regarding a *Request for Segregation* prior to the run of the *day-ahead market calculation engine* if the request is submitted on the *day prior to the relevant dispatch day* by 8:00 EPT or 9:00 EPT as applicable, in accordance with section 1.3.3. The *IESO* shall make a decision regarding a *Request for Segregation* submitted after 9:00 EPT on the *day prior to the relevant dispatch day* as soon as practicable but no later than such time that allows the *transmitter*, referred to in section 1.3.5, a minimum of 90 minutes or such lesser time as agreed to by the *transmitter* to switch any applicable

equipment or *facilities* required to permit implementation of the *segregated mode of operation* prior to the time set out in section 1.3.1.1, and shall notify the *registered market participant* of such decision. The *IESO*:

1.3.4.1 shall deny such *Request for Segregation* if:

- a. such *Request for Segregation* pertains to a *generation resource* located in the province of Ontario and would threaten the reliability of the *IESO-controlled grid*; or
- b. the *metering installation* for the *generation resource* to which such *Request for Segregation* relates does not comply with MR Ch. 6 s.4.1A.1; or
- c. such *Request for Segregation* pertains to a *generation resource* located outside the province of Ontario and would threaten the *security* of the *IESO-controlled grid*; and

1.3.4.2 may deny such *Request for Segregation* if the *metered market participant* for the *metering installation* for the *generation resource* to which such *Request for Segregation* relates has previously failed to comply with MR Ch.6 App.6.1 s.1.2.1.7 for a period in which such *generation resource* operated in a *segregated mode of operation*.

1.3.5 If the *IESO* approves a *Request for Segregation*, it shall direct the relevant *transmitter* to:

1.3.5.1 switch any applicable equipment or *facilities* required to permit implementation of the *segregated mode of operation* at the time referred to in section 1.3.1.1;

1.3.5.2 switch any applicable equipment or *facilities* required to cease implementation of the *segregated mode of operation* at the expiry of the time referred to in section 1.3.1.2.

1.3.6 The *IESO* may at any time revoke its approval to operate a *generation resource* in a *segregated mode of operation* or terminate the operation of a *generation resource* in a *segregated mode of operation*, as the case may be, for the reason described in section 1.3.4.1(b), where the *metered market participant* is failing to comply with MR Ch.6 App.6.1 s. 1.2.1.7 in respect of the *metering installation* for such *generation resource* or where, in the *IESO's* opinion, such approval or such continued operation would threaten the reliability of a local area which forms part of the *IESO-controlled grid* or the security of the *integrated power system*, and shall notify the *registered market participant* accordingly. Where the *IESO* intends to revoke its approval to operate a *generation resource* in a *segregated mode of operation*, it shall revoke any direction issued pursuant to section 1.3.5.

Where the *IESO* intends to terminate such operation, the *IESO* shall direct the relevant *transmitter* to switch any applicable equipment or *facilities* required to cease implementation of the *segregated mode of operation*. Where the *IESO* revokes its approval to operate a *generation resource* in a *segregated mode of operation* or terminates the operation of a *generation resource* in a *segregated mode of operation*, as the case may be, the *registered market participant* for that *generation resource* shall not be entitled to compensation for any costs, losses or damages from the *IESO* for such revocation or termination.

1.3.7 The *IESO* shall coordinate and confirm with the applicable *control area operator*:

1.3.7.1 the switching to be effected by the relevant *transmitter* in accordance with section 1.3.5 or 1.3.6; and

1.3.7.2 the names of the *generation resources* that will operate in a *segregated mode of operation*.

1.3.8 The *IESO* shall not issue *dispatch instructions* to a *generation resource* in respect of any *dispatch hour* during which *such generation resource* is operating in a *segregated mode of operation*. All instructions relating to *dispatch* for the *generation resource* while operating in a *segregated mode of operation* shall be sent directly by the applicable *control area operator* to the *registered market participant*.

1.3.9 A *registered market participant* may only cancel or revise a *Request for Segregation* that requires an *outage* to equipment that the *IESO* has designated as critical, in accordance with the applicable *market manual*, after 8:00 EPT on the *day prior to the relevant dispatch day* if operating its *generation resource* in a *segregated mode of operation* would endanger the safety of any person, damage equipment, or violate any *applicable law*.

1.3.10 A *registered market participant* may cancel a *Request for Segregation* that does not require an *outage* to equipment that the *IESO* has designated as critical, in accordance with the applicable *market manual*, at any time.

1.3.11 A *registered market participant* that cancels a *Request for Segregation* pursuant to sections 1.3.9 and 1.3.10 shall cancel the *outage* request associated with the *Request for Segregation* for its *generation resource*.

## 1.4 Settlements

1.4.1 The delivery of electricity or a *physical service* by a *generation resource* while operating in a *segregated mode of operation* shall be excluded from the *IESO's settlement process* and in no event shall the *IESO* be required to effect payment in respect of any electricity or *physical service* so delivered.



- 1.4.2 Notwithstanding section 1.4.1, a *registered market participant* that operates a *generation resource* in a *segregated mode of operation* shall submit such scheduling information to the *IESO* as may be necessary to enable the *IESO* to determine the amounts payable by the *registered market participant* for *export transmission service* related to such operation.
- 1.4.3 Any costs incurred by a *transmitter* in complying with a direction issued pursuant to section 1.3.5 or 1.3.6 shall be borne by the *registered market participant* or the *transmitter* in the manner specified in their *connection agreement*.
- 1.4.4 The *registered market participant* shall be solely liable in respect of any positive or negative inadvertent accumulated while its *generation resources* are operating in the *segregated mode of operation*.

# Appendix 7.8 – Economic Operating Point

## 1. Introduction

### 1.1 Purpose

- 1.1.1 This appendix describes the processes used to determine the economic operating points for lost cost in the *day-ahead market* and *real-time market*, and for lost opportunity in the *real-time market*.

## 2. Day-Ahead Market Lost Cost Economic Operating Point

### 2.1 Purpose

- 2.1.1 This section describes the process used to determine the lost cost economic operating point for eligible *resources* in the *day-ahead market* (DAM LC EOP).

### 2.2 Sets, Indices and Parameters used in the DAM LC EOP Calculation

#### Fundamental Sets and Indices

- 2.2.1  $A$  designates the set of all *intertie zones*;
- 2.2.2  $B$  designates the set of buses identifying all *dispatchable* and *non-dispatchable resources* within Ontario;
- 2.2.3  $B^{DG} \subseteq B$  designates the set of buses identifying *dispatchable generation resources*;
- 2.2.4  $B^{DL} \subseteq B$  designates the set of buses identifying *dispatchable loads*;
- 2.2.5  $B^{HE} \subseteq B^{DG}$  designates the subset of buses identifying *dispatchable hydroelectric generation resources*;
- 2.2.6  $B_s^{HE} \subseteq B^{HE}$  designates the subset of buses identifying *dispatchable hydroelectric generation resources* in set  $s \in \text{SHE}$ ;
- 2.2.7  $D$  designates the set of buses outside Ontario, corresponding to imports and exports in *intertie zones*;
- 2.2.8  $D_a \subseteq D$  designates the set of all buses identifying *boundary entity resources* in *intertie zone*  $a \in A$ ;

- 2.2.9  $DI \subseteq D$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers*;
- 2.2.10  $DI_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers* in *intertie zone*  $a \in A$ ;
- 2.2.11  $DX \subseteq D$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids*;
- 2.2.12  $DX_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids* in *intertie zone*  $a \in A$ ;
- 2.2.13  $f_{h,b}^E$  designates the set of *bid* laminations for *energy* at bus  $b \in B^{DL} \cup DX$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.14  $f_{h,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B^{DL}$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.15  $f_{h,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B^{DL} \cup DX$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.16  $f_{h,b}^{30R}$  designates the set of *offer* laminations for *thirty-minute operating reserve* at  $b \in B^{DL} \cup DX$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.17  $K_{h,b}^E$  designates the set of *offer* laminations for *energy* at bus  $b \in B \cup DI$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.18  $K_{h,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B^{DG} \cup DI$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.19  $K_{h,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B^{DG} \cup DI$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.20  $K_{h,b}^{30R}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B^{DG} \cup DI$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.21  $\wp(B^{HE})$  designates the set of all subsets of the set  $B^{HE}$ ;
- 2.2.22  $B_{up}^{HE} \subseteq \wp(B^{HE})$  designates the set of buses identifying all upstream *dispatchable hydroelectric generation resources* with a *linked forebay*;
- 2.2.23  $B_{dn}^{HE} \subseteq \wp(B^{HE})$  designates the set of buses identifying all downstream *dispatchable hydroelectric generation resources* with a *linked forebay*;

## Market Participant Data Parameters

2.2.24 With respect to all *resources*:

2.2.24.1  $Derate_{h,b}$  designates the maximum amount of *energy and operating reserve* that can be scheduled for a *resource* in a *dispatch hour*  $h \in \{1, \dots, 24\}$ .

2.2.25 With respect to a *dispatchable generation resource* identified by bus  $b \in B^{DG}$ :

2.2.25.1  $MinQDG_b$  designates the *minimum loading point*;

2.2.25.2  $ORRDG_b$  designates the maximum *operating reserve* ramp rate in MW per minute;

2.2.25.3  $PDG_{h,b,k}$  designates the price for the maximum incremental quantity of *energy* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$ ;

2.2.25.4  $P10SDG_{h,b,k}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10S}$ ;

2.2.25.4  $P10NDG_{h,b,k}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10N}$ ;

2.2.25.6  $P30RDG_{h,b,k}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{30R}$ ;

2.2.25.7  $QDG_{h,b,k}$  designates the maximum incremental quantity of *energy* above the *minimum loading point* that may be scheduled for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$ ;

2.2.25.8  $Q10SDG_{h,b,k}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10S}$ ;

2.2.25.9  $Q10NDG_{h,b,k}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10N}$ ;

- 2.2.25.10  $Q30RDG_{h,b,k}$  designates the maximum incremental quantity of *thirty-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with offer lamination  $k \in K_{h,b}^{30R}$ ;
- 2.2.25.11  $RLP10S_{h,b}$  designates the *reserve loading point* for synchronized *ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  ;
- 2.2.25.12  $RLP30R_{h,b}$  designates the *reserve loading point* for *thirty-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  ; and
- 2.2.25.13  $QDLFIRM_{h,b}$  designates the quantity of *energy* that is *bid* at the *maximum market clearing price* in hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.26 With respect to a *dispatchable hydroelectric generation resource* identified by bus  $b \in B^{HE}$ :
- 2.2.26.1  $ForL_{b,i}, ForU_{b,i}$  shall designate the lower and upper limits, respectively, of the *resource's forbidden regions* indicating that the *resource* cannot be scheduled between  $ForL_{b,i}$  and  $ForU_{b,i}$  for all  $i \in \{1, \dots, N_{Forb}\}$ ;
- 2.2.26.2  $MaxStartsHE_b$  designates the *maximum number of starts per day* for the *resource*;
- 2.2.26.3  $MaxDEL_b$  designates the *maximum daily energy limit* for a single *resource* with or without a *linked forebay*;
- 2.2.26.4  $MinDEL_b$  designates the *minimum daily energy limit* for a single *resource* with or without a *linked forebay*;
- 2.2.26.5  $MinHMR_{h,b}$  designates the *hourly must-run* quantity for the *resource* for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.26.6  $MinHO_{h,b}$  designates the *minimum hourly output* quantity for the *resource* for hour  $h \in \{1, \dots, 24\}$ ; and
- 2.2.26.7  $StartMW_{b,i}$  for  $i \in \{1, \dots, NStartMW_b\}$  designates the *start indication value* for measuring *maximum number of starts per day*;
- 2.2.27 With respect to *dispatchable hydroelectric generation resources* with a *linked forebay*:
- 2.2.27.1  $MaxSDEL_s$  designates the *maximum daily energy limit* shared by all *dispatchable hydroelectric generation resources* in set  $s \in SHE$ ; and

- 2.2.27.2  $MinSDEL_s$  designates the *minimum daily energy limit* shared by all *dispatchable hydroelectric generation resources* in set  $s \in SHE$ ;
- 2.2.28 With respect to a *dispatchable hydroelectric generation resource* for which a *MWh ratio* was respected:
- 2.2.28.1  $LNK \subseteq B_{up}^{HE} \times B_{dn}^{HE}$  designates the set of linked *dispatchable hydroelectric generation resources*, where  $LNK$  is a set with elements of the form  $(b_1, b_2)$  and  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ ;
- 2.2.29 With respect to a *pseudo-unit* identified by bus  $b \in B^{PSU}$ :
- 2.2.29.1  $CTShareMLP_b$  designates the combustion turbine share of the *minimum loading point* region;
- 2.2.29.2  $CTShareDR_b$  designates the combustion turbine share of the *dispatchable* region;
- 2.2.29.3  $STShareMLP_b$  designates the steam turbine share of the *minimum loading point* region; and
- 2.2.29.4  $STShareDR_b$  designates the steam turbine share of the *dispatchable* region;
- 2.2.30 With respect to a *dispatchable load* identified by bus  $b \in B^{DL}$ :
- 2.2.30.1  $PDL_{h,b,j}$  designates the price for the maximum incremental quantity of *energy* for hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,b}^E$ ;
- 2.2.30.2  $P10SDL_{h,b,j}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{10S}$ ;
- 2.2.30.3  $P10NDL_{h,b,j}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{10N}$ ;
- 2.2.30.4  $P30RDL_{h,b,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,b}^{30R}$ ;
- 2.2.30.5  $QDL_{h,b}$  shall designate the maximum *bid* quantity for *energy* at  $b \in B^{DL}$  for hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,b}^E$ ;

- 2.2.30.6  $QDLFIRM_{h,b}$  designates the quantity of *energy* that is *bid* at the *maximum market clearing price* at  $b \in B^{DL}$  for hour  $h \in \{1, \dots, 2\}$ ;
- 2.2.30.7  $Q10SDL_{h,b}$  designates the maximum incremental quantity of *synchronized ten-minute operating reserve* that may be scheduled for hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $j \in J_{h,b}^{10S}$ ;
- 2.2.30.8  $Q10NDL_{h,b}$  designates the maximum incremental quantity of *non-synchronized ten-minute operating reserve* that may be scheduled for hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $j \in J_{h,b}^{10N}$ ; and
- 2.2.30.9  $Q30RDL_{h,b}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled for hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $j \in J_{h,b}^{30R}$ ;
- 2.2.31 With respect to a *boundary entity resource* import from *intertie zone* bus  $d \in DI$ , where the *locational marginal price* represents the price at the *intertie metering point*:
- 2.2.31.1  $PIG_{h,d,k}$  designates the price for the maximum incremental quantity of *energy* that may be scheduled to import in hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,b}^E$ ;
- 2.2.31.2  $P10NIG_{h,d,k}$  designates the price for the maximum incremental quantity of *non-synchronized ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,d}^{10N}$ ;
- 2.2.31.3  $P30RIG_{h,d,k}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,d}^{30R}$ ;
- 2.2.31.4  $QIG_{h,d,k}$  designates the maximum incremental quantity of *energy* for hour  $h \in \{1, \dots, 24\}$  that may be scheduled in association with *offer lamination*  $k \in K_{h,d}^E$ ;
- 2.2.31.5  $Q10NIG_{h,d,k}$  designates the maximum incremental quantity of *non-synchronized ten-minute operating reserve* that may be scheduled for hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{h,d}^{10N}$ ;
- 2.2.31.6  $Q30RIG_{h,d,k}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled for hour  $h \in \{1, \dots, 24\}$  in association with *offer lamination*  $k \in K_{d,b}^{30R}$ ;

- 2.2.32 With respect to a *boundary entity resource* export at *intertie zone* bus  $d \in DX$ , where the *locational marginal price* represents the price at the *intertie metering point*;
- 2.2.32.1  $PXL_{h,d,j}$  designates the price for the maximum incremental quantity of *energy* that may be scheduled to export in hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in J_{h,d}^E$ ;
- 2.2.32.2  $P10NXL_{h,d,j}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,d}^{10N}$ ;
- 2.2.32.3  $P30RXL_{h,d,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,d}^{30R}$ ;
- 2.2.32.4  $QXL_{h,d,j}$  designates the maximum quantity of *energy* for hour  $h \in \{1, \dots, 24\}$  may be scheduled in association with *bid* lamination  $j \in J_{h,d}^E$ ;
- 2.2.32.5  $Q10NXL_{h,d,j}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,d}^{10N}$ ;
- 2.2.32.6  $Q30RXL_{h,d,j}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in J_{h,d}^{30R}$ ;

### **IESO Data Parameters**

- 2.2.33  $ASD G_{h,b}$  designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide by the *day-ahead market calculation engine* at bus  $b$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.34  $COMCYCMW_{h,b}$  designates the MWh constraint placed onto a *resource* that is not modelled as a *pseudo unit* at bus  $b$  for hour  $h \in \{1, \dots, 24\}$  to reflect that *resource's energy* capability in combined cycle mode;
- 2.2.35  $ExtLMP_{h,d}^3$  designates the *locational marginal price* for *energy* for hour  $h \in \{1, \dots, 24\}$  as determined by Pass 3 of the *day-ahead market calculation engine* for *intertie zone* bus  $d \in D$ ;
- 2.2.36  $ExtL10NP_{h,d}^3$  designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* for the *dispatch hour*  $h \in \{1, \dots, 24\}$  as calculated by Pass 3 of the *day-ahead market calculation engine* for *intertie zone* bus  $d \in D$ ;



- 2.2.37  $ExtL30RP_{h,d}^3$  designates the *locational marginal price* for *thirty-minute operating reserve* for the *dispatch hour*  $h \in \{1, \dots, 24\}$  as calculated by Pass 3 of the *day-ahead market calculation engine* for *intertie zone bus*  $d \in D$ ;
- 2.2.38  $FG_{h,b}$  designates the *IESO's centralized variable generation forecast* for a *variable generation resource* identified by bus  $b \in B^{VG}$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.39  $GridConnected_{h,b}$  designates whether the *resource* is connected to the *IESO-controlled grid* at bus  $b$  for hour  $h \in \{1, \dots, 24\}$ ;
- 2.2.40  $IHE_{h,b,i}$  designates whether the *dispatchable hydroelectric generation resource* at bus  $b \in B^{HE}$  registered a start between hours  $(h - 1)$  and  $h \in \{1, \dots, 24\}$  as a result of its schedule increasing from below  $StartMW_{b,i}$  to at or above  $StartMW_{b,i}$  for  $i \in \{1, \dots, NStartMW_b\}$ ;
- 2.2.41  $LMP_{h,b}^3$  designates the *locational marginal price* for *energy* for hour  $h \in \{1, \dots, 24\}$  as determined by Pass 3 of the *day-ahead market calculation engine*;
- 2.2.42  $L10SP_{h,b}^3$  designates the *locational marginal price* for *synchronized ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  as determined by Pass 3 of the *day-ahead market calculation engine*;
- 2.2.43  $L10NP_{h,b}^3$  designates the *locational marginal price* for *non-synchronized ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  as determined by Pass 3 of the *day-ahead market calculation engine*;
- 2.2.44  $L30RP_{h,b}^3$  designates the *locational marginal price* for *thirty-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  as determined by Pass 3 of the *day-ahead market calculation engine*;
- 2.2.47  $REGULATIONMW_{h,b}$  designates the MWh constraint placed onto a *resource* at bus  $b$  for hour  $h \in \{1, \dots, 24\}$  for *regulation*;
- 2.2.48  $SHE$  designates the set indexing the sets of *dispatchable hydroelectric generation resources* with a *maximum daily energy limit* or a *minimum daily energy limit* or both for a *linked forebay*; and
- 2.2.49  $SEALMW_{h,b}$  designates the MWh constraint placed onto a *resource* at bus  $b$  for hour  $h \in \{1, \dots, 24\}$  for actions taken to ensure the safety of any person, prevent the damage of equipment, or prevent the violation of any *applicable law*;

## Constraint Violation Variables

- 2.2.50  $SLdViol_{h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{LdViol_h}\}$  of the penalty curve for the *energy* balance constraint allowing under-generation;
- 2.2.51  $SGenViol_{h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{GenViol_h}\}$  of the penalty curve for the *energy* balance constraint allowing over-generation;
- 2.2.52  $S10SViol_{h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{10SViol_h}\}$  of the penalty curve for the synchronized *ten-minute operating reserve* requirement;
- 2.2.53  $S10RViol_{h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{10RViol_h}\}$  of the penalty curve for the total *ten-minute operating reserve* requirement;
- 2.2.54  $S30RViol_{h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{30RViol_h}\}$  of the penalty curve for the *thirty-minute operating reserve* requirement and, when applicable, the flexibility *operating reserve* requirement;
- 2.2.55  $SREG10RViol_{r,h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{REG10RViol_h}\}$  of the penalty curve for violating the area total *ten-minute operating reserve* minimum requirement in region  $r \in ORREG$ ;
- 2.2.56  $SREG30RViol_{r,h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{REG30RViol_h}\}$  of the penalty curve for violating the area *thirty-minute operating reserve* minimum requirement in region  $r \in ORREG$ ;
- 2.2.57  $SXREG10RViol_{r,h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{XREG10RViol_h}\}$  of the penalty curve for violating the area total *ten-minute operating reserve* maximum restriction in region  $r \in ORREG$ ;
- 2.2.58  $SXREG30RViol_{r,h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{XREG30RViol_h}\}$  of the penalty curve for violating the area *thirty-minute operating reserve* maximum restriction in region  $r \in ORREG$ ;
- 2.2.59  $SPreITLViol_{f,h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{PreITLViol_{f,h}}\}$  of the penalty curve for violating the pre-contingency transmission limit for *facility*  $f \in F$ ;

- 2.2.60  $SITLViol_{c,f,h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{ITLViol_{c,f,h}}\}$  of the penalty curve for violating the post-contingency transmission limit for *facility*  $f \in F$  and contingency  $c \in C$ ;
- 2.2.61  $SPreXTLViol_{z,h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{PreXTLViol_{z,h}}\}$  of the penalty curve for violating the import/export limit associated with *intertie* limit constraint  $z \in Z_{Sch}$ ;
- 2.2.62  $SNIUViol_{h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{NIUViol_h}\}$  of the penalty curve for exceeding the net interchange increase limit between hours  $(h - 1)$  and  $h$ ;
- 2.2.63  $SNIDViol_{h,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{NIDViol_h}\}$  of the penalty curve for exceeding the net interchange decrease limit between hours  $(h - 1)$  and  $h$ ;
- 2.2.64  $SMaxDelViol_{h,b,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{MaxDelViol_h}\}$  of the penalty curve for exceeding the *maximum daily energy limit* constraint for a *resource* at bus  $b \in B^{ELR}$ ;
- 2.2.65  $SMinDelViol_{h,b,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{MinDelViol_h}\}$  of the penalty curve for violating the *minimum daily energy limit* constraint for a *resource* at bus  $b \in B^{HE}$ ;
- 2.2.66  $SSMaxDelViol_{h,s,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{SSMaxDelViol_h}\}$  of the penalty curve for exceeding the shared *maximum daily energy limit* constraint for *dispatchable hydroelectric generation resources* in set  $s \in SHE$ ;
- 2.2.67  $SSMinDelViol_{h,s,i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{SSMinDelViol_h}\}$  of the penalty curve for violating the shared *minimum daily energy limit* constraint for *dispatchable hydroelectric generation resources* in set  $s \in SHE$ ;
- 2.2.68  $SOGenLnkViol_{h,(b_1,b_2),i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{OGenLnkViol_h}\}$  of the penalty curve for violating the *linked forebay* constraint for *dispatchable hydroelectric generation resources* by over-generating the downstream *resource*, for  $(b_1, b_2) \in LNK$  such that  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ ; and
- 2.2.69  $SUGenLnkViol_{h,(b_1,b_2),i}$  designates the violation variable associated with segment  $i \in \{1, \dots, N_{UGenLnkViol_h}\}$  of the penalty curve for violating the *linked forebay* constraint for *dispatchable hydroelectric generation resources* by under-

generating the downstream *resource*, for  $(b_1, b_2) \in LNK$  such that  $b_1 \in B_{up}^{HE}$  and  $b_2 \in B_{dn}^{HE}$ .

## 2.3 Objective Functions

2.3.1 The objective functions for the DAM LC EOP calculation shall solve for the following variables:

- 2.3.1.1  $ESDG_{h,b,k}$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^E$ ;
- 2.3.1.2  $ES10SDG_{h,b,k}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10S}$ ;
- 2.3.1.3  $ES10NDG_{h,b,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{10N}$ ;
- 2.3.1.4  $ES30RDG_{h,b,k}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,b}^{30R}$ ;
- 2.3.1.5  $ESIG_{h,d,k}$  which designates the amount of *energy* that a *boundary entity resource* is scheduled to import from *intertie zone* bus  $d \in DI$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^E$ ;
- 2.3.1.6  $ES10NIG_{h,d,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that an import *boundary entity resource* is scheduled to provide from *intertie zone* bus  $d \in DI$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^E$ ;
- 2.3.1.7  $ES30RIG_{h,d,k}$  which designates the amount of *thirty-minute operating reserve* that an import *boundary entity resource* is scheduled to provide at bus  $d \in DI$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^E$ ;

- 2.3.1.8  $ESDL_{h,b,j}$  which designates the amount of *energy* that a *dispatchable load* is scheduled to consume at bus  $b \in B^{DL}$  for hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $j \in \mathcal{J}_{h,b}^F$ ;
- 2.3.1.9  $ES10SDL_{h,b,j}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in \mathcal{J}_{h,b}^{10S}$ ;
- 2.3.1.10  $ES10NDL_{h,b,j}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in \mathcal{J}_{h,b}^{10N}$ ;
- 2.3.1.11  $ES30RDL_{h,b,j}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $j \in \mathcal{J}_{h,b}^{30R}$ ;
- 2.3.1.12  $ESXL_{h,d,k}$  which designates the amount of *energy* a *boundary entity resource* is scheduled to export at *intertie zone* at bus  $d \in DX$  for hour  $h \in \{1, \dots, 24\}$  in association with *bid* lamination  $k \in K_{h,d}^E$ ;
- 2.3.1.13  $ES10NXL_{h,d,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that an export *boundary entity resource* is scheduled to provide at *intertie zone* bus  $d \in DX$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^E$ ;
- 2.3.1.14  $ES30RXL_{h,d,k}$  which designates the amount of *thirty-minute operating reserve* that an export *boundary entity resource* is scheduled to provide at *intertie zone* bus  $d \in DX$  for hour  $h \in \{1, \dots, 24\}$  in association with *offer* lamination  $k \in K_{h,d}^E$ ;

2.3.2 For each of the following *resource* types, the objective function for determining a DAM LC EOP shall maximize the value of the following expressions:

2.3.2.1 For *dispatchable generation resources*:

$$ObjSDG_h = \sum_{k \in K_{h,b}^E} ESG_{h,b,k} \cdot (LMP_{h,b}^3 - PDG_{h,b,k})$$

$$Obj10SDG_h = \sum_{k \in K_{h,b}^{10S}} ES10SG_{h,b,k} \cdot (L10SP_{h,b}^3 - P10SDG_{h,b,k})$$

$$Obj10NDG_h = \sum_{k \in K_{h,b}^{10N}} ES10NDG_{h,b,k} \cdot (L10NP_{h,b}^3 - P10NDG_{h,b,k})$$

$$Obj30RDG_h = \sum_{k \in K_{h,b}^{30R}} ES30RDG_{h,b,k} \cdot (L30RP_{h,b}^3 - P30RDG_{h,b,k})$$

2.3.2.2 For *dispatchable loads*:

$$ObjSDL_h = \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} \cdot (PDL_{h,b,j} - LMP_{h,b}^3)$$

$$Obj10SDL_h = \sum_{j \in J_{h,b}^{10S}} ES10SDL_{h,b,j} \cdot (L10SP_{h,b}^3 - P10SDL_{h,b,j})$$

$$Obj10NDL_h = \sum_{j \in J_{h,b}^{10N}} ES10NDL_{h,b,j} \cdot (L10NP_{h,b}^3 - P10NDL_{h,b,j})$$

$$Obj30RDL_h = \sum_{j \in J_{h,b}^{30R}} ES30RDL_{h,b,j} \cdot (L30RP_{h,b}^3 - P30RDL_{h,b,j})$$

2.3.2.3 For import transactions associated with *boundary entity resources*:

$$ObjSIG_h = \sum_{k \in K_{h,d}^E} ESIG_{h,d,k} \cdot (ExtLMP_{h,d}^3 - PIG_{h,d,k})$$

$$Obj10NIG_h = \sum_{k \in K_{h,d}^{10N}} ES10NIG_{h,d,k} \cdot (ExtL10NP_{h,d}^3 - P10NIG_{h,d,k})$$

$$Obj30RIG_h = \sum_{k \in K_{h,d}^{30R}} ES30RIG_{h,d,k} \cdot (ExtL30RP_{h,d}^3 - P30RIG_{h,d,k})$$

2.3.2.4 For export transactions associated with *boundary entity resources*

$$ObjSXL_h = \sum_{j \in J_{h,b}^E} ESXL_{h,d,j} \cdot (PXL_{h,d,j} - ExtLMP_{h,d}^3)$$

$$Obj10NXL_h = \sum_{j \in J_{h,b}^{10N}} ES10NXL_{h,d,j} \cdot (ExtL10NP_{h,d}^3 - P10NXL_{h,d,j})$$

$$Obj30RXL_h = \sum_{j \in J_{h,b}^{30R}} ES30RXL_{h,d,j} \cdot (ExtL30RP_{h,d}^3 - P30RXL_{h,d,j})$$

## 2.4 Constraints

2.4.1 The constraints described in this section 2.4 shall apply to the objective functions used for the DAM LC EOP calculation.

### Scheduling Variable Bounds

2.4.2 No DAM LC EOP shall be negative, nor shall any DAM LC EOP exceed the *offer* or *bid* quantity for *energy* or the *offer* quantity for *operating reserve*. Therefore, for all hours  $h \in \{1, \dots, 24\}$ :

$$\begin{aligned}
0 \leq ESDL_{h,b,j} &\leq QDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^E; \\
0 \leq ES10SDL_{h,b,j} &\leq Q10SDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^{10S}; \\
0 \leq ES10NDL_{h,b,j} &\leq Q10NDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^{10N}; \\
0 \leq ES30RDL_{h,b,j} &\leq Q30RDL_{h,b,j} && \text{for all } b \in B^{DL}, j \in J_{h,b}^{30R}; \\
0 \leq ESDG_{h,b,k} &\leq QDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^E; \\
0 \leq ES10SDG_{h,b,k} &\leq Q10SDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{10S}; \\
0 \leq ES10NDG_{h,b,k} &\leq Q10NDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{10N}; \\
0 \leq ES30RDG_{h,b,k} &\leq Q30RDG_{h,b,k} && \text{for all } b \in B^{DG}, k \in K_{h,b}^{30R}; \\
0 \leq ESXL_{h,d,j} &\leq QXL_{h,d,j} && \text{for all } b \in DX, j \in J_{h,d}^E; \\
0 \leq ES10NXL_{h,d,j} &\leq Q10NXL_{h,d,j} && \text{for all } b \in DX, j \in J_{h,d}^{10N}; \\
0 \leq ES30RXL_{h,d,j} &\leq Q30RXL_{h,d,j} && \text{for all } b \in DX, j \in J_{h,d}^{30R}; \\
0 \leq ESIG_{h,d,k} &\leq QIG_{h,d,k} && \text{for all } b \in DI, k \in K_{h,d}^E; \\
0 \leq ES10NIG_{h,d,k} &\leq Q10NIG_{h,d,k} && \text{for all } b \in DI, k \in K_{h,d}^{10N}; \\
0 \leq ES30RIG_{h,d,k} &\leq Q30RIG_{h,d,k} && \text{for all } b \in DI, k \in K_{h,d}^{30R};
\end{aligned}$$

2.4.3 For a *dispatchable load*, its DAM LC EOP for each class of *operating reserve* shall not exceed its DAM LC EOP for *energy*.

$$\begin{aligned}
\sum_{j \in J_{h,b}^{10S}} ES10SDL_{h,b,j} &\leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} \\
\sum_{j \in J_{h,b}^{10N}} ES10NDL_{h,b,j} &\leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} \\
\sum_{j \in J_{h,b}^{30R}} ES30RDL_{h,b,j} &\leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j}
\end{aligned}$$

2.4.4 For a *dispatchable generation resource* for a *dispatch hour*  $h \in \{1, \dots, 24\}$ :

For all  $b \in B^{VG}$ :



$$VGForecast_{h,b} = \begin{cases} AFG_{h,b} & \text{if provided} \\ FG_{h,b} & \text{otherwise} \end{cases}$$

For all  $b \in B^{DG}$ :

$$AdjMaxDG_{h,b} = \begin{cases} \min \left( \sum_{k \in K_{h,b}^E} QDG_{h,b,k}, Derate_{h,b}, VGForecast_{h,b} \right) & \text{if } b \in B^{VG} \\ \min \left( \sum_{k \in K_{h,b}^E} QDG_{h,b,k}, Derate_{h,b} \right) & \text{otherwise} \end{cases}$$

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} \leq AdjMaxDG_{h,b}$$

$$\sum_{k \in K_{h,b}^{10S}} ES10SDG_{h,b,k} \leq AdjMaxDG_{h,b}$$

$$\sum_{k \in K_{h,b}^{10N}} ES10NDG_{h,b,k} \leq AdjMaxDG_{h,b}$$

$$\sum_{k \in K_{h,b}^{30R}} ES30RDG_{h,b,k} \leq AdjMaxDG_{h,b}$$

2.4.5 Subject to section 2.4.6, the DAM LC EOP for a *resource* that is a *GOG-eligible resource* or has a primary fuel type of uranium shall be greater than or equal to its *minimum loading point*:

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} \geq MinQDG_b$$

2.4.6 For a *resource* that is a *GOG-eligible resource* or has a primary fuel type of uranium and that is scheduled below its *minimum loading point*, its DAM LC EOP shall be equal to its *day-ahead schedule*:

If  $\sum_{k \in K_{h,b}^E} ASDG_{h,b,k} < MinQDG_b$  for  $b \in B^{NQS}$  then:

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} = ASDG_{h,b}$$

### Constraints for Regulation Requirements

- 2.4.7 For a *dispatchable generation resource*, its DAM LC EOP for *energy* shall be greater than or equal to any *regulation* constraint that is applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} \geq REGULATIONMW_{h,b}$$

- 2.4.8 For a *dispatchable generation resource*, its DAM LC EOP for *energy* and each class of *operating reserve* shall not exceed the maximum available capacity the *resource* has less the *regulation constraint* that is applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} \leq AdjMaxDG_{h,b} - REGULATIONMW_{h,b}$$

$$\sum_{k \in K_{h,b}^{10S}} ES10SDG_{h,b,k} \leq AdjMaxDG_{h,b} - REGULATIONMW_{h,b}$$

$$\sum_{k \in K_{h,b}^{10N}} ES10NDG_{h,b,k} \leq AdjMaxDG_{h,b} - REGULATIONMW_{h,b}$$

$$\sum_{k \in K_{h,b}^{30R}} ES30RDG_{h,b,k} \leq AdjMaxDG_{h,b} - REGULATIONMW_{h,b}$$

### Constraints for Market Participant Requirements

- 2.4.9 For a *dispatchable generation resource*, its DAM LC EOP for *energy* shall be greater than or equal to any minimum  $SEALMW_{h,b}$  constraint that is applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} \geq SEALMW_{h,b}$$

- 2.4.10 For a *dispatchable load*, its DAM LC EOP for *energy* shall be greater than or equal to any minimum  $SEALMW_{h,b}$  constraint that is applied and for each class of *operating reserve*, the DAM LC EOP shall be less than or equal to the DAM LC EOP for *energy* for that *resource* less any minimum  $SEALMW_{h,b}$  constraint that is applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{h,b}^E} ESDL_{h,b,j} \geq SEALMW_{h,b}$$

$$\sum_{j \in J_{h,b}^{10S}} ES10SDL_{h,b,k} \leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} - SEALMW_{h,b}$$

$$\sum_{j \in J_{h,b}^{10N}} ES10NDL_{h,b,k} \leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} - SEALMW_{h,b}$$

$$\sum_{j \in J_{h,b}^{30R}} ES30RDL_{h,b,k} \leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} - SEALMW_{h,b}$$

- 2.4.11 For a *dispatchable generation resource*, its DAM LC EOP for *energy* shall be less than or equal to any maximum  $SEALMW_{h,b}$  constraint that is applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} \leq SEALMW_{h,b}$$

- 2.4.12 For a *dispatchable load*, its DAM LC EOP for *energy* shall be less than or equal to any maximum  $SEALMW_{h,b}$  constraint that is applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{h,b}^E} ESDL_{h,b,j} \leq SEALMW_{h,b}$$

- 2.4.13 For a *dispatchable generation resource*, its DAM LC EOP for *energy* shall be equal to any fixed  $SEALMW_{h,b}$  constraint that is applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} = SEALMW_{h,b}$$

- 2.4.14 For a *dispatchable load*, its DAM LC EOP for *energy* shall be equal to any fixed  $SEALMW_{h,b}$  constraint that is applied and equal to zero for each class of *operating reserve* for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{h,b}^E} ESDL_{h,b,j} = SEALMW_{h,b}$$

$$\sum_{j \in J_{h,b}^{10S}} ES10SDL_{h,b,j} = 0$$

$$\sum_{j \in J_{h,b}^{10N}} ES10NDL_{h,b,j} = 0$$

$$\sum_{j \in J_{h,b}^{30R}} ES30RDL_{h,b,j} = 0$$

- 2.4.15 For a *dispatchable load*, its DAM LC EOP for *energy* shall be greater than or equal to the *bid* quantity for *energy* priced at the *maximum market clearing price*:

$$\sum_{j \in J_{h,b}^E} ESDL_{h,b,j} \geq QDLFIRM_{h,b}$$

- 2.4.16 For a *dispatchable load*, its DAM LC EOP for *operating reserve* shall be less than or equal its DAM LC EOP for *energy* less the *bid* quantity for *energy* priced at the *maximum market clearing price*:

$$\begin{aligned}\sum_{j \in J_{h,b}^{10S}} ES10SDL_{h,b,j} &\leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} - QDLFIRM_{h,b} \\ \sum_{j \in J_{h,b}^{10N}} ES10NDL_{h,b,j} &\leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} - QDLFIRM_{h,b} \\ \sum_{j \in J_{h,b}^{30R}} ES30RDL_{h,b,j} &\leq \sum_{j \in J_{h,b}^E} ESDL_{h,b,j} - QDLFIRM_{h,b}\end{aligned}$$

### Constraints for Operating Reserve Ramping

- 2.4.18 For a *dispatchable generation resource* with  $RLP10S_{h,b} > 0$ , its DAM LC EOP for *ten-minute operating reserve* shall be less than or equal to its *reserve loading point* for *ten-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DG}$ :

$$\begin{aligned}\sum_{k \in K_{h,b}^{10S}} ES10SDG_{h,b,k} \\ \leq \left( \sum_{k \in K_{h,b}^E} ESDG_{h,b,k} \right) \cdot \left( \frac{1}{RLP10S_{h,b}} \right) \cdot \left( \min \left\{ 10 \cdot ORRDG_b, \sum_{k \in K_{h,b}^{10S}} Q10SDG_{h,b,k} \right\} \right)\end{aligned}$$

- 2.4.19 For a *dispatchable generation resource* with  $RLP30R_{h,b} > 0$ , its DAM LC EOP for *thirty-minute operating reserve* shall be less than or equal to its *reserve loading point* for *thirty-minute operating reserve* for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{DG}$ :

$$\begin{aligned}\sum_{k \in K_{h,b}^{30R}} ES30RDG_{h,b,k} \\ \leq \left( \sum_{k \in K_{h,b}^E} ESDG_{h,b,k} \right) \cdot \left( \frac{1}{RLP30R_{h,b}} \right) \cdot \left( \min \left\{ 30 \cdot ORRDG_b, \sum_{k \in K_{h,b}^{30R}} Q30RDG_{h,b,k} \right\} \right)\end{aligned}$$

### Constraints for Pseudo-Units

- 2.4.20 For a *pseudo-unit*, its DAM LC EOP for *energy* for the *dispatchable* region and duct firing region shall be less than or equal to the respective maximum capabilities for those regions for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{PSU}$ :

$$\sum_{k \in K_{h,b}^{DR}} ESDG_{h,b,k} \leq MaxDR_{h,b}$$

$$\sum_{k \in K_{h,b}^{DF}} ESDG_{h,b,k} \leq MaxDF_{h,b}$$

- 2.4.21 For a *pseudo-unit*, its DAM LC EOP for each class of *operating reserve* shall be less than or equal to the sum of the maximum capabilities for its *dispatchable* region and duct firing region for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{PSU}$ :

$$\sum_{k \in K_{h,b}^{10S}} ES10SDG_{h,b,k} \leq MaxDR_{h,b} + MaxDF_{h,b}$$

$$\sum_{k \in K_{h,b}^{10N}} ES10NDG_{h,b,k} \leq MaxDR_{h,b} + MaxDF_{h,b}$$

$$\sum_{k \in K_{h,b}^{30R}} ES30RDG_{h,b,k} \leq MaxDR_{h,b} + MaxDF_{h,b}$$

- 2.4.22 For a *pseudo-unit* that cannot provide *ten-minute operating reserve* from its duct firing region, the following constraint shall apply:

$$\sum_{k \in K_{h,b}^E} ESDG_{h,b,k} + \sum_{k \in K_{h,b}^{10S}} ES10SDG_{h,b,k} + \sum_{k \in K_{h,b}^{10N}} ES10NDG_{h,b,k} \leq MINQDG_b + QDR_{h,k}$$

### Constraints for Resources with Linked Forebays

- 2.4.23 For all *dispatchable* hydroelectric *generation resources* with a *linked forebay*, the DAM LC EOP for *energy* at the upstream *resources* in one hour shall result in a proportional DAM LC EOP for *energy* at the downstream *resources* in the hour determined by the *time lag*.

For all *dispatchable* hydroelectric *generation resources* with a *linked forebay* between upstream *resources*  $b_1 \in B_{up}^{HE}$  and downstream *resources*  $b_2 \in B_{dn}^{HE}$  for  $(b_1, b_2) \in LNK$  and hours  $h \in \{1, \dots, 24\}$  such that  $h + Lag_{b_1, b_2} \leq 24$ :

$$\sum_{b_2 \in B_{dn}^{HE}} \left( \sum_{k \in K_{b_2, h+Lag_{b_1, b_2}}^E} ESDG_{k, h+Lag_{b_1, b_2}, b_2} \right) = MWhRatio_{b_1, b_2} \cdot \sum_{b_1 \in B_{up}^{HE}} \left( \sum_{k \in K_{b_1, h}^E} ESDG_{k, h, b_1} \right)$$

## 2.5 Calculation of DAM LC EOP for Resources with a Linked Forebay Under Certain Conditions

2.5.1 For *dispatchable* hydroelectric *resources* with a *linked forebay*, the DAM LC EOP shall be equal to the *resource's day-ahead schedule* if the conditions in sections 2.4.24.1 and 2.4.24.2 are both satisfied:

2.4.24.1 The following constraint violation prices were non-binding in Pass 1 or Pass 3 of the *day-ahead market calculation engine* run for any *dispatch hour* in the *dispatch day*:

$$\sum_{i=1:N_{MaxDelViol_h}} SMaxDelViol_{h,b,i} = 0$$

$$\sum_{i=1:N_{MinDelViol_h}} SMinDelViol_{h,b,i} = 0$$

$$\sum_{i=1:N_{SMaxDelViol_h}} SSMaxDelViol_{h,s,i} = 0$$

$$\sum_{i=1:N_{SMinDelViol_h}} SSMinDelViol_{h,s,i} = 0; \text{ or}$$

$$\sum_{i=1:N_{LdViol_h}} SLdViol_{h,i} = 0$$

$$\sum_{i=1:N_{GenViol_h}} SGenViol_{h,i} = 0$$

$$\sum_{i=1:N_{10SViol_h}} S10SViol_{h,i} = 0$$

$$\sum_{i=1:N_{10RViol_h}} S10RViol_{h,i} = 0$$

$$\sum_{i=1:N_{30RViol_h}} S30RViol_{h,i} = 0$$

$$\sum_{i=1:N_{REG10RViol_h}} SREG10RViol_{r,h,i} = 0$$

$$\sum_{i=1:N_{REG30RViol_h}} SREG30RViol_{r,h,i} = 0$$

$$\sum_{i=1:N_{XREG10RViol_h}} SXREG10RViol_{r,h,i} = 0$$

$$\sum_{i=1:N_{XREG30RViol_h}} SXREG30RViol_{r,h,i} = 0$$

$$\sum_{i=1:N_{PreITLViol_{f,h}}} SPreITLViol_{f,h,i} = 0$$

$$\sum_{i=1:N_{ITLViol_{c,f,h}}} SITLViol_{c,f,h,i} = 0$$

$$\sum_{i=1:N_{PreXTLViol_{z,h}}} SPreXTLViol_{z,h,i} = 0$$

$$\sum_{i=1:N_{NIUViol_h}} SNIUViol_{h,i} = 0$$



$$\sum_{i=1:N_{NDViol_h}} SNIDViol_{h,i} = 0$$

$$\sum_{i=1:N_{OGenLnkViol_h}} SOGenLnkViol_{h,(b1,b2),i} = 0$$

$$\sum_{i=1:N_{UGenLnkViol_h}} SUGenLnkViol_{h,(b1,b2),i} = 0, \text{ and}$$

2.4.24.2 At least one of the conditions set out in sections 2.4.24.2.1-2.4.24.2.4 is met:

2.4.24.2.1 At least one *resource* with a *linked forebay* has a *day-ahead schedule* that satisfies any one of the following conditions for a *dispatch hour* in which the *time lag* was evaluated:

- a.  $\sum_{k \in K_{h,b}^E} ASDG_{h,b,k} \leq MinHMR_{h,b};$
- b.  $\sum_{k \in K_{h,b}^E} ASDG_{h,b,k} \leq MinHO_{h,b};$  or
- c.  $ForL_{b,i} \leq \sum_{k \in K_{h,b}^E} ASDG_{h,b,k} \leq ForU_{b,i};$

2.4.24.2.2 For all *resources* with a *linked forebay* where at least one of the following daily constraints are binding for at least one *dispatch hour* in a *dispatch day*:

$$\sum_{h=1..24} \left( \sum_{i=1..N_{StartMW_b}} IHE_{h,b,i} \right) \geq MaxStartsHE_b$$

$$\sum_{h=1..H} \left( \sum_{b \in B_S^{HE}} \left( \sum_{k \in K_{h,b}^E} ASDG_{h,b,k} \right) \right)$$

$$+ \sum_{b \in B_S^{HE}} \left( 10ORConv \left( \sum_{k \in K_{H,b}^{10S}} S10SDG_{H,b,k} \right) \right)$$

$$+ \sum_{k \in K_{H,b}^{10N}} S10NDG_{H,b,k} \Bigg)$$

$$+ 30ORConv \left( \sum_{k \in K_{H,b}^{30R}} S30RDG_{H,b,k} \right) \Bigg) \geq MaxSDEL_s$$

$$\sum_{h=1..24} \left( \sum_{b \in B_S^{HE}} \left( \sum_{k \in K_{h,b}^E} ASDG_{h,b,k} \right) \right) \leq MinSDEL_s;$$

2.4.24.2.3 For all *resources* with a *linked forebay* that do not have a binding *reliability* constraint applied for a *dispatch hour* in which the *time lag* was evaluated:

$$\sum_{k \in K_{h,b}^E} ASDG_{h,b,k} \neq RELIABILITYMW_{h,b} \quad \text{where } b \in B^{HE}$$

2.4.24.2.4 For all *resources* with a *linked forebay* that have at least one binding  $SEALMW_{h,b}$  constraint for a *dispatch hour* in which the *time lag* was evaluated, at least one of the following conditions was met:

- a. For a *resource* that has a fixed  $SEALMW_{h,b}$  constraint applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{HE}$ :

$$\sum_{k \in K_{h,b}^E} ASDG_{h,b,k} = SEALMW_{h,b}$$

- For a *resource* that has a minimum  $SEALMW_{h,b}$  constraint applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{HE}$ :

$$\sum_{k \in K_{h,b}^E} ASDG_{h,b,k} \leq SEALMW_{h,b}$$

- For a *resource* that has a maximum  $SEALMW_{h,b}$  constraint applied for hour  $h \in \{1, \dots, 24\}$  and bus  $b \in B^{HE}$ :

$$\sum_{k \in K_{h,b}^E} ASDG_{h,b,k} \geq SEALMW_{h,b}$$

## 2.6 Outputs

- 2.5.1 The DAM LC EOPs used for *settlement* for *energy* and *operating reserve* for all *resources* except *pseudo-units* for each hour of the *dispatch day* shall be the sum of each DAM LC EOP variable determined by the objective function in section 2.3 for that *resource*, subject to constraints in section 2.4 applicable for that *resource* determined as follows:

$$DGEnergyEOP_{h,b} = \sum_{k \in K_{h,b}^E} ESDG_{h,b,k}$$

$$DG10SEOP_{h,b} = \sum_{k \in K_{h,b}^{10S}} ES10SDG_{h,b,k}$$

$$DG10NEOP_{h,b} = \sum_{k \in K_{h,b}^{10N}} ES10NDG_{h,b,k}$$

$$DG30REOP_{h,b} = \sum_{k \in K_{h,b}^{30R}} ES30RDG_{h,b,k}$$

$$DLEnergyEOP_{h,b} = \sum_{j \in J_{h,b}^E} ESDL_{h,b,j}$$

$$DL10SEOP_{h,b} = \sum_{j \in J_{h,b}^{10S}} ES10SDL_{h,b,j}$$

$$DL10NEOP_{h,b} = \sum_{j \in J_{h,b}^{10N}} ES10NDL_{h,b,j}$$

$$DL30REOP_{h,b} = \sum_{j \in J_{h,b}^{30R}} ES30RDL_{h,b,j}$$

$$DIEnergyEOP_{h,b} = \sum_{k \in K_{h,b}^E} ESIG_{h,b,k}$$

$$DI10NEOP_{h,b} = \sum_{k \in K_{h,b}^{10N}} ES10NIG_{h,b,k}$$

$$DI30REOP_{h,b} = \sum_{k \in K_{h,b}^{30R}} ES30RIG_{h,b,k}$$

$$DXEnergyEOP_{h,b} = \sum_{j \in J_{h,b}^E} ESXL_{h,b,j}$$

$$DX10NEOP_{h,b} = \sum_{j \in J_{h,b}^{10N}} ES10NXL_{h,b,j}$$

$$DX30REOP_{h,b} = \sum_{j \in J_{h,b}^{30R}} ES30RXL_{h,b,j}$$

2.5.2 The DAM LC EOPs for *energy* and *operating reserve* for a *pseudo-unit* for each hour of the *dispatch day*, which will be used for converting the DAM LC EOPs to physical *resource* equivalents in accordance with sections 2.5.3 to 2.5.4, shall be determined as follows:

$$PSUMLP_{EnergyEOP_{h,k}} = \sum_{k \in K_{h,b}^{MLP}} ESDG_{h,b,k}$$

$$PSUDRE_{EnergyEOP_{h,k}} = \sum_{k \in K_{h,b}^{DR}} ESDG_{h,b,k}$$

$$PSUDF_{EnergyEOP_{h,k}} = \sum_{k \in K_{h,b}^{DF}} ESDG_{h,b,k}$$

$$PSU10SEOP_{h,k} = \sum_{k \in K_{h,b}^{10S}} ES10SDG_{h,b,k}$$

$$PSU10NEOP_{h,k} = \sum_{k \in K_{h,b}^{10N}} ES10NDG_{h,b,k}$$

$$PSU30REOP_{h,k} = \sum_{k \in K_{h,b}^{30R}} ES30RDG_{h,b,k}$$

### Conversion of DAM LC EOPs for Pseudo-Units to Physical Resource Equivalents

2.6.3 The DAM LC EOP used for *settlement* for *energy* for a combustion turbine and a steam turbine that is associated with *pseudo-unit*  $k \in \{1, \dots, K\}$  in hour  $h$  shall be determined as follows:

$$\begin{aligned} CT_{EnergyEOP_{h,k}} &= PSUMLP_{EnergyEOP_{h,k}} \cdot CTShareMLP_{h,k} + PSUDRE_{EnergyEOP_{h,k}} \\ &\quad \cdot CTShareDR_{h,k} \end{aligned}$$

$$\begin{aligned} ST_{EnergyEOP_{h,k}} &= PSUMLP_{EnergyEOP_{h,k}} \cdot STShareMLP_k + PSUDRE_{EnergyEOP_{h,k}} \\ &\quad \cdot STShareDR_k + PSUDF_{EnergyEOP_{h,k}} \end{aligned}$$

2.6.4 The DAM LC EOPs used for *settlement* for *operating reserve* for a combustion turbine and a steam turbine that is associated with *pseudo-unit*  $k \in \{1, \dots, K\}$  in hour  $h$  shall be determined as follows and in the following order for each class of *operating reserve*:

$$10SDR_{h,k} = \min(QDR_{h,k}, PSU10SEOP_{h,k})$$

$$10NDR_{h,k} = \min(QDR_{h,k} - 10SDR_{h,k}, PSU10NEOP_{h,k})$$

$$30RDR_{h,k} = \min(QDR_{h,k} - 10SDR_{h,k} - 10NDR_{h,k}, PSU30REOP_{h,k})$$

$$CT10SEOP_{h,k} = 10SDR_{h,k} \cdot CTShareDR_k$$

$$ST10SEOP_{h,k} = 10SDR_{h,k} \cdot STShareDR_k + (PSU10SEOP_{h,k} - 10SDR_{h,k})$$

$$CT10NEOP_{h,k} = 10NDR_{h,k} \cdot CTShareDR_k$$

$$ST10NEOP_{h,k} = 10NDR_{h,k} \cdot STShareDR_k + (PSU10NEOP_{h,k} - 10NDR_{h,k})$$

$$CT30REOP_{h,k} = 30RDR_{h,k} \cdot CTShareDR_k$$

$$ST30REOP_{h,k} = 30RDR_{h,k} \cdot STShareDR_k + (PSU30REOP_{h,k} - 30RDR_{h,k})$$

### 3. Real-Time Market Lost Cost Economic Operating Point

#### 3.1 Purpose

3.1.1 This section describes the process used to determine lost cost economic operating point (RT LC EOP) for eligible *resources* in the *real-time market*.

#### 3.2 Sets, Indices and Parameters used by the Real-Time Lost Cost Economic Operating Point Calculation

##### Fundamental Sets and Indices

3.2.1  $A$  designates the set of all *intertie zones*;

3.2.2  $B$  designates the set of buses identifying all *dispatchable* and *non-dispatchable resources* within Ontario;

3.2.3  $B^{DG} \subseteq B$  designates the set of buses identifying *dispatchable generation resources*;

3.2.4  $B^{DL} \subseteq B$  designates the set of buses identifying *dispatchable loads*;

3.2.5  $D$  designates the set of buses outside Ontario, corresponding to imports and exports in *intertie zones*;

3.2.6  $D_a \subseteq D$  designates the set of all buses identifying *boundary entity resources* in *intertie zone*  $a \in A$ ;

3.2.7  $DI \subseteq D$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers*;

3.2.8  $DI_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers* in *intertie zone*  $a \in A$ ;

3.2.9  $DX \subseteq B^{DL}$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to import *offers*;

3.2.10  $DX_a \subseteq D_a$  designates the subset of *intertie zone* buses identifying *boundary entity resources* that correspond to export *bids* in *intertie zone*  $a \in A$ ;

3.2.11  $ExtLMP_{i,d}^{PD}$  designates the *locational marginal price for energy* for the *dispatch hour* in which interval  $i \in I$  falls as determined by Pass 1 of the *pre-dispatch calculation engine*;

3.2.12  $I = \{1, \dots, n_I\}$  designates the set of all intervals, where  $n_I$  designates the number of five-minute intervals considered within the real-time look-ahead period;

- 3.2.13  $J_{i,b}^E$  designates the set of *bid* laminations for *energy* at  $b \in B^{DL} \cup DX$  for interval  $i \in I$ ;
- 3.2.14  $J_{i,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at  $b \in B^{DL}$  for interval  $i \in I$ ;
- 3.2.15  $J_{i,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at  $b \in B^{DL} \cup DX$  for interval  $i \in I$ ;
- 3.2.16  $J_{i,b}^{30R}$  designates the set of *offer* laminations for *thirty-minute operating reserve* at  $b \in B^{DL} \cup DX$  for interval  $i \in I$ ;
- 3.2.17  $J_{t,d}^E$  designates the set of *bid* laminations for *energy* at *intertie zone* bus  $d \in DX$  for time-step  $t \in TS$ ;
- 3.2.18  $J_{t,d}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at  $d \in DX$  for time-step  $t \in TS$ ;
- 3.2.19  $J_{t,d}^{30R}$  shall designate the set of *offer* laminations for *thirty-minute operating reserve* at  $d \in DX$  for time-step  $t \in TS$ ;
- 3.2.20  $K_{i,b}^E$  designates the set of *offer* laminations for *energy* at  $b \in B^{DG} \cup DI$  for interval  $i \in I$ ;
- 3.2.21  $K_{i,b}^{10S}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $b \in B^{DG}$  for interval  $i \in I$ ;
- 3.2.22  $K_{i,b}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $b \in B^{DG} \cup DI$  for interval  $i \in I$ ;
- 3.2.23  $K_{i,b}^{30R}$  designates the set of *offer* laminations for non-synchronized *thirty-minute operating reserve* at bus  $b \in B^{DG} \cup DI$  for interval  $i \in I$ ;
- 3.2.24  $K_{t,d}^E$  designates the set of *offer* laminations for *energy* at  $d \in DI$  for time-step  $t \in TS$ ;
- 3.2.25  $K_{t,d}^{10N}$  designates the set of *offer* laminations for non-synchronized *ten-minute operating reserve* at bus  $d \in DI$  for time-step  $t \in TS$ ;
- 3.2.26  $K_{t,d}^{30R}$  designates the set of *offer* laminations for synchronized *ten-minute operating reserve* at bus  $d \in DI$  for time-step  $t \in TS$ ; and

- 3.2.27  $TS = \{2, \dots, n_{LAP}\}$  designates the set of all time-steps in the look-ahead period that are included in the *pre-dispatch calculation engine* optimization, where  $n_{LAP}$  designates the number of time-steps in the pre-dispatch look-ahead period;

### Market Participant Data Parameters

- 3.2.28 With respect to all *resources*:
- 3.2.28.1  $Derate_{i,b}$  designates the maximum amount of *energy* and *operating reserve* that can be scheduled for a *resource* in a *dispatch interval*;
- 3.2.29 With respect to a *dispatchable generation resource* identified by bus  $b \in B^{DG}$ :
- 3.2.29.1  $MinQDG_{i,b}$  designates the *minimum loading point* indicating the minimum output at which a *resource* must be scheduled to except for times when the *resource* is starting up or shutting down at  $b \in B^{DG}$  for interval  $i$ ;
- 3.2.29.2  $ORRDG_b$  designates the maximum *operating reserve* ramp rate in MW per minute for the *resource* at  $b \in B^{DG}$ ;
- 3.2.29.3  $PDG_{i,b,k}$  designates the price for the maximum incremental quantity of *energy* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^E$ ;
- 3.2.29.4  $P10SDG_{i,b,k}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10S}$ ;
- 3.2.30.5  $P10NDG_{i,b,k}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10N}$ ;
- 3.2.30.6  $P30RDG_{i,b,k}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{30R}$ ;
- 3.2.30.7  $QDG_{i,b,k}$  designates the maximum incremental quantity of *energy* above the *minimum loading point* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^E$ ;
- 3.2.30.8  $Q10SDG_{i,b,k}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10S}$ ;



- 3.2.30.9  $Q10NDG_{i,b,k}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10N}$ ; and
- 3.2.30.10  $Q30RDG_{i,b,k}$  designates the maximum incremental quantity of *thirty-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{30R}$ ;
- 3.2.31 With respect to a *dispatchable load* identified by bus  $b \in B^{DL}$ :
- 3.2.31.1  $PDL_{i,b,j}$  designates the price for the maximum incremental quantity of *energy* for interval  $i \in I$  in association with *bid* lamination  $j \in J_{i,b}^E$ ;
- 3.2.31.2  $P10SDL_{i,b,j}$  designates the price for the maximum incremental quantity of synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10S}$ ;
- 3.2.31.3  $P10NDL_{i,b,j}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10N}$ ;
- 3.2.31.4  $P30RDL_{i,b,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{30R}$ ;
- 3.2.31.5  $QDL_{i,b}$  designates the maximum *bid* quantity for *energy* at  $b \in B^{DL}$  for interval  $i \in I$  in association with *bid* lamination  $j \in J_{i,b}^E$ ;
- 3.2.31.6  $QDLFIRM_{i,b}$  designates the quantity of *energy* that is *bid* at the *maximum market clearing price* at  $b \in B^{DL}$  in interval  $i \in I$ ;
- 3.2.31.7  $Q10SDL_{i,b}$  designates the maximum incremental quantity of synchronized *ten-minute operating reserve* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10S}$ ;
- 3.2.31.8  $Q10NDL_{i,b}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10N}$ ;
- 3.2.31.9  $Q30RDL_{i,b}$  designates the maximum incremental quantity of *thirty-minute operating reserve* that may be scheduled in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{30R}$ ;

- 3.2.31.10  $RLP10S_{i,b}$  designates the *reserve loading point* for synchronized *ten-minute operating reserve* in interval  $i \in I$ ; and
- 3.2.31.11  $RLP30R_{i,b}$  designates the *reserve loading point* for *thirty-minute operating reserve* in interval  $i \in I$ ;
- 3.2.32 With respect to a *pseudo-unit* identified by bus  $b \in B^{PSU}$ :
- 3.2.32.1  $CTShareMLP_b$  designates the combustion turbine share of the *minimum loading point* region;
- 3.2.32.2  $CTShareDR_b$  designates the combustion turbine share of the *dispatchable* region;
- 3.2.32.3  $STShareMLP_b$  designates the steam turbine share of the *minimum loading point* region; and
- 3.2.32.4  $STShareDR_b$  designates the steam turbine share of the *dispatchable* region;
- 3.2.33 With respect to a *boundary entity resource* import from *intertie zone* bus  $d \in DI$ , where the *locational marginal price* represents the price at the *intertie metering point*:
- 3.2.33.1  $PIG_{t,d,k}$  designates the price for the maximum incremental quantity of *energy* that may be scheduled to import in time-step  $t \in TS$  in association with *offer* lamination  $k \in$ ;
- 3.2.33.2  $P10NIG_{t,d,k}$  designates the price for the maximum incremental quantity of non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^{10N}$ ;
- 3.2.33.3  $P30RIG_{t,d,k}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^{30R}$ ;
- 3.2.33.4  $QIG_{t,d,k}$  designates the maximum quantity of *energy* for which an import at bus  $d \in DI$  in time-step  $t \in TS$  may be scheduled in association with *offer* lamination  $k \in K_{t,d}^E$ ;
- 3.2.33.5  $Q10NIG_{t,d,k}$  designates the maximum incremental quantity of non-synchronized *ten-minute operating reserve* that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^{10N}$ ; and

- 3.2.33.6  $Q30RIG_{t,d,k}$  designates the maximum incremental quantity of *thirty-minute operating reserve* quantity that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $k \in K_{t,d}^{30R}$ ;
- 3.2.34 With respect to a *boundary entity resource* export to *intertie zone* bus  $d \in DX$ , where the *locational marginal price* represents the price at the *intertie metering point*:
- 3.2.34.1  $PXL_{t,d,j}$  designates the price of the exporter at bus  $d$  for an incremental quantity of *energy* in time-step  $t \in TS$  in association with *bid* lamination  $j \in J_{t,d}^E$ ;
- 3.2.34.2  $P10NXL_{t,d,j}$  designates the price of being scheduled to provide non-synchronized *ten-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,d}^{10N}$ ;
- 3.2.34.3  $P30RXL_{t,d,j}$  designates the price for the maximum incremental quantity of *thirty-minute operating reserve* in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,d}^{30R}$ ;
- 3.2.34.4  $QXL_{t,d,j}$  designates the maximum quantity of *energy* for which the export at bus  $b$  in time-step  $t \in TS$  may be scheduled in association with *bid* lamination  $j \in J_{t,d}^E$ ;
- 3.2.34.5  $Q10NXL_{t,d,j}$  designates the quantity of non-synchronized *ten-minute operating reserve* that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,d}^{10N}$ ; and
- 3.2.34.6  $Q30RXL_{t,d,j}$  designates the quantity of *thirty-minute operating reserve* that may be scheduled in time-step  $t \in TS$  in association with *offer* lamination  $j \in J_{t,d}^{30R}$ ;

### IESO Data Parameters

- 3.2.35  $ASDG_{i,b}$  designates the amount of *energy* that a *dispatchable generation resource* is scheduled to provide by the *real-time calculation engine* at bus  $b$  for interval  $i \in I$ ;
- 3.2.36  $COMCYCMW_{i,b}$  designates the MWh constraint placed onto a *resource* that is not modelled as a *pseudo-unit* at bus  $b$  for interval  $i \in I$  to reflect that *resource's* *energy* capability in combined cycle mode;

- 3.2.37  $ExtL10NP_{i,d}^{PD}$  designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* for the *dispatch hour* in which interval  $i \in I$  falls as calculated by Pass 1 of the *pre-dispatch calculation engine*;
- 3.2.38  $ExtL30RP_{i,d}^{PD}$  designates the *locational marginal price* for *thirty-minute operating reserve* for the *dispatch hour* in which interval  $i \in I$  falls as calculated by Pass 1 of the *pre-dispatch calculation engine*;
- 3.2.39  $FG_{i,b}$  designates the IESO's centralized *variable generation* forecast for a *variable generation resource* identified by bus  $b$  for interval  $i \in I$ ;
- 3.2.40  $LMP_{i,b}^1$  designates the *locational marginal price* for *energy* in interval  $i \in I$  as determined by Pass 1 of the *real-time calculation engine*;
- 3.2.41  $L10SP_{i,b}^1$  designates the *locational marginal price* for synchronized *ten-minute operating reserve* in interval  $i \in I$  as determined by Pass 1 of the *real-time calculation engine*;
- 3.2.42  $L10NP_{i,b}^1$  designates the *locational marginal price* for non-synchronized *ten-minute operating reserve* in interval  $i \in I$  as determined by Pass 1 of the *real-time calculation engine*;
- 3.2.43  $L30RP_{i,b}^1$  designates the *locational marginal price* for *thirty-minute operating reserve* in interval  $i \in I$  as determined by Pass 1 of the *real-time calculation engine*;
- 3.2.44  $REGULATIONMW_{h,b}$  designates the MWh constraint placed onto a *resource* at bus  $b$  for interval  $i \in I$  for *regulation*; and
- 3.2.45  $SEALMW_{i,b}$  designates the MWh constraint placed onto a *resource* at bus  $b$  for interval  $i \in I$  for actions taken to ensure the safety of any person, prevent the damage of equipment, or prevent the violation of any *applicable law*.

### 3.3 Objective Functions

- 3.3.1 The objective functions for the Real-Time Market Lost Cost Economic Operating Point calculation shall solve for the following variables:
- 3.3.1.1  $ESDG_{i,b,kr}$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with *offer lamination*  $k \in K_{i,b}^E$ ;
- 3.3.1.2  $ES10SDG_{i,b,kr}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is

scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10S}$ ;

3.3.1.3  $ES10NDG_{i,b,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{10N}$ ;

3.3.1.4  $ES30RDG_{i,b,k}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,b}^{30R}$ ;

3.3.1.5  $ESIG_{i,d,k}$  which designates the amount of *dispatchable* imports scheduled at bus  $d \in DI$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,d}^E$ ;

3.3.1.6  $ES10NIG_{i,d,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* scheduled at bus  $d \in DI$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,d}^E$ ;

3.3.1.7  $ES30RIG_{i,d,k}$  which designates the amount of *thirty-minute operating reserve* scheduled at bus  $d \in DI$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,d}^E$ ;

3.3.1.8  $ESDL_{i,b,j}$  which designates the amount of *energy* that a *dispatchable load* scheduled at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^E$ ;

3.3.1.9  $ES10SDL_{i,b,j}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10S}$ ;

3.3.1.10  $ES10NDL_{i,b,j}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10N}$ ;

- 3.3.1.11  $ES30RDL_{i,b,j}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{30R}$ ;
- 3.3.1.12  $ESXL_{i,d,k}$  which designates the amount of *dispatchable* imports scheduled at bus  $d \in DX$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,d}^E$ ;
- 3.3.1.13  $ES10NXL_{i,d,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* scheduled at bus  $d \in DX$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,d}^E$ ; and
- 3.3.1.14  $ES30RXL_{i,d,k}$  which designates the amount of *thirty-minute operating reserve* scheduled at bus  $d \in DX$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,d}^E$ .

3.3.2 For each of the following *resource* types, the objective function for determining an RT LC EOP will maximize the value of the following expressions:

3.3.2.1 For *dispatchable generation resources*:

$$ObjSDG = \sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \cdot (LMP_{i,b}^1 - PDG_{i,b,k})$$

$$Obj10SDG = \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} \cdot (L10SP_{i,b}^1 - P10SDG_{i,b,k})$$

$$Obj10NDG = \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} \cdot (L10NP_{i,b}^1 - P10NDG_{i,b,k})$$

$$Obj30RDG = \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \cdot (L30RP_{i,b}^1 - P30RDG_{i,b,k})$$

3.3.2.2 For *dispatchable loads*:

$$ObjSDL_i = \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \cdot (PDL_{i,b,j} - LMP_{i,b}^1)$$

$$Obj10SDL_i = \sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} \cdot (P10SDL_{i,b,j} - L10SP_{i,b}^I)$$

$$Obj10NDL_i = \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} \cdot (P10NDL_{i,b,j} - L10NP_{i,b}^I)$$

$$Obj30RDL_i = \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} \cdot (P30RDL_{i,b,j} - L30RP_{i,b}^I)$$

3.3.2.3 For import transactions associated with *boundary entity resources*:

$$ObjSIG_i = \sum_{k \in K_{i,d}^E} ESIG_{i,d,k} \cdot (ExtLMP_{i,d}^{PD} - PIG_{t,d,k})$$

$$Obj10NIG_i = \sum_{k \in K_{i,d}^{10N}} ES10NIG_{i,d,k} \cdot (ExtL10NP_{i,d}^{PD} - P10NIG_{t,d,k})$$

$$Obj30RIG_i = \sum_{k \in K_{i,d}^{30R}} ES30RIG_{i,d,k} \cdot (ExtL30RP_{i,d}^{PD} - P30RIG_{t,d,k})$$

3.3.2.4 For export transactions associated with *boundary entity resources*:

$$ObjSXL_i = \sum_{j \in J_{i,d}^E} ESXL_{i,d,j} \cdot (PXL_{t,d,j} - ExtLMP_{i,d}^{PD})$$

$$Obj10NXL_i = \sum_{j \in J_{i,d}^{10N}} ES10NXL_{i,d,j} \cdot (P10NXL_{t,d,j} - ExtL10NP_{i,d}^{PD})$$

$$Obj30RXL_i = \sum_{j \in J_{i,d}^{30R}} ES30RXL_{i,d,j} \cdot (P30RXL_{t,d,j} - ExtL30RP_{i,d}^{PD})$$

### 3.4 Constraints

3.4.1 The constraints described in this section 3.4 shall apply to the objective functions used for the RT LC EOP calculation.

#### Scheduling Variable Bounds

3.4.2 No RT LC EOP shall be negative, nor shall any RT LC EOP exceed the *offer* or *bid* quantity for *energy* or the *offer* quantity for *operating reserve*. For all intervals  $i \in I$ :

$0 \leq ESDL_{i,b,j} \leq QDL_{i,b,j}$	for all $b \in B^{DL}, j \in J_{i,b}^E$ ;
$0 \leq ES10SDL_{i,b,j} \leq Q10SDL_{i,b,j}$	for all $b \in B^{DL}, j \in J_{i,b}^{10S}$ ;
$0 \leq ES10NDL_{i,b,j} \leq Q10NDL_{i,b,j}$	for all $b \in B^{DL}, j \in J_{i,b}^{10N}$ ;
$0 \leq ES30RDL_{i,b,j} \leq Q30RDL_{i,b,j}$	for all $b \in B^{DL}, j \in J_{i,b}^{30R}$ ;
$0 \leq ESDG_{i,b,k} \leq QDG_{i,b,k}$	for all $b \in B^{DG}, k \in K_{i,b}^E$ ;
$0 \leq ES10SDG_{i,b,k} \leq Q10SDG_{i,b,k}$	for all $b \in B^{DG}, k \in K_{i,b}^{10S}$ ;
$0 \leq ES10NDG_{i,b,k} \leq Q10NDG_{i,b,k}$	for all $b \in B^{DG}, k \in K_{i,b}^{10N}$ ;
$0 \leq ES30RDG_{i,b,k} \leq Q30RDG_{i,b,k}$	for all $b \in B^{DG}, k \in K_{i,b}^{30R}$ ;
$0 \leq ESDX_{i,d,j} \leq QXL_{t,d,j}$	for all $d \in DX, j \in J_{t,d}^E$ ;
$0 \leq ES10NXL_{i,d,j} \leq Q10NXL_{t,d,j}$	for all $d \in DX, j \in J_{t,d}^{10N}$ ;
$0 \leq ES30RXL_{i,d,j} \leq Q30RXL_{t,d,j}$	for all $d \in DX, j \in J_{t,d}^{30R}$ ;
$0 \leq ESIG_{i,d,k} \leq QIG_{t,d,k}$	for all $d \in DI, k \in K_{t,d}^E$ ;
$0 \leq ES10NIG_{i,d,k} \leq Q10NIG_{t,d,k}$	for all $d \in DI, k \in K_{t,d}^{10N}$ ;
$0 \leq ES30RIG_{i,d,k} \leq Q30RIG_{t,d,k}$	for all $d \in DI, k \in K_{t,d}^{30R}$ ;

3.4.3 Subject to section 3.4.4, the RT LC EOP for a *non-quick start resource* shall be greater than or equal to its *minimum loading point* for interval  $i \in I$  and bus  $b \in B^{NQS}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \geq MinQDG_b$$

3.4.4 The RT LC EOP for a *non-quick start resource* shall be equal to its *real-time schedule* when it is scheduled below its *minimum loading point* for interval  $i \in I$  and bus  $b \in B^{NQS}$ :



If  $\sum_{k \in K_{i,b}^E} ASDG_{i,b,k} < MinQDG_b$  for  $b \in B^{NQS}$  then:

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} = ASDG_{i,b}$$

### Constraints for Regulation Requirements

3.4.5 For a *dispatchable generation resource*, its RT LC EOP for *energy* shall be greater than or equal to any *regulation* constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \geq REGULATIONMW_{i,b}$$

3.4.6 For a *dispatchable generation resource*, its RT LC EOP for *energy* and each class of *operating reserve* shall not exceed the maximum available capacity the *resource* has less the *regulation* constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \leq AdjMaxDG_{i,b} - REGULATIONMW_{i,b}$$

$$\sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} \leq AdjMaxDG_{i,b} - REGULATIONMW_{i,b}$$

$$\sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} \leq AdjMaxDG_{i,b} - REGULATIONMW_{i,b}$$

$$\sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \leq AdjMaxDG_{i,b} - REGULATIONMW_{i,b}$$

### Constraints for Market Participant Requirements

3.4.7 For a *dispatchable generation resource*, its RT LC EOP for *energy* shall be greater than or equal to any minimum  $SEALMW_{i,b}$  constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \geq SEALMW_{i,b}$$

- 3.4.8 For a *dispatchable load*, its RT LC EOP for *energy* shall be greater than or equal to any minimum  $SEALMW_{i,b}$  constraint that is applied and for each class of *operating reserve*, the RT LC EOP shall be less than or equal to the RT LC EOP for *energy* for that *resource* less any minimum  $SEALMW_{i,b}$  constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \geq SEALMW_{i,b}$$

$$\sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} - SEALMW_{i,b}$$

$$\sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} - SEALMW_{i,b}$$

$$\sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} - SEALMW_{i,b}$$

- 3.4.9 For a *dispatchable generation resource*, its RT LC EOP for *energy* shall be less than or equal to any maximum  $SEALMW_{i,b}$  constraint applied for all intervals  $i \in I$  and buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \leq SEALMW_{i,b}$$

- 3.4.10 For a *dispatchable load*, its RT LC EOP for *energy* shall be less than or equal to any maximum  $SEALMW_{i,b}$  constraint applied for all intervals  $i \in I$  and buses  $b \in B^{DG}$ :

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \leq SEALMW_{i,b}$$

- 3.4.11 For a *dispatchable generation resource*, its RT LC EOP for *energy* shall be equal to any fixed  $SEALMW_{i,b}$  constraint applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} = SEALMW_{i,b}$$

- 3.4.12 For a *dispatchable load*, its RT LC EOP for *energy* shall be equal to any fixed  $SEALMW_{h,b}$  constraint that is applied and equal to zero for each class of *operating reserve* for interval  $i \in I$  and buses  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} = SEALMW_{i,b}$$

$$\sum_{j \in J_{h,b}^{10S}} ES10SDL_{i,b,k} = 0$$

$$\sum_{j \in J_{h,b}^{10N}} ES10NDL_{i,b,k} = 0$$

$$\sum_{j \in J_{h,b}^{30R}} ES30RDL_{i,b,k} = 0$$

- 3.4.13 For a *dispatchable load*, its RT LC EOP for *energy* shall be greater than or equal to the *bid* quantity for *energy* priced at the *maximum market clearing price*:

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \geq QDLFIRM_{i,b}$$

- 3.4.14 For a *dispatchable load*, its RT LC EOP for *operating reserve* shall be less than or equal its RT LC EOP for *energy* less the *bid* quantity for *energy* priced at the *maximum market clearing price*:

$$\sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} - QDLFIRM_{i,b}$$

$$\sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} - QDLFIRM_{i,b}$$

$$\sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} - QDLFIRM_{i,b}$$

### Constraints for Operating Reserve Ramping

- 3.4.15 For a *dispatchable generation resource* with  $RLP10S_{h,b} > 0$ , the amount of *ten-minute operating reserve* that the *resource* is scheduled to provide shall be less

than or equal to its *reserve loading point* for *ten-minute operating reserve* and , the following constraint shall apply for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} \leq \left( \sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \right) \cdot \left( \frac{1}{RLP10S_{i,b}} \right) \cdot \left( \min \left\{ 10 \cdot ORRDG_{i,b}, \sum_{k \in K_{i,b}^{10S}} Q10SDG_{i,b,k} \right\} \right)$$

3.4.16 For a *dispatchable generation resource* with  $RLP30R_{h,b} > 0$ , the amount of *thirty-minute operating reserve* that the *resource* is scheduled to provide shall be less than or equal to its *reserve loading point* for *thirty-minute operating reserve* and the following constraint shall apply for all hours  $h \in \{1, \dots, 24\}$  and all buses  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \leq \left( \sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \right) \cdot \left( \frac{1}{RLP30R_{i,b}} \right) \cdot \left( \min \left\{ 30 \cdot ORRDG_{i,b}, \sum_{k \in K_{i,b}^{30R}} Q30RDG_{i,b,k} \right\} \right)$$

### Constraints for Pseudo-units

3.4.17 For a *pseudo-unit*, its RT LC EOP for *energy* for the *dispatchable* region and duct firing region shall be less than or equal to the respective maximum capabilities for those regions for interval  $i \in I$  and bus  $b \in B^{PSU}$ :

$$\sum_{k \in K_{i,b}^{DR}} ESDG_{i,b,k} \leq MaxDR_{i,b}$$

$$\sum_{k \in K_{i,b}^{DF}} ESDG_{i,b,k} \leq MaxDF_{i,b}$$

3.4.18 For a *pseudo-unit*, its RT LC EOP for each class of *operating reserve* shall be less than or equal to the sum of the maximum capabilities for its *dispatchable* region and duct firing region for hour  $i \in I$  and bus  $b \in B^{PSU}$ :

$$\sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} \leq MaxDR_{i,b} + MaxDF_{i,b}$$

$$\sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} \leq MaxDR_{i,b} + MaxDF_{i,b}$$

$$\sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \leq MaxDR_{i,b} + MaxDF_{i,b}$$

3.4.19 For a *pseudo-unit* that cannot provide *ten-minute operating reserve* from its duct firing region, the following constraint shall apply:

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} + \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} \leq MINQDG_b + QDR_{i,k}$$

### 3.5 Outputs

3.5.1 The RT LC EOP s used for *settlement* for *energy* and *operating reserve* for all *resources* except *pseudo-unit resources* for each interval of the *dispatch hour* shall be the sum of each RT LC EOP variable determined by the objective function in section 3.3 for that *resource*, subject to constraints in section 3.4 applicable for that *resource* determined as follows:

$$DGEnergyEOP_{i,b}^{LC} = \sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \qquad DG10SEOP_{i,b}^{LC} = \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k}$$

$$DG10NEOP_{i,b}^{LC} = \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k}$$

$$DG30REOP_{i,b}^{LC} = \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k}$$

$$DLEnergyEOP_{i,b}^{LC} = \sum_{j \in J_{i,b}^E} ESDL_{i,b,j}$$

$$DL10SEOP_{i,b}^{LC} = \sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j}$$

$$DL10NEOP_{i,b}^{LC} = \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j}$$

$$DL30REOP_{i,b}^{LC} = \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j}$$

$$DIEnergyEOP_{i,b}^{LC} = \sum_{k \in K_{i,b}^E} ESIG_{i,b,k}$$

$$DI10NEOP_{i,b}^{LC} = \sum_{k \in K_{i,b}^{10N}} ES10NIG_{i,b,k}$$

$$DI30REOP_{i,b}^{LC} = \sum_{k \in K_{i,b}^{30R}} ES30RIG_{i,b,k}$$

$$DXEnergyEOP_{i,b}^{LC} = \sum_{j \in J_{i,b}^E} ESXL_{i,b,j}$$

$$DX10NEOP_{i,b}^{LC} = \sum_{j \in J_{i,b}^{10N}} ES10NXL_{i,b,j}$$

$$DX30REOP_{i,b}^{LC} = \sum_{j \in J_{i,b}^{30R}} ES30RXL_{i,b,j}$$

3.5.2 The RT LC EOPs for *energy* and *operating reserve* for a *pseudo-unit* for each interval of the *dispatch hour*, which will be used for converting the RT LC EOPs

to physical *resource* equivalents in accordance with sections 3.5.3 to 3.5.4, shall be determined as follows:

$$PSUMLP_{EnergyEOP_{i,k}}^{LC} = \sum_{k \in K_{i,b}^{MLP}} ESDG_{i,b,k}$$

$$PSUDRE_{EnergyEOP_{i,k}}^{LC} = \sum_{k \in K_{i,b}^{DR}} ESDG_{i,b,k}$$

$$PSUDF_{EnergyEOP_{i,k}}^{LC} = \sum_{k \in K_{i,b}^{DF}} ESDG_{i,b,k}$$

$$PSU10SE_{EOP_{i,k}}^{LC} = \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k}$$

$$PSU10NE_{EOP_{i,k}}^{LC} = \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k}$$

$$PSU30RE_{EOP_{i,k}}^{LC} = \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k}$$

### Conversion of RT LC EOPs for Pseudo-Units to Physical Resource Equivalents

3.5.3 The RT LC EOP used for *settlement* for *energy* for a combustion turbine and a steam turbine that is associated with *pseudo-unit*  $k \in \{1, \dots, K\}$  in interval  $i$  shall be determined as follows:

$$\begin{aligned} CTE_{EnergyEOP_{i,k}} &= PSUMLP_{EnergyEOP_{i,k}}^{LC} \cdot CTShareMLP_{i,k} + PSUDRE_{EnergyEOP_{i,k}}^{LC} \\ &\quad \cdot CTShareDR_{i,k} \end{aligned}$$

$$\begin{aligned} STE_{EnergyEOP_{i,k}} &= PSUMLP_{EnergyEOP_{i,k}}^{LC} \cdot STShareMLP_k + PSUDRE_{EnergyEOP_{i,k}}^{LC} \\ &\quad \cdot STShareDR_k + PSUDF_{EnergyEOP_{i,k}}^{LC} \end{aligned}$$

3.5.4 The RT LC EOPs used for *settlement* for *operating reserve* for a combustion turbine and a steam turbine that is associated with *pseudo-unit*  $k \in \{1, \dots, K\}$  in interval  $i$  shall be determined as follows and in the following order for each class of *operating reserve*:

$$\begin{aligned}
10SDR_{i,k} &= \min(QDR_{i,k}, PSU10SEOP_{i,k}^{LC}) \\
10NDR_{i,k} &= \min(QDR_{i,k} - 10SDR_{i,k}, PSU10NEOP_{i,k}^{LC}) \\
30RDR_{i,k} &= \min(QDR_{i,k} - 10SDR_{i,k} - 10NDR_{i,k}, PSU30REOP_{i,k}^{LC})
\end{aligned}$$

$$\begin{aligned}
CT10SEOP_{i,k} &= 10SDR_{i,k} \cdot CTShareDR_k \\
ST10SEOP_{i,k} &= 10SDR_{i,k} \cdot STShareDR_k + (PSU10SEOP_{i,k}^{LC} - 10SDR_{i,k}) \\
CT10NEOP_{i,k} &= 10NDR_{i,k} \cdot CTShareDR_k \\
ST10NEOP_{i,k} &= 10NDR_{i,k} \cdot STShareDR_k + (PSU10NEOP_{i,k}^{LC} - 10NDR_{i,k}) \\
CT30REOP_{i,k} &= 30RDR_{i,k} \cdot CTShareDR_k \\
ST30REOP_{i,k} &= 30RDR_{i,k} \cdot STShareDR_k + (PSU30REOP_{i,k}^{LC} - 30RDR_{i,k})
\end{aligned}$$

## 4. Real-Time Market Lost Opportunity Cost Economic Operating Point

### 4.1 Purpose

- 4.1.1 This section describes the process used to determine the lost opportunity cost economic operating point for eligible *resources* in the *real-time market* (RT LOC EOP).

### 4.2 Sets, Indices and Parameters Used by the Real-Time Market Lost Opportunity Cost Economic Operating Point

#### Fundamental Sets and Indices

- 4.2.1 The fundamental inputs used to calculate RT LOC EOP are described in section 3.2.

#### Market Participant Data Parameters

- 4.2.2 In addition to the *market participant* data parameters described in section 3.2, the following parameters are also used to calculate the RT LOC EOP.
- 4.2.3 With respect to a *dispatchable generation resource* identified by bus  $b \in B^{DG}$ :
- 4.2.3.1  $DRRDG_{i,b,w}$  designates the maximum rate in MW per minute at which the *resource* can decrease the amount of *energy* it supplies at  $b \in B^{DG}$  for interval  $i$  while operating in the range between



$RmpRngMaxDG_{i,b,w-1}$  and  $RmpRngMaxDG_{i,b,w}$  for  
 $w \in \{1, \dots, NumRRDG_{i,b}\}_i$

- 4.2.3.2  $NumRRDG_{i,b}$  designates the number of ramp rates provided in time-step  $i \in I$ ; and
- 4.2.3.3  $URRDG_{i,b,w}$  designates the maximum rate in MW per minute at which the *resource* can increase the amount of *energy* it supplies at  $b \in B^{DG}$  for interval  $i \in I$  while operating in the range between  $RmpRngMaxDG_{i,b,w-1}$  and  $RmpRngMaxDG_{i,b,w}$  for  $w \in \{1, \dots, NumRRDG_{i,b}\}_i$

4.2.4 With respect to a *dispatchable load* identified by bus  $b \in B^{DL}$ :

- 4.2.4.1  $DRRDL_{i,b,w}$  designates the maximum rate in MW per minute at which the *resource* can decrease the amount of *energy* it supplies at  $b \in B^{DL}$  for interval  $i \in I$  while operating in the range between  $RmpRngMaxDL_{i,b,w-1}$  and  $RmpRngMaxDL_{i,b,w}$  for  $w \in \{1, \dots, NumRRDL_{i,b}\}_i$
- 4.2.4.2  $NumRRDL_{i,b}$  designates the number of ramp rates provided at  $b \in B^{DL}$  for interval  $i \in I$ ;
- 4.2.4.3  $ORRDL_b$  designates the *operating reserve* ramp rate in MW per minute of reductions in load consumption;
- 4.2.4.4  $RmpRngMaxDG_{i,b,w}$  designates the  $w^{th}$  ramp rate break point provided at  $b \in B^{DG}$  for interval  $i \in I$  where  $w \in \{1, \dots, NumRRDG_{i,b}\}_i$ ;
- 4.2.4.5  $RmpRngMaxDL_{i,b,w}$  designates the  $w^{th}$  ramp rate break point provided at  $b \in B^{DL}$  for interval  $i \in I$  where  $w \in \{1, \dots, NumRRDL_{i,b}\}_i$ ; and
- 4.2.4.6  $URRDL_{i,b,w}$  designates the maximum rate in MW per minute at which the *resource* can increase the amount of *energy* it supplies at  $b \in B^{DL}$  for interval  $i \in I$  while operating in the range between  $RmpRngMaxDL_{i,b,w-1}$  and  $RmpRngMaxDL_{i,b,w}$  for  $w \in \{1, \dots, NumRRDL_{i,b}\}_i$ .

## IESO Data Parameters

- 4.2.5 In addition to the *IESO* data parameters described in section 3.2, the following parameters are also used to calculate the RT LOC EOP.

- 4.2.5.1  $GridConnected_{i,b}$  designates if the *resource* is connected to the *IESO-controlled grid* at bus  $b$  for interval  $i \in I$ ; and
- 4.2.5.2  $RELIABILITYMW_{i,b}$  designates the MWh constraint placed onto a *resource* at bus  $b$  for interval  $i \in I$  for *reliability* purposes.

### 4.3 Objective Functions

- 4.3.1 The objective functions for the Real-Time Market Lost Opportunity Cost Economic Operating Point calculation shall solve for the following variables:
  - 4.3.1.1  $ESDG_{i,b,k}$  which designates the amount of *energy* that a *dispatchable generation resource* is scheduled at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with *offer lamination*  $k \in K_{i,b}^E$ ;
  - 4.3.1.2  $ES10SDG_{i,b,k}$  which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with *offer lamination*  $k \in K_{i,b}^{10S}$ ;
  - 4.3.1.3  $ES10NDG_{i,b,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with *offer lamination*  $k \in K_{i,b}^{10N}$ ;
  - 4.3.1.4  $ES30RDG_{i,b,k}$  which designates the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide at bus  $b \in B^{DG}$  in interval  $i \in I$  in association with *offer lamination*  $k \in K_{i,b}^{30R}$ ;
  - 4.3.1.5  $ESIG_{i,d,k}$  which designates the amount of *energy* that a *boundary entity resource* is scheduled to import from *intertie zone* bus  $d \in DI$  in interval  $i \in I$  in association with *offer lamination*  $k \in K_{i,d}^E$ ;
  - 4.3.1.6  $ES10NIG_{i,d,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *boundary entity resource* is scheduled to provide from *intertie zone* bus  $d \in DI$  in interval  $i \in I$  in association with *offer lamination*  $k \in K_{i,d}^E$ ;
  - 4.3.1.7  $ES30RIG_{i,d,k}$  which designates the amount of *thirty-minute operating reserve* that a *boundary entity resource* is scheduled to provide at bus  $d \in DI$  in interval  $i \in I$  in association with *offer lamination*  $k \in K_{i,d}^E$ ;

- 4.3.1.8  $ESDL_{i,b,j}$ , which designates the amount of *energy* that a *dispatchable load* is scheduled to consume at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with *bid* lamination  $j \in J_{i,b}^E$ ;
- 4.3.1.9  $ES10SDL_{i,b,j}$ , which designates the amount of synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10S}$ ;
- 4.3.1.10  $ES10NDL_{i,b,j}$ , which designates the amount of non-synchronized *ten-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{10N}$ ;
- 4.3.1.11  $ES30RDL_{i,b,j}$ , which designates the amount of *thirty-minute operating reserve* that a *dispatchable load* is scheduled to provide at bus  $b \in B^{DL}$  in interval  $i \in I$  in association with *offer* lamination  $j \in J_{i,b}^{30R}$ ;
- 4.3.1.12  $ESXL_{i,d,k}$  which designates the amount of *energy* a *boundary entity resource* is scheduled to export at *intertie zone* bus  $d \in DX$  in interval  $i \in I$  in association with *bid* lamination  $k \in K_{i,d}^E$ ;
- 4.3.1.13  $ES10NXL_{i,d,k}$  which designates the amount of non-synchronized *ten-minute operating reserve* that a *boundary entity resource* is scheduled to provide at *intertie zone* bus  $d \in DX$  in interval  $i \in I$  in association with *offer* lamination  $k \in K_{i,d}^E$ ;
- 4.3.1.14  $ES30RXL_{i,d,k}$  which designates the amount of *thirty-minute operating reserve* that a *boundary entity resource* is scheduled to provide at *intertie zone* bus  $d \in DX$  in interval  $i$  in association with *offer* lamination  $k \in K_{i,d}^E$ ;
- 4.3.1.15  $ESDGInitSch_{i,b}$  designates the initial schedule for a *dispatchable generation resource* at bus  $b \in B^{DG}$ ; and
- 4.3.1.16  $ESDLInitSch_{i,b}$  designates the initial schedule for a *dispatchable load* at bus  $b \in B^{DL}$ .
- 4.3.2 For each of the following *resource* types, the objective function for determining an RT LOC EOP shall maximize the value of the following expressions:
- 4.3.2.1 For *dispatchable generation resources*:

$$\begin{aligned}
ObjDG_i = \sum_{b \in B^{DG}} \left( \sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \cdot (LMP_{i,b}^1 - PDG_{i,b,k}) \right. \\
+ \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} \cdot (L10SP_{i,b}^1 - P10SDG_{i,b,k}) \\
+ \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} \cdot (L10NP_{i,b}^1 - P10NDG_{i,b,k}) \\
\left. + \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \cdot (L30RP_{i,b}^1 - P30RDG_{i,b,k}) \right)
\end{aligned}$$

4.3.2.2 For *dispatchable loads*:

$$\begin{aligned}
ObjDL_i = \sum_{b \in B^{DL}} \left( \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \cdot (PDL_{i,b,j} - LMP_{i,b}^1) \right. \\
+ \sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} \cdot (P10SDL_{i,b,j} - L10SP_{i,b}^1 - P10SDL_{i,b,j}) \\
+ \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} \cdot (L10NP_{i,b}^1 - P10NDL_{i,b,j} - L10NP_{i,b}^1) \\
\left. + \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} \cdot (L30RP_{i,b}^1 - P30RDL_{i,b,j} - L30RP_{i,b}^1) \right)
\end{aligned}$$

4.3.2.3 For an import transaction at an *intertie metering point* 'i' associated with a *boundary entity resource*:

$$\begin{aligned}
ObjDI_i = \sum_{d \in DI} \left( \sum_{k \in K_{i,d}^E} EDIG_{i,d,k} \cdot (ExtLMP_{i,d}^{PD} - PIG_{t,d,k}) \right. \\
+ \sum_{k \in K_{i,d}^{10N}} ES10NIG_{i,d,k} \cdot (ExtL10NP_{i,d}^{PD} - P10NIG_{t,d,k}) \\
\left. + \sum_{k \in K_{i,d}^{30R}} ES30RIG_{i,d,k} \cdot (ExtL30RP_{i,d}^{PD} - P30RIG_{t,d,k}) \right)
\end{aligned}$$

4.3.2.4 For an export transaction at an *intertie metering point* 'i' associated with a *boundary entity resource*:

$$\begin{aligned}
ObjDX_i = \sum_{d \in DX} & \left( \sum_{j \in J_{i,d}^E} ESXL_{i,d,j} \cdot (PXL_{t,d,j} - ExtLMP_{i,d}^{PD}) \right. \\
& + \sum_{j \in J_{i,d}^{10N}} ES10NXL_{i,d,j} \cdot (ExtL10NP_{i,d}^{PD} - P10NXL_{t,d,j}) \\
& \left. + \sum_{j \in J_{i,d}^{30R}} ES30RXL_{i,d,j} \cdot (ExtL30RP_{i,d}^{PD} - P30RXL_{t,d,j}) \right)
\end{aligned}$$

#### 4.4 Constraints

- 4.4.1 The constraints described in this section 4.4 shall apply to the objective functions used for the RT LOC EOP calculation.

#### Scheduling Variable Bounds

- 4.4.2 No RT LOC EOP shall be negative, nor shall any RT LOC EOP exceed the *offer* or *bid* quantity for *energy* or the *offer* quantity for *operating reserve*. Therefore, for all intervals  $i \in I$ :

$0 \leq ESDL_{i,b,j} \leq QDL_{i,b,j}$	for all $b \in B^{DL}, j \in J_{i,b}^E$ ;
$0 \leq ES10SDL_{i,b,j} \leq Q10SDL_{i,b,j}$	for all $b \in B^{DL}, j \in J_{i,b}^{10S}$ ;
$0 \leq ES10NDL_{i,b,j} \leq Q10NDL_{i,b,j}$	for all $b \in B^{DL}, j \in J_{i,b}^{10N}$ ;
$0 \leq ES30RDL_{i,b,j} \leq Q30RDL_{i,b,j}$	for all $b \in B^{DL}, j \in J_{i,b}^{30R}$ ;
$0 \leq ESG_{i,b,k} \leq QDG_{i,b,k}$	for all $b \in B^{DG}, k \in K_{i,b}^E$ ;
$0 \leq ES10SDG_{i,b,k} \leq Q10SDG_{i,b,k}$	for all $b \in B^{DG}, k \in K_{i,b}^{10S}$ ;
$0 \leq ES10NDG_{i,b,k} \leq Q10NDG_{i,b,k}$	for all $b \in B^{DG}, k \in K_{i,b}^{10N}$ ;
$0 \leq ES30RDG_{i,b,k} \leq Q30RDG_{i,b,k}$	for all $b \in B^{DG}, k \in K_{i,b}^{30R}$ ;
$0 \leq ESX_{i,d,j} \leq QXL_{t,d,j}$	for all $d \in DX, j \in J_{t,d}^E$ ;
$0 \leq ES10NXL_{i,d,j} \leq Q10NXL_{t,d,j}$	for all $d \in DX, j \in J_{t,d}^{10N}$ ;
$0 \leq ES30RXL_{i,d,j} \leq Q30RXL_{t,d,j}$	for all $d \in DX, j \in J_{t,d}^{30R}$ ;
$0 \leq ESDI_{i,d,k} \leq QIG_{t,d,k}$	for all $d \in DI, k \in K_{t,d}^E$ ;
$0 \leq ES10NIG_{i,d,k} \leq Q10NIG_{t,d,k}$	for all $d \in DI, k \in K_{t,d}^{10N}$ ;
$0 \leq ES30RIG_{i,d,k} \leq Q30RIG_{t,d,k}$	for all $d \in DI, k \in K_{t,d}^{30R}$ ;

- 4.4.3 For a *dispatchable generation resource* that is not connected to the *IESO-controlled grid* and is not eligible for *dispatch*, its RT LOC EOP shall be set to zero for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} + \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} = 0$$

- 4.4.4 For a *dispatchable load* that is not connected to the *IESO-controlled grid* and is not eligible for *dispatch*, its RT LOC EOP shall be set to zero for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} + \sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} = 0$$

- 4.4.5 For a *dispatchable load*, the sum of the RT LOC EOP for all classes of *operating reserve* for the *resource* shall not exceed its RT LOC EOP for *energy* for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j}$$

- 4.4.6 For a *dispatchable generation resource*, its RT LOC EOP shall not exceed the maximum available capacity for the *resource* for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$AdjMaxDG_{i,b} = \left\{ \begin{array}{ll} \min \left( \sum_{k \in K_{i,b}^E} QDG_{i,b,k}, Derate_{i,b}, FG_{i,b} \right) & \text{if } b \in B^{VG} \\ \min \left( \sum_{k \in K_{i,b}^E} QDG_{i,b,k}, Derate_{i,b} \right) & \text{otherwise} \end{array} \right\}$$

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} + \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \leq AdjMaxDG_{i,b}$$

- 4.4.7 Subject to section 4.4.8, the RT LOC EOP for a *non-quick start resource* shall be greater than or equal to its *minimum loading point*  $f$  for interval  $i \in I$  and bus  $b \in B^{NQS}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \geq MinQDG_b$$

- 4.4.8 The RT LOC EOP for a *non-quick start resource* shall be equal to its *real-time schedule* when it is scheduled below its *minimum loading point* for interval  $i \in I$  and bus  $b \in B^{NQS}$ :

If  $\sum_{k \in K_{i,b}^E} ASDG_{i,b,k} < MinQDG_b$  for  $b \in B^{NQS}$ , then:

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} = ASDG_{i,b}$$

### Constraints for Reliability Requirements

- 4.4.9 For a *dispatchable generation resource*, its RT LOC EOP shall be greater than or equal to any minimum *reliability* constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \geq RELIABILITYMW_{i,b}$$

- 4.4.10 For a *dispatchable load* its RT LOC EOP shall be greater than or equal to any minimum *reliability* constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DL}$

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,k} \geq RELIABILITYMW_{i,b}$$

- 4.4.11 For a *dispatchable generation resource* its RT LOC EOP for *energy* shall be greater than or equal to any *regulation* constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \geq REGULATIONMW_{i,b}$$

- 4.4.12 For a *dispatchable generation resource*, the sum of RT LOC EOP for *energy* and all classes of *operating reserve* shall be less than or equal to its maximum available capacity less the *regulation* constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} + \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \leq AdjMaxDG_{i,b} - REGULATIONMW_{i,b}$$

### Constraints for Market Participant Requirements

- 4.4.13 For a *dispatchable generation resource*, its RT LOC EOP for *energy* shall be greater than or equal to any minimum  $SEALMW_{i,b}$  constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \geq SEALMW_{i,b}$$

- 4.4.14 For a *dispatchable load*, its RT LOC EOP for *energy* shall be greater than or equal to any minimum  $SEALMW_{i,b}$  constraint that is applied and the sum of RT LOC EOP for all classes of *operating reserve* shall be less than or equal to the RT LOC EOP for *energy* for that *resource* less the minimum  $SEALMW_{i,b}$  constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \geq SEALMW_{i,b}$$

$$\sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} - SEALMW_{i,b}$$

- 4.4.15 For a *dispatchable generation resource*, the sum of its RT LOC EOPs for *energy* shall be less than or equal to any maximum  $SEALMW_{i,b}$  constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \leq SEALMW_{i,b}$$

- 4.4.16 For a *dispatchable load*, its RT LOC EOP for *energy* shall be less than or equal to any maximum  $SEALMW_{i,b}$  constraint that is applied for interval  $i \in I$  and buses  $b \in B^{DL}$ :



$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \leq SEALMW_{i,b}$$

- 4.4.17 For a *dispatchable generation resource*, its RT LOC EOP for *energy* shall be equal to any fixed  $SEALMW_{i,b}$  constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} = SEALMW_{i,b}$$

- 4.4.18 For a *dispatchable load*, its RT LOC EOP for *energy* shall be equal to any fixed  $SEALMW_{i,b}$  constraint that is applied and equal to zero for each class of *operating reserve* for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} = SEALMW_{i,b}$$

$$\sum_{j \in J_{h,b}^{10S}} ES10SDL_{i,b,k} = 0$$

$$\sum_{j \in J_{h,b}^{10N}} ES10NDL_{i,b,k} = 0$$

$$\sum_{j \in J_{h,b}^{30R}} ES30RDL_{i,b,k} = 0$$

- 4.4.19 For a *dispatchable non-quick start resource* that is not being modelled as a *pseudo-unit*, its RT LOC EOP for *energy* shall be greater than or equal to the  $COMCYCMW_{i,b}$  constraint that is applied for interval  $i \in I$  and bus  $b \in B^{DG}$  :

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \geq COMCYCMW_{i,b}$$

- 4.4.20 For a *dispatchable load*, its RT LOC EOP for *energy* shall be greater than or equal to the *bid* quantity for *energy* priced at the *maximum market clearing price* for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \geq QDLFIRM_{i,b}$$

- 4.4.21 For a *dispatchable load*, the sum of RT LOC EOPs for all classes of *operating reserve* shall not exceed the RT LOC EOP for *energy* less the *bid* quantity for *energy* priced at the *maximum market clearing price* for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} - QDLFIRM_{i,b}$$

### Constraints for Operating Reserve Ramping

- 4.4.22 For a *dispatchable resource*, the upper bound of the RT LOC EOP for all classes of *operating reserve* shall be less than or equal to its *operating reserve* ramp rates as follows:

- 4.4.22.1 For a *dispatchable generation resource*, for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$\sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} + \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \leq 30 \cdot ORRDG_b$$

$$\sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} \leq 10 \cdot ORRDG_b$$

- 4.4.22.2 For a *dispatchable load*, for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$\sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} + \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j} \leq 30 \cdot ORRD L_b$$

$$\sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j} + \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j} \leq 10 \cdot ORRD L_b$$

- 4.4.23 For a *dispatchable generation resource* with  $RLP10S_{i,b} > 0$ , the amount of *ten-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall be less than or equal to its *reserve loading point* for *ten-minute operating reserve*:

$$\sum_{k \in K_{i,b}^{10S}} ESDG_{i,b,k} \leq \left( \sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \right) \cdot \left( \frac{1}{RLP10S_{i,b}} \right) \cdot \left( \min \left\{ 10 \cdot ORRDG_b, \sum_{k \in K_{i,b}^{10S}} Q10SDG_{i,b,k} \right\} \right)$$

- 4.4.24 For all *dispatchable generation resources* with  $RLP30R_{i,b} > 0$ , the amount of *thirty-minute operating reserve* that a *dispatchable generation resource* is scheduled to provide shall be less than or equal to its *reserve loading point* for *thirty-minute operating reserve*:

$$\sum_{k \in K_{i,b}^{30R}} ESDG_{i,b,k} \leq \left( \sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \right) \cdot \left( \frac{1}{RLP30R_{i,b}} \right) \cdot \left( \min \left\{ 30 \cdot ORRDG_b, \sum_{k \in K_{i,b}^{30R}} Q30RDG_{i,b,k} \right\} \right)$$

### Constraints for Energy Ramping

- 4.4.25 With the exception of the first *interval* of each *dispatch day*, the RT LOC EOP shall use its RT LOC EOP for the prior interval as its initial starting point as follows:

- 4.4.25.1 For a *dispatchable generation resource*, its RT LOC EOP for *energy* cannot vary by more than five minutes of the *resource's energy* ramping capability for interval  $i \in I$  and bus  $b \in B^{DG}$ :

$$ESDGInitSch_{i,b} - 5 \cdot DRRDG_{i,b,w} \leq \sum_{k \in K_{i,b}^E} ESDG_{i,b,k} \leq ESGDInitSch_{i,b} + 5 \cdot URRDG_{i,b,w}$$

- 4.4.25.2 For a *dispatchable load*, its RT LOC EOP for *energy* cannot vary by more than five minutes of the *resource's energy* ramping capability for interval  $i \in I$  and bus  $b \in B^{DL}$ :

$$ESDLInitSch_{i,b} - 5 \cdot DRRDL_{i,b,w} \leq \sum_{j \in J_{i,b}^E} ESDL_{i,b,j} \leq ESGDInitSch_{i,b} + 5 \cdot URRDL_{i,b,w}$$

### Constraints for Pseudo-Units

- 4.4.26 For a *pseudo-unit*, its RT LOC EOP for *energy* for the *dispatchable* region and duct firing region shall be less than or equal to the respective maximum capabilities for those regions for interval  $i \in I$  and bus  $b \in B^{PSU}$ :

$$\sum_{k \in K_{i,b}^{DR}} ESDG_{i,b,k} \leq MaxDR_{i,b}$$

$$\sum_{k \in K_{i,b}^{DF}} ESDG_{i,b,k} \leq MaxDF_{i,b}$$

- 4.4.27 For a *pseudo-unit*, the sum of its RT LOC EOP for *energy* and the RT LOC EOP s for all classes of *operating reserve* shall be less than or equal to the sum of the maximum capabilities for its *dispatchable* region and duct firing region for interval  $i \in I$  and bus  $b \in B^{PSU}$

$$\begin{aligned} \sum_{k \in K_{i,b}^{DR}} ESDG_{i,b,k} + \sum_{k \in K_{i,b}^{DF}} ESDG_{i,b,k} + \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} \\ + \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k} \leq MaxDR_{i,b} + MaxDF_{i,b} \end{aligned}$$

- 4.4.28 For a *pseudo-unit* that cannot provide *ten-minute operating reserve* in from its duct firing region, the following constraint shall apply:

$$\sum_{k \in K_{i,b}^E} ESDG_{i,b,k} + \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k} + \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k} \leq MINQDG_b + QDR_{i,k}$$

## 4.5 Outputs

- 4.5.1 The RT LOC EOP s used for *settlement* for *energy* and *operating reserve* for all *resources* except *pseudo-units* for each hour of the *dispatch day* shall be the sum of each RT LOC EOP variable determined by the objective function in section 4.3 for that *resource*, subject to constraints in section 4.4 applicable for that *resource* determined as follows:

$$DGEnergyEOP_{i,b}^{LOC} = \sum_{k \in K_{i,b}^E} ESDG_{i,b,k}$$

$$DG10SEOP_{i,b}^{LOC} = \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k}$$

$$DG10NEOP_{i,b}^{LOC} = \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k}$$

$$DG30REOP_{i,b}^{LOC} = \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k}$$

$$DLEnergyEOP_{i,b}^{LOC} = \sum_{j \in J_{i,b}^E} ESDL_{i,b,j}$$

$$DL10SEOP_{i,b}^{LOC} = \sum_{j \in J_{i,b}^{10S}} ES10SDL_{i,b,j}$$

$$DL10NEOP_{i,b}^{LOC} = \sum_{j \in J_{i,b}^{10N}} ES10NDL_{i,b,j}$$

$$DL30REOP_{i,b}^{LOC} = \sum_{j \in J_{i,b}^{30R}} ES30RDL_{i,b,j}$$

$$DLEnergyEOP_{i,b}^{LOC} = \sum_{k \in K_{i,b}^E} ESDI_{i,b,k}$$

$$DI10NEOP_{i,b}^{LOC} = \sum_{k \in K_{i,b}^{10N}} ES10NDI_{i,b,k}$$

$$DI30REOP_{i,b}^{LOC} = \sum_{k \in K_{i,b}^{30R}} ES30RDI_{i,b,k}$$

$$DXEnergyEOP_{i,b}^{LOC} = \sum_{j \in J_{i,b}^E} ESDX_{i,b,j}$$

$$DX10NEOP_{i,b}^{LOC} = \sum_{j \in J_{i,b}^{10N}} ES10NDX_{i,b,j}$$

$$DX30REOP_{i,b}^{LOC} = \sum_{j \in J_{i,b}^{30R}} ES30RDX_{i,b,j}$$

4.5.2 The RT LOC EOPs for *energy* and *operating reserve* for a *pseudo-unit* for each interval of the *dispatch hour*, which will be used for converting the RT LOC EOPs to physical *resource* equivalents in accordance with sections 4.5.3 to 4.5.4, shall be determined as follows:

$$PSUMLPEnergyEOP_{i,k}^{LOC} = \sum_{k \in K_{i,b}^{MLP}} ESDG_{i,b,k}$$

$$PSUDREnergyEOP_{i,k}^{LOC} = \sum_{k \in K_{i,b}^{DR}} ESDG_{i,b,k}$$

$$PSUDFEnergyEOP_{i,k}^{LOC} = \sum_{k \in K_{i,b}^{DF}} ESDG_{i,b,k}$$

$$PSU10SEOP_{i,k}^{LOC} = \sum_{k \in K_{i,b}^{10S}} ES10SDG_{i,b,k}$$

$$PSU10NEOP_{i,k}^{LOC} = \sum_{k \in K_{i,b}^{10N}} ES10NDG_{i,b,k}$$

$$PSU30REOP_{i,k}^{LOC} = \sum_{k \in K_{i,b}^{30R}} ES30RDG_{i,b,k}$$

### Conversion of RT LOC EOPs for Pseudo-Units to Physical Resource Equivalents

- 4.5.3 The RT LOC EOP *energy* and *operating reserve* for a combustion turbine and steam turbine that is associated with *pseudo-unit*  $k \in \{1, \dots, K\}$  in interval  $i$  shall be determined as follows:

$$\begin{aligned} CTEnergyEOP_{i,k} &= PSUMLPEnergyEOP_{i,k}^{LOC} \cdot CTShareMLP_k + PSUDREnergyEOP_{i,k}^{LOC} \\ &\quad \cdot CTShareDR_k \end{aligned}$$

$$\begin{aligned} STEnergyEOP_{i,k} &= PSUMLPEnergyEOP_{i,k}^{LOC} \cdot STShareMLP_k + PSUDREnergyEOP_{i,k}^{LOC} \\ &\quad \cdot STShareDR_k + PSUDFEnergyEOP_{i,k}^{LOC} \end{aligned}$$

- 4.5.4 The RT LOC EOPs used for *settlement* for *operating reserve* for a combustion turbine and a steam turbine that is associated with *pseudo-unit*  $k \in \{1, \dots, K\}$  in interval  $i$  shall be determined as follows and in the following order for each class of *operating reserve*:

$$RoomDR_{i,k} = QDR_{i,k} - PSUDREnergyEOP_{i,k}^{LOC}$$

$$10SDR_{i,k} = \min(RoomDR_{i,k}, PSU10SEOP_{i,k}^{LOC})$$

$$10NDR_{i,k} = \min(RoomDR_{i,k} - 10SDR_{i,k}, PSU10NEOP_{i,k}^{LOC})$$

$$30RDR_{i,k} = \min(RoomDR_{i,k} - 10SDR_{i,k} - 10NDR_{i,k}, PSU30REOP_{i,k}^{LOC})$$

$$CT10SEOP_{i,k} = 10SDR_{i,k} \cdot CTShareDR_k$$

$$ST10SEOP_{i,k} = 10SDR_{i,k} \cdot STShareDR_k + (PSU10NEOP_{i,k}^{LOC} - 10SDR_{i,k})$$

$$CT10NEOP_{i,k} = 10NDR_{i,k} \cdot CTShareDR_k$$

$$ST10NEOP_{i,k} = 10NDR_{i,k} \cdot STShareDR_k + (PSU10NEOP_{i,k}^{LOC} - 10NDR_{i,k})$$

$$CT30REOP_{i,k} = 30RDR_{i,k} \cdot CTShareDR_k$$

$$ST30REOP_{i,k} = 30RDR_{i,k} \cdot STShareDR_k + (PSU30REOP_{i,k}^{LOC} - 30RDR_{i,k})$$